



# Multiple View Geometry Applications to Robotic and Video Manipulation

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200507022

International Institute Of Information Technology

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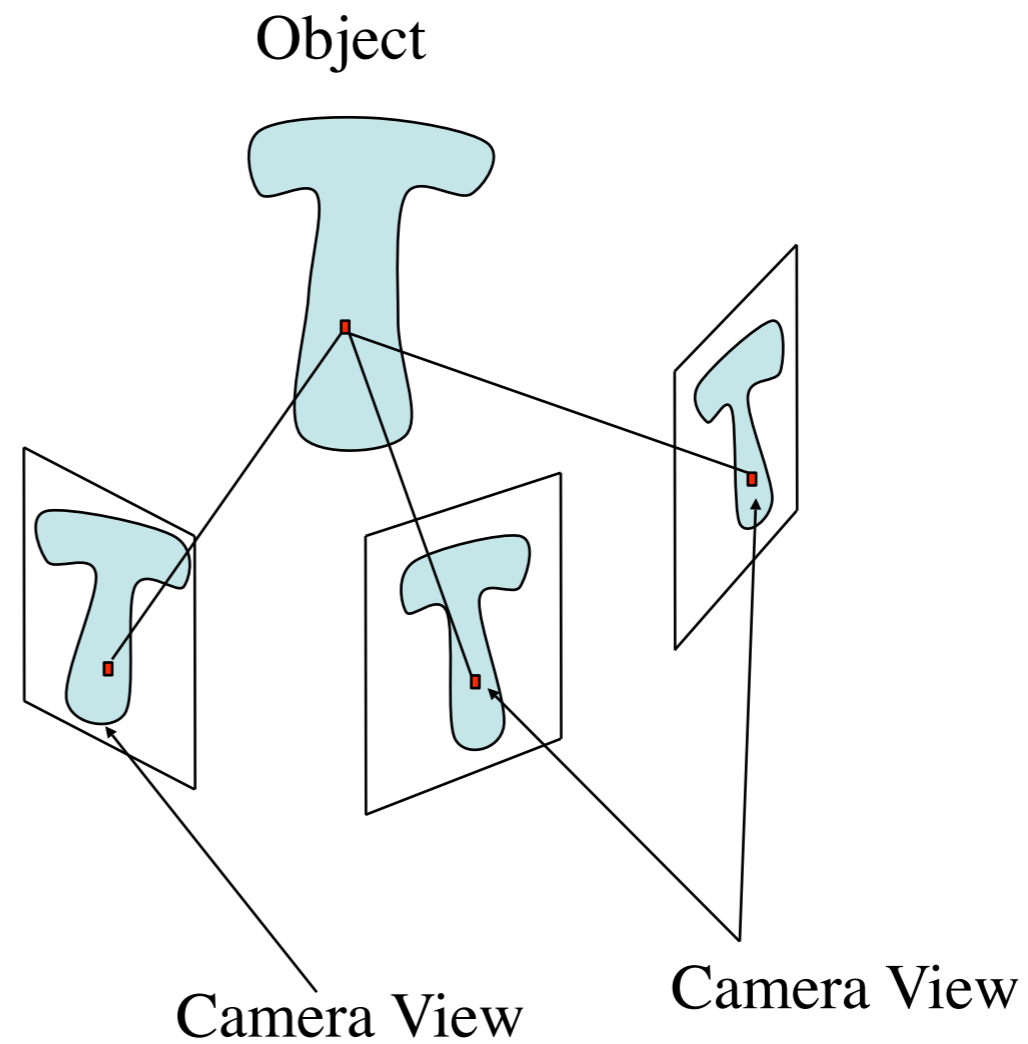


# Multiple View Geometry



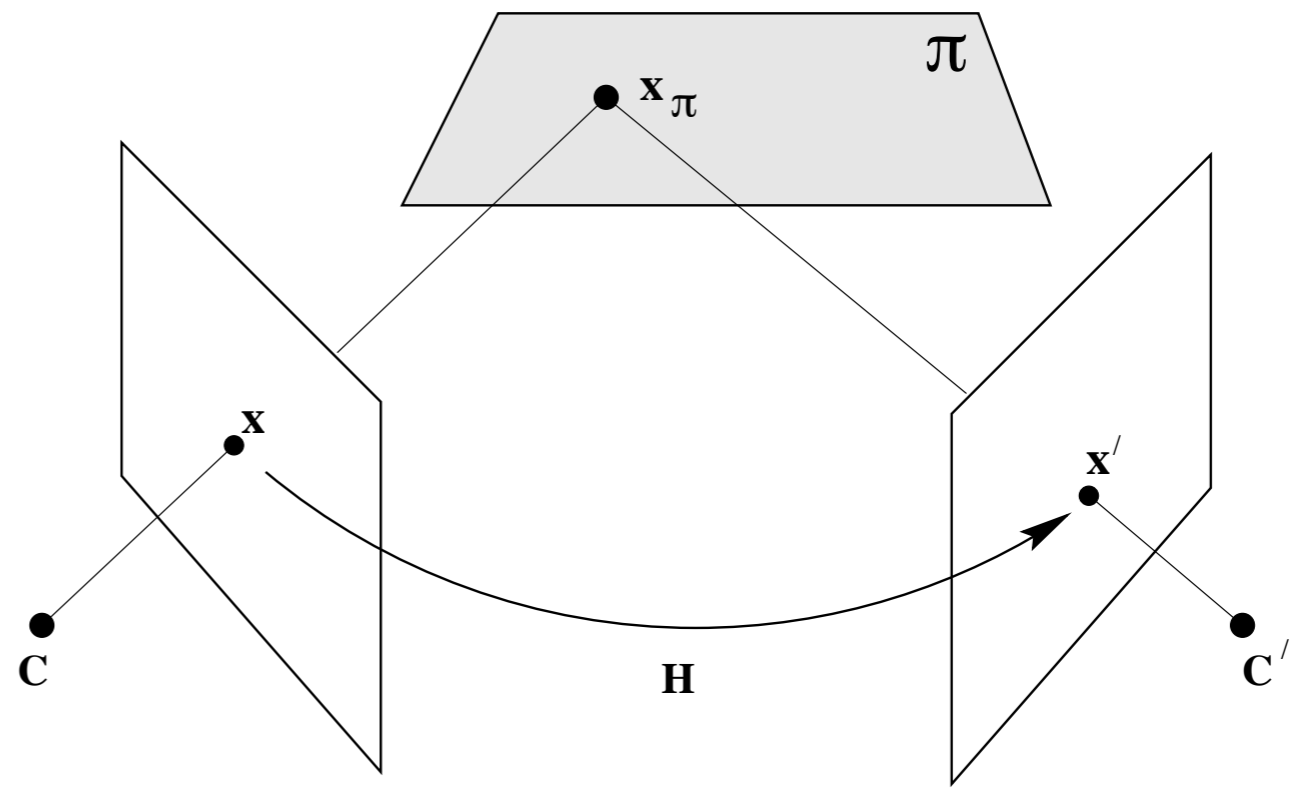
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- As name states, geometry of multiple views!



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- Our focus, geometry governing images of planes.





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# Multiple View Geometry Applications



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- Robotics





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# Multiple View Geometry Applications

- Robotics
- Mosaicing



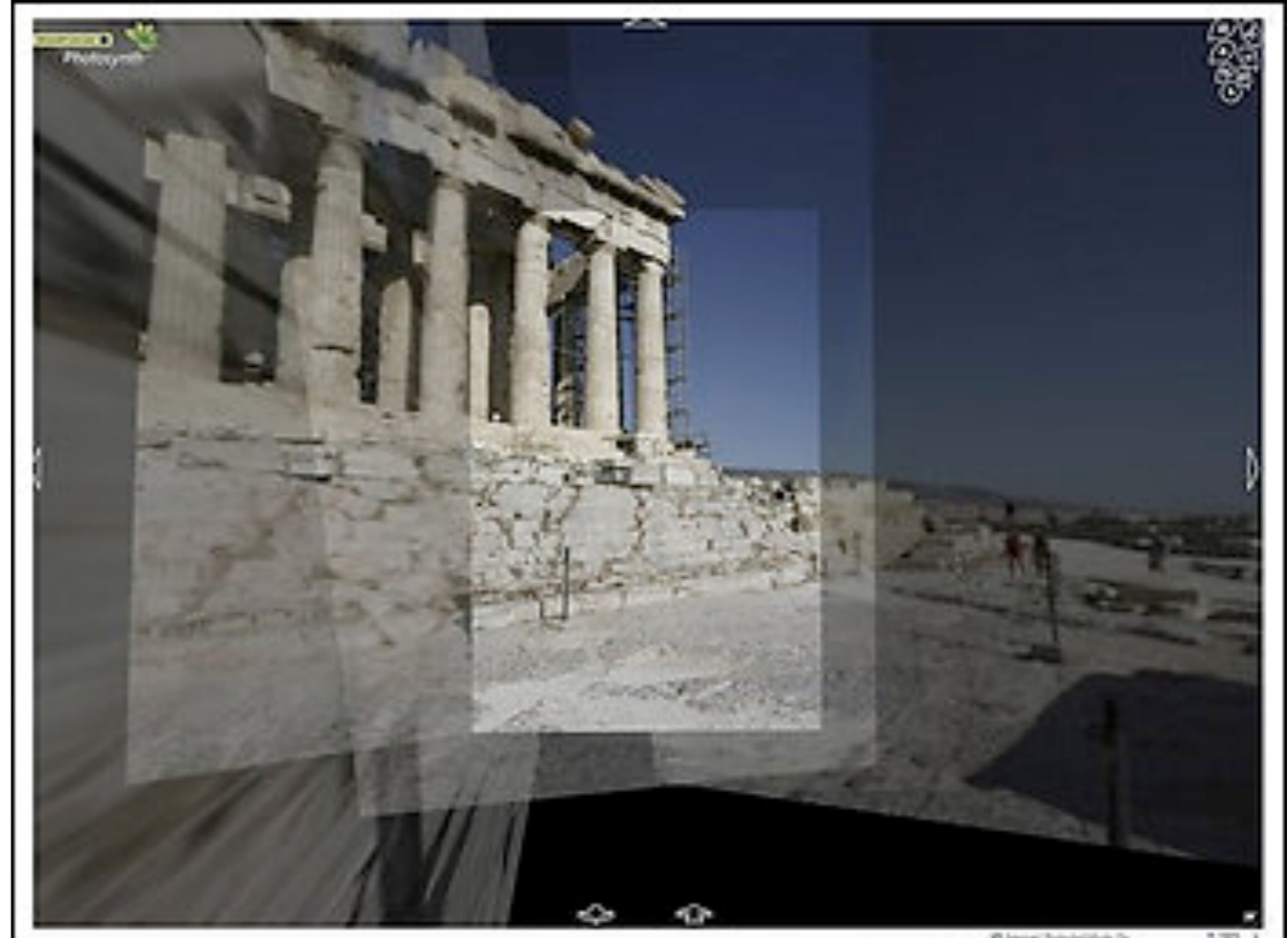


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- Robotics
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- Image Based Rendering





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# Thesis Contributions



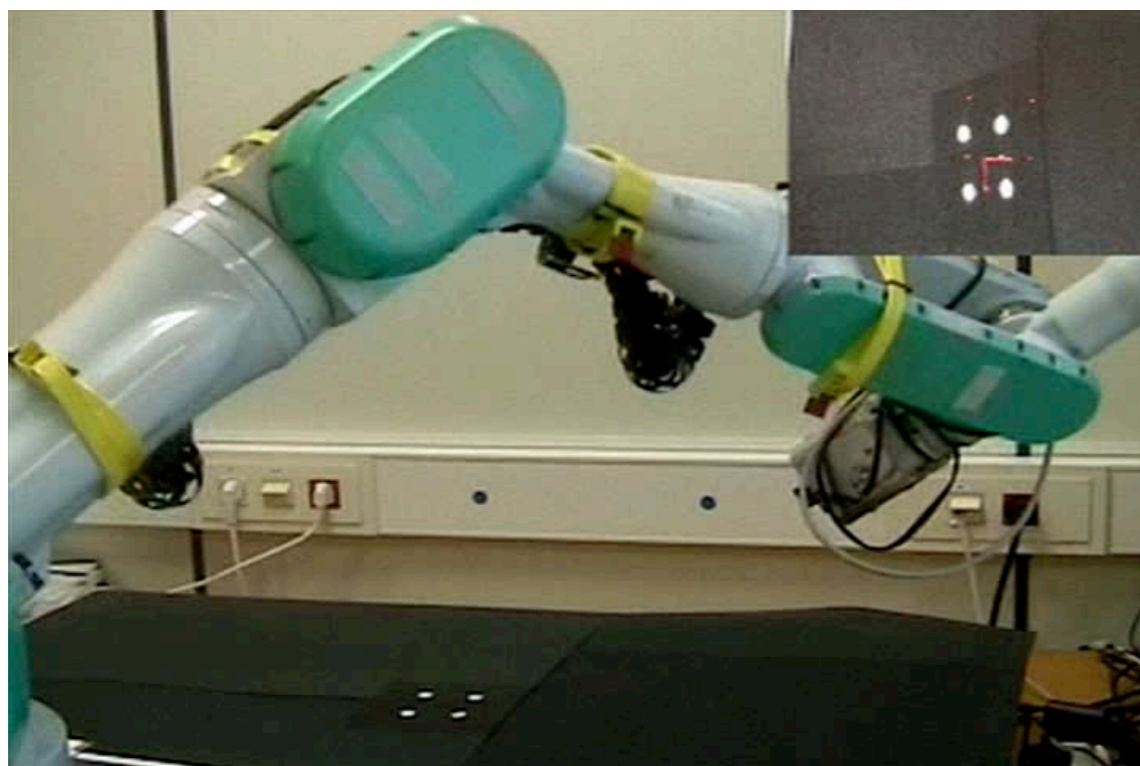
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New Algorithms for Robotic and  
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- Video Manipulation.

New Algorithms for Robotic and Video Manipulation

Tracking  
Single Plane

Visual  
Servoing

Tracking  
Multiple Planes

Video  
Inpainting

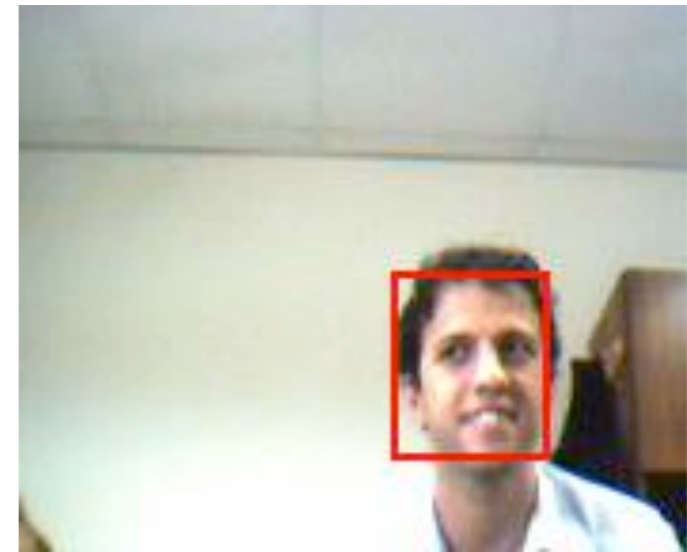
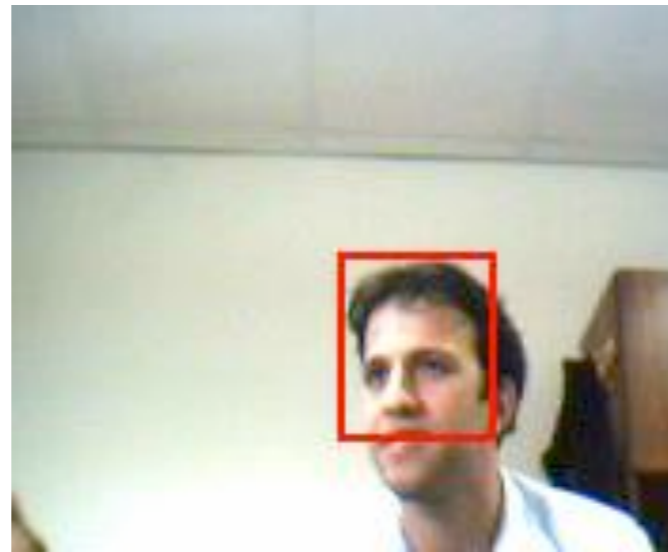
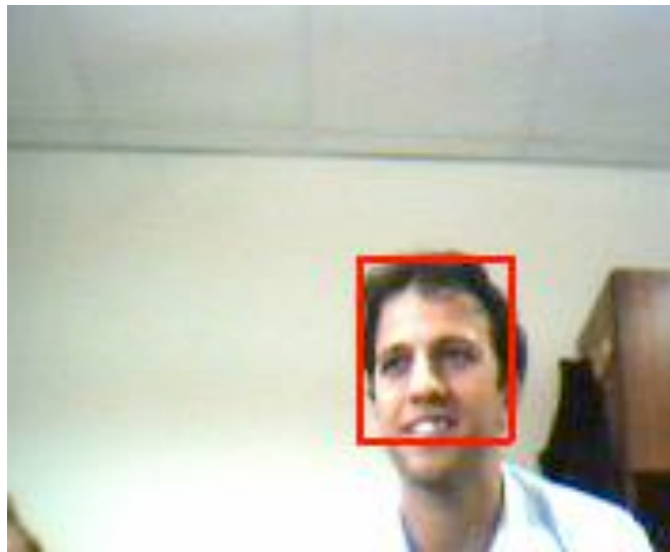
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# Tracking: Past Work

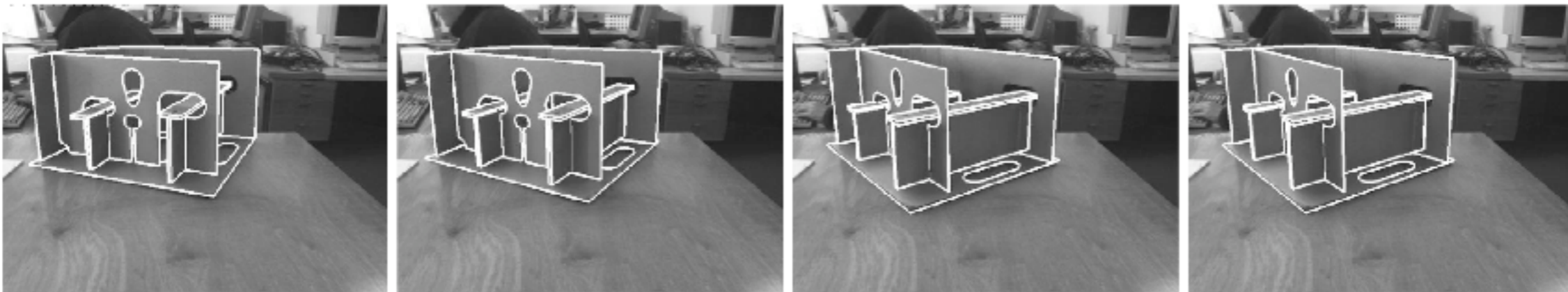
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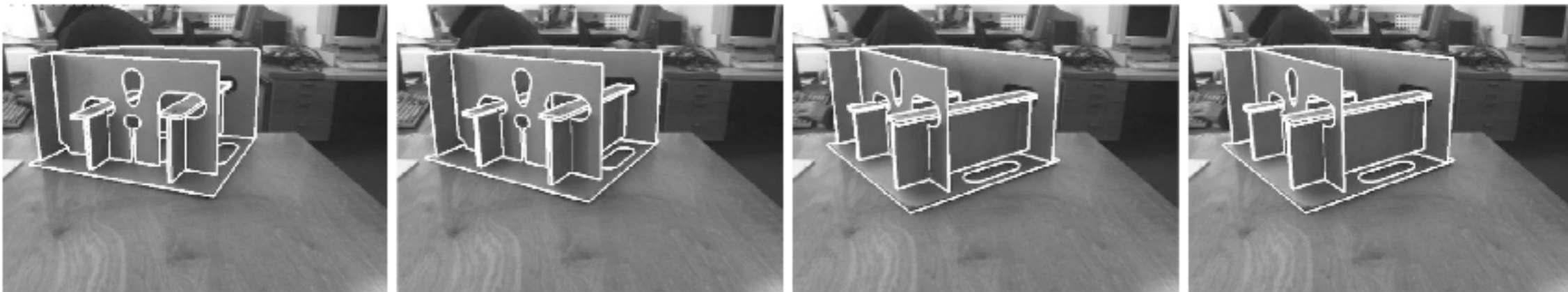
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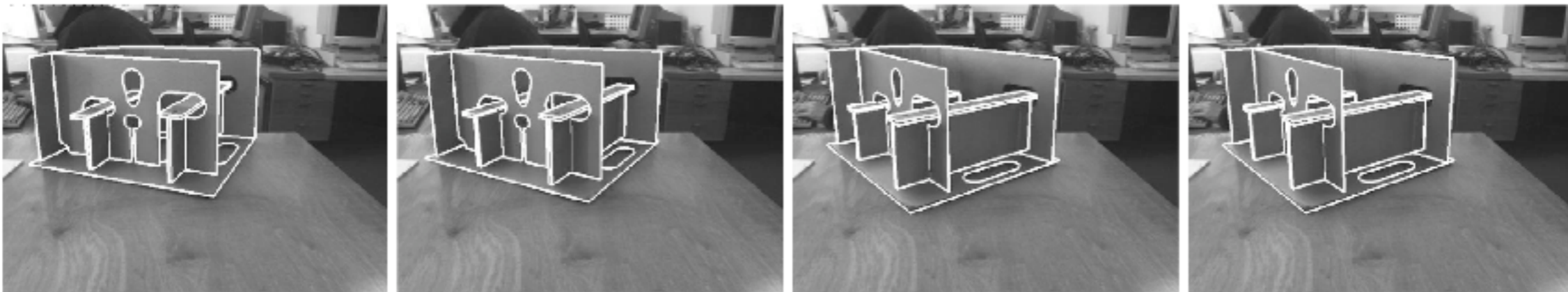
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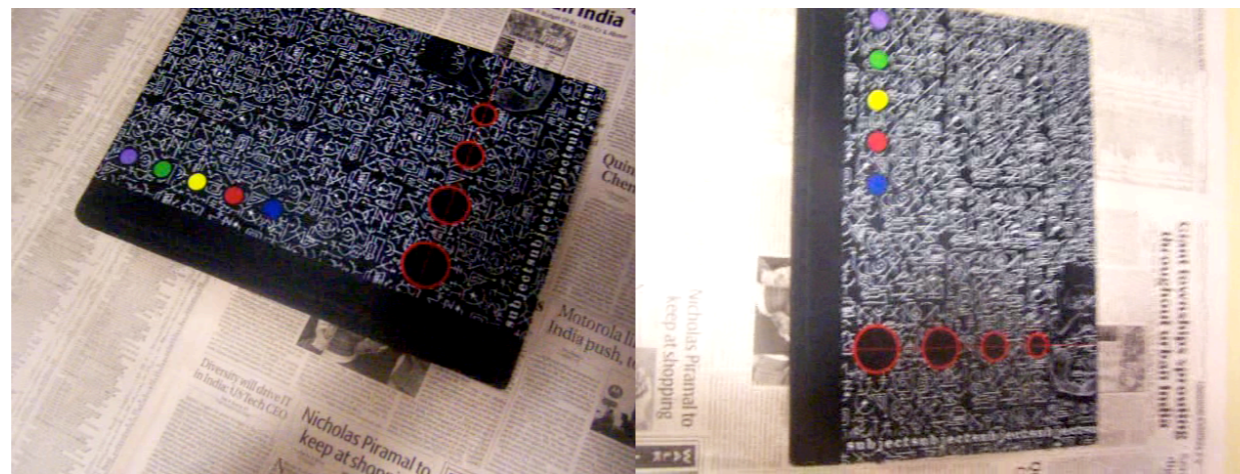
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# Tracking: Algorithm



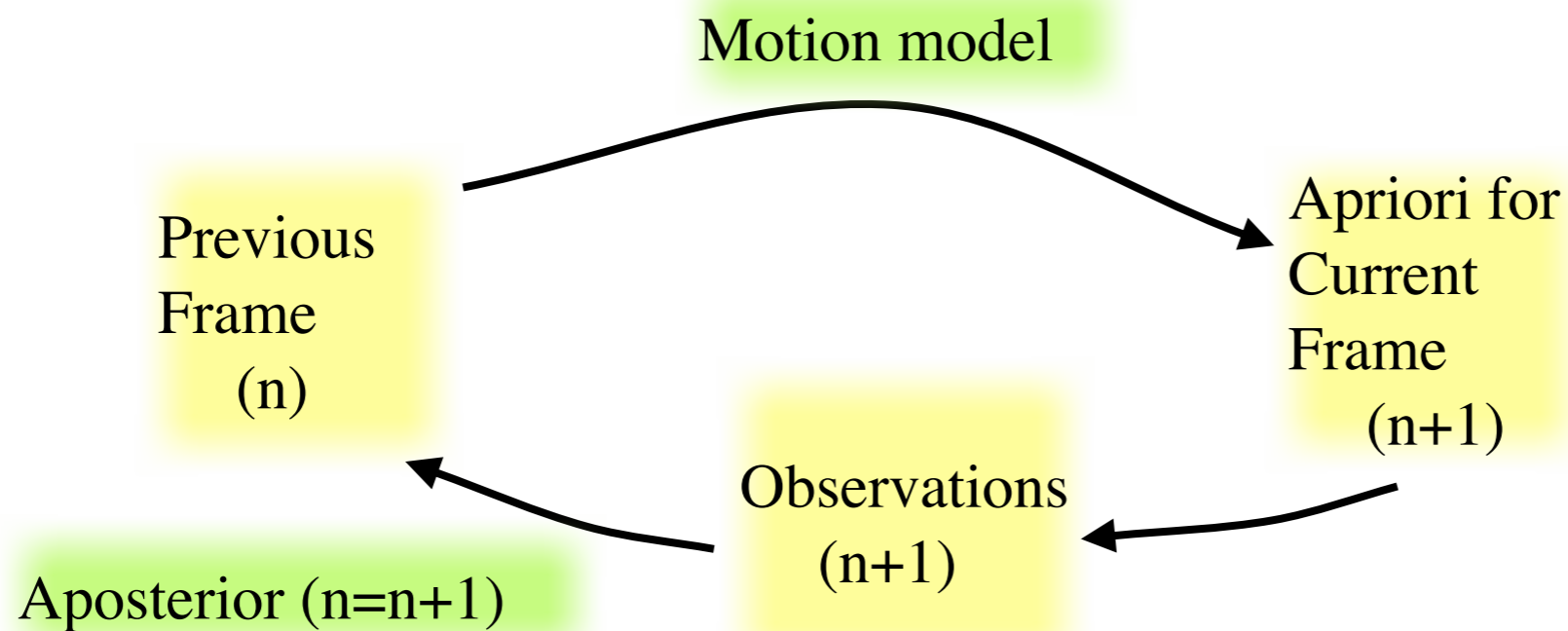
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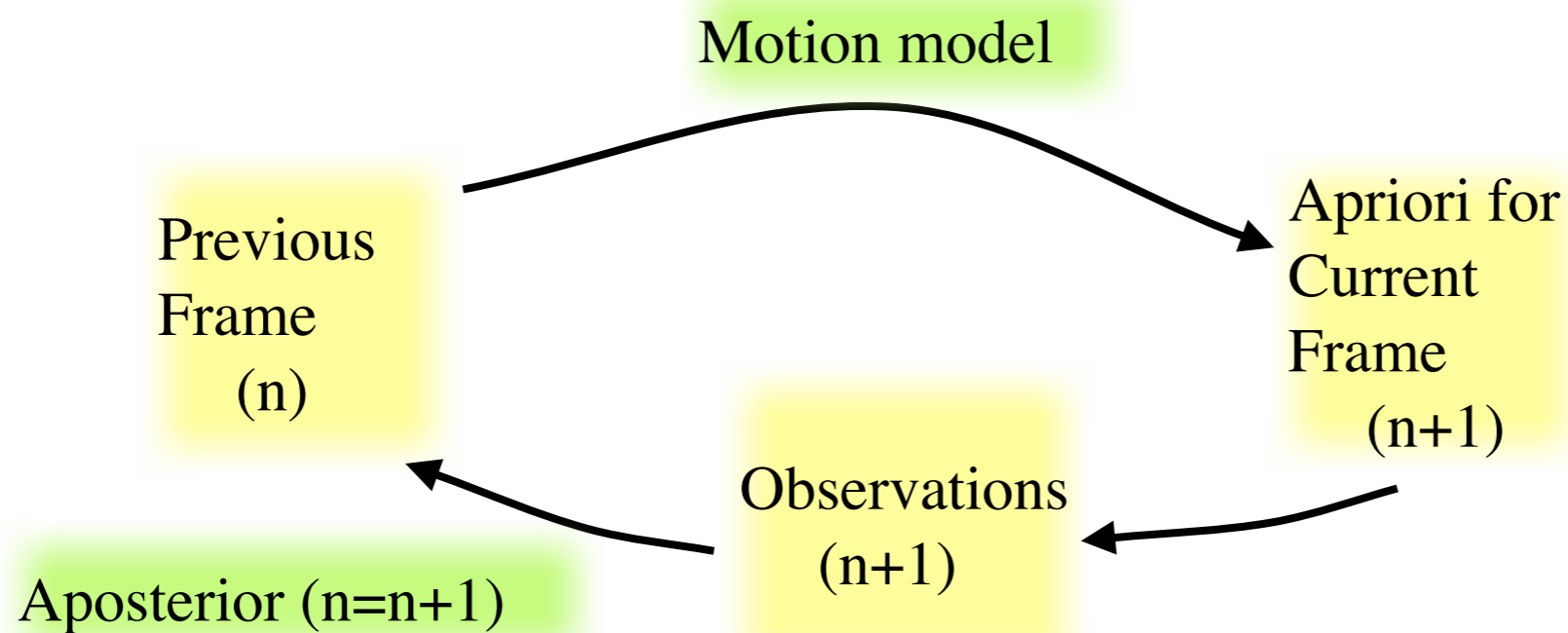




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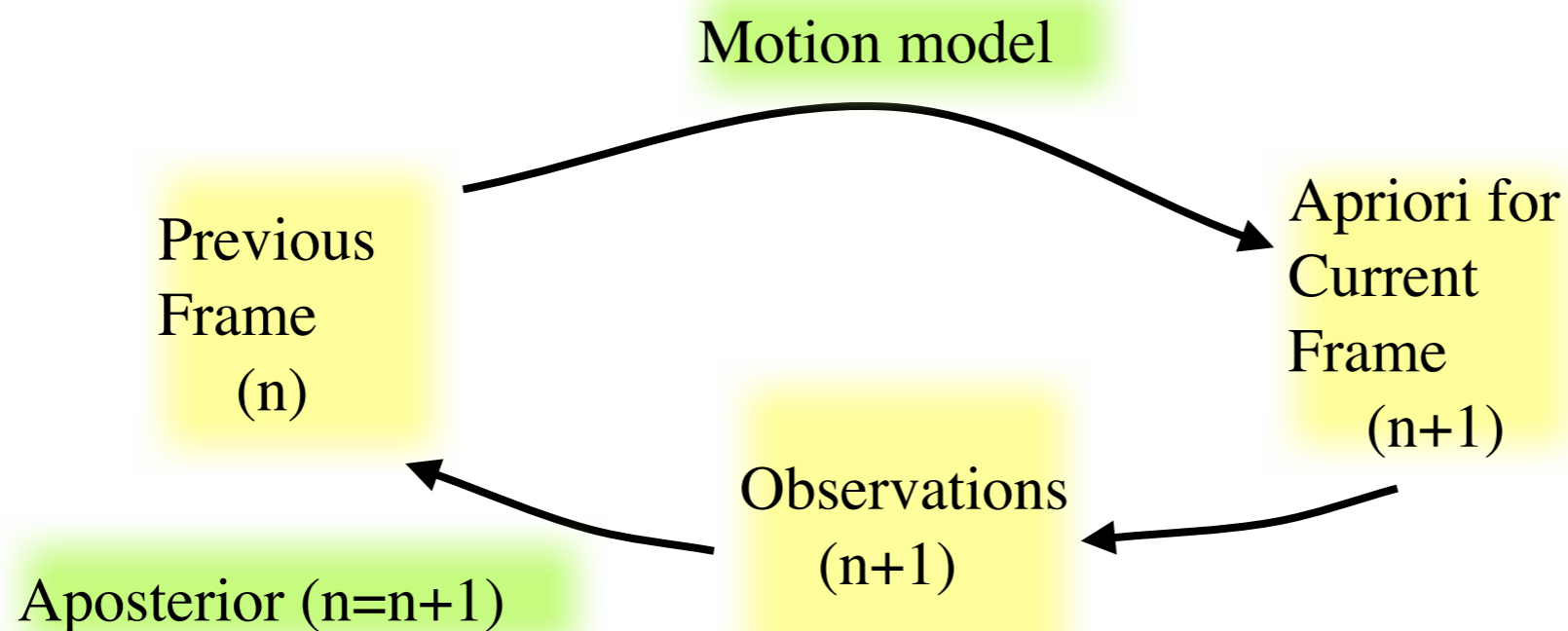




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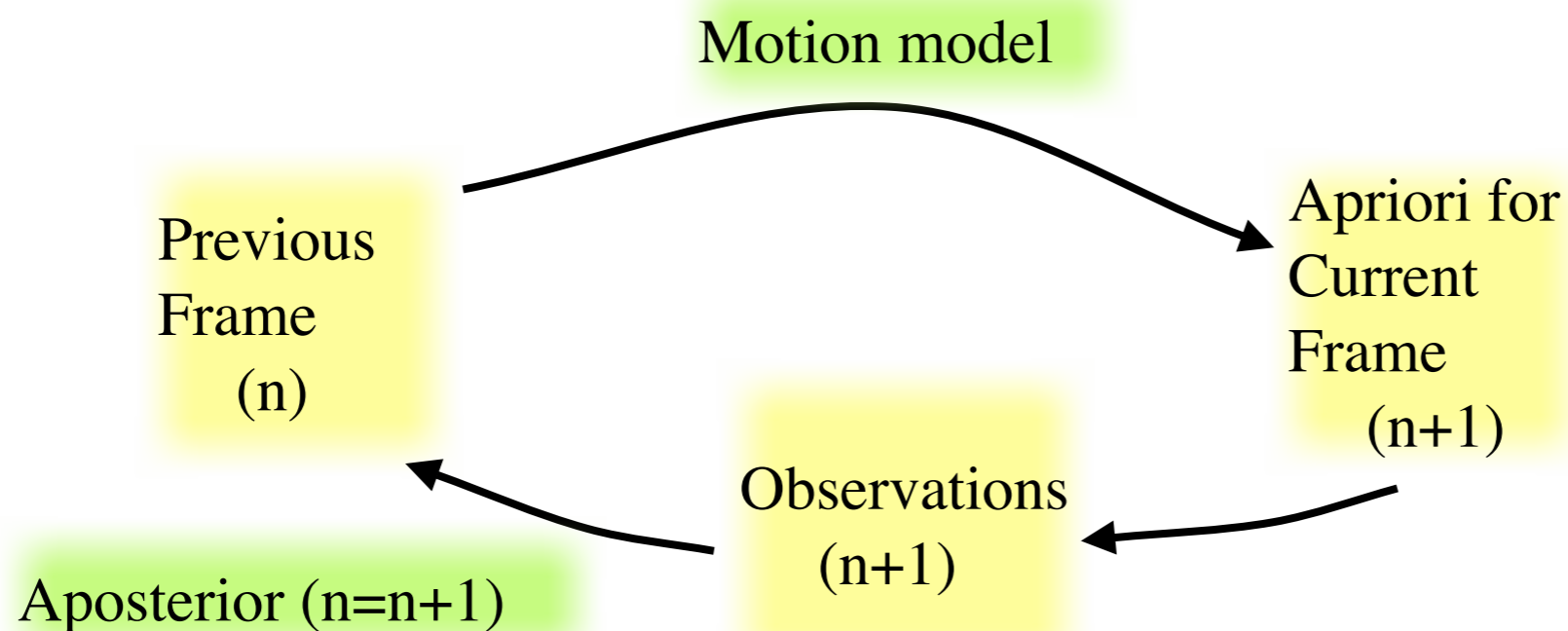




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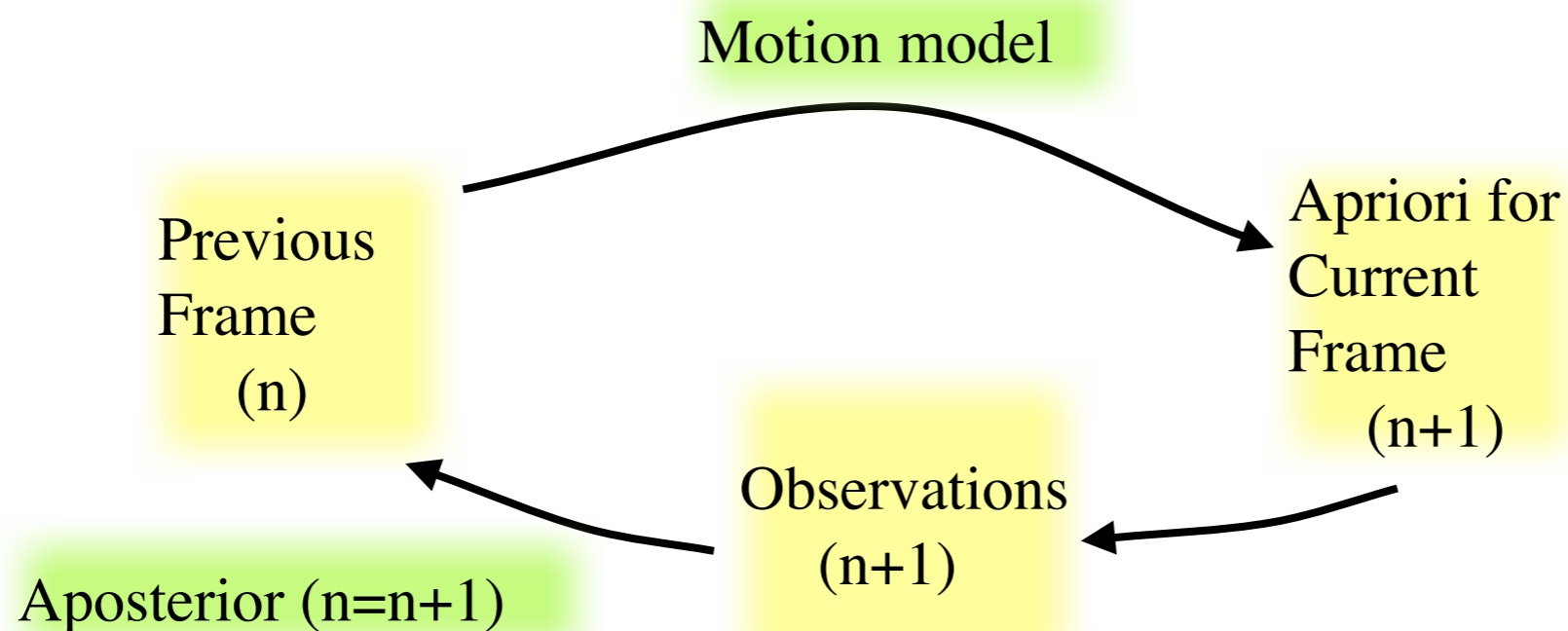




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- Unscented Kalman Filter.





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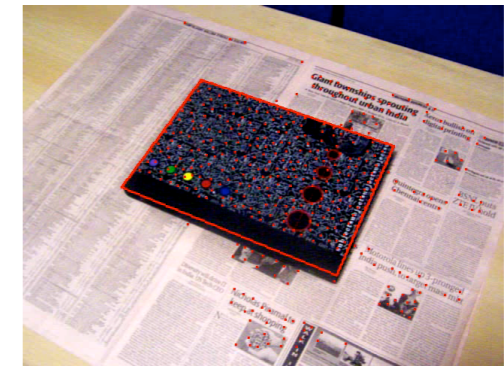
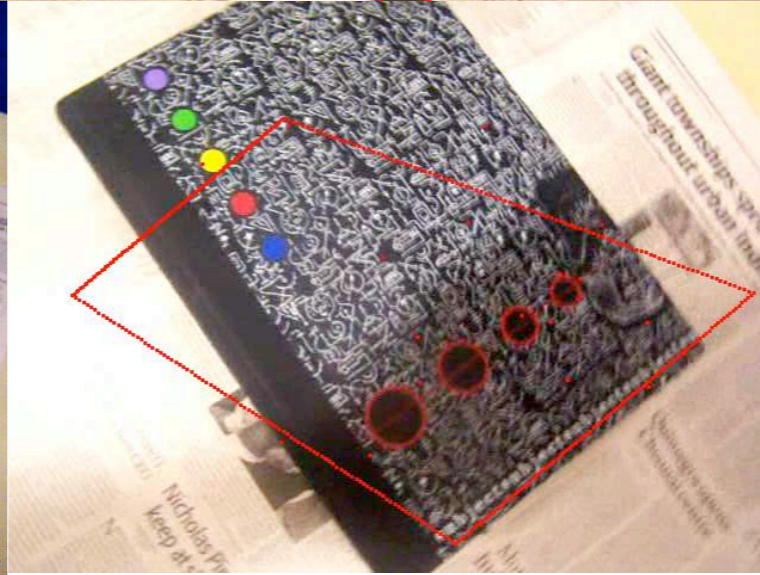
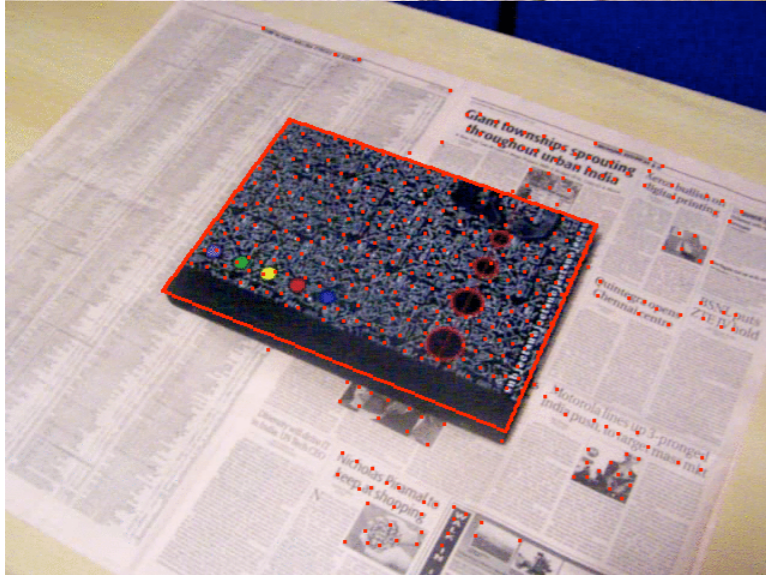
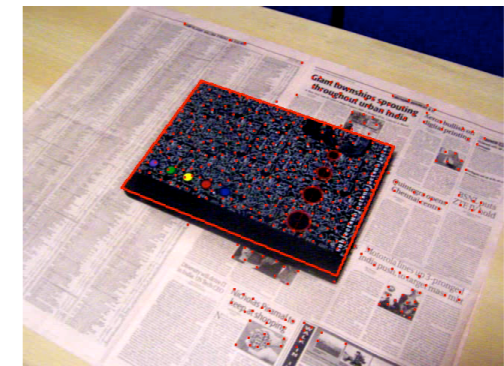
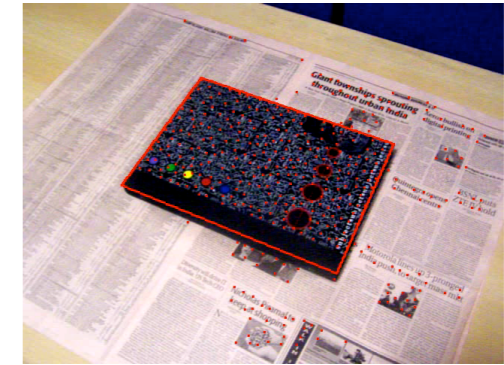
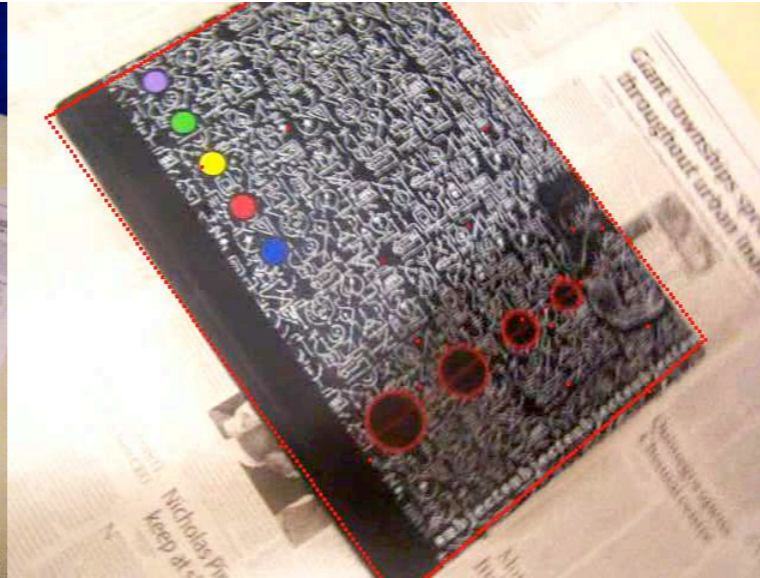
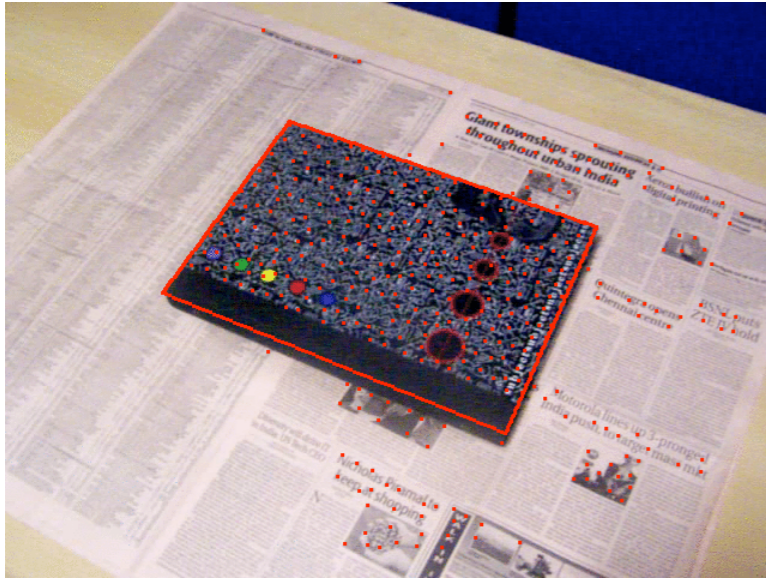
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Important Differences and Choices!



# Tracking: Results



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# Tracking: Summary

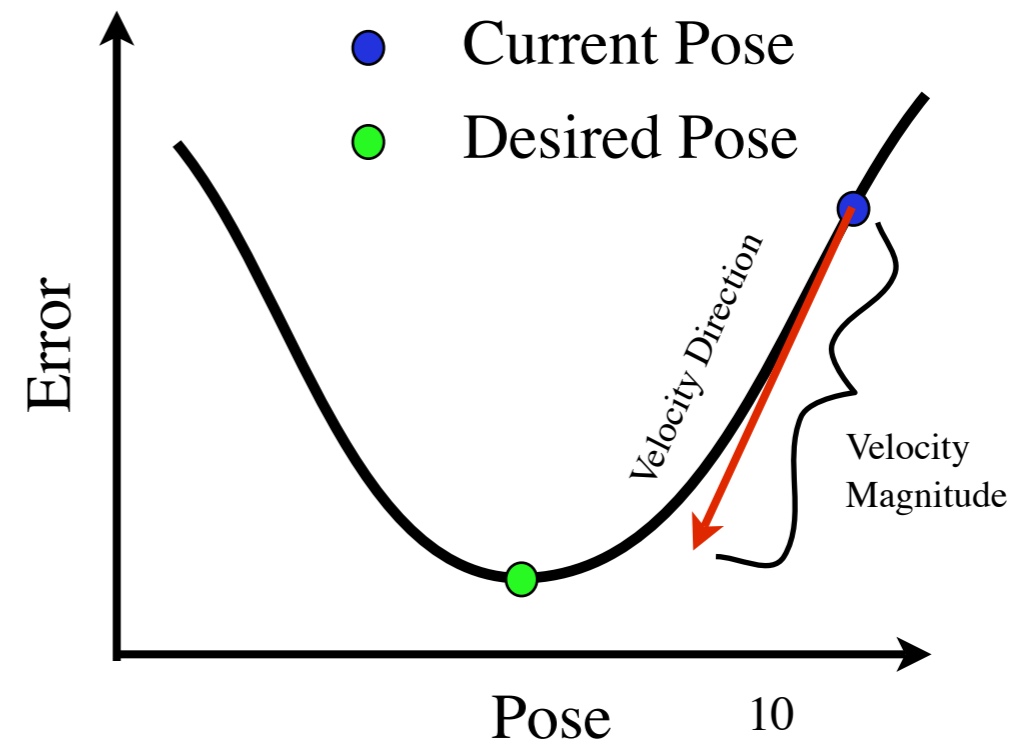
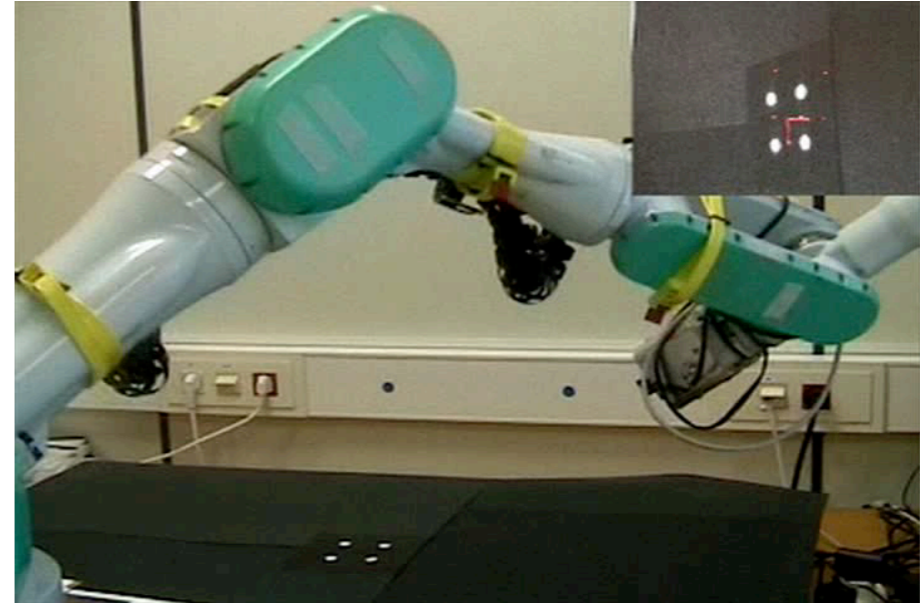
- Tracking as pre-requisite.
- 2D + 3D tracking.
- Illumination and Occlusion handling.
- Globally optimal initialization.
- Two complementary algorithms.



# Visual Servoing: Past Work

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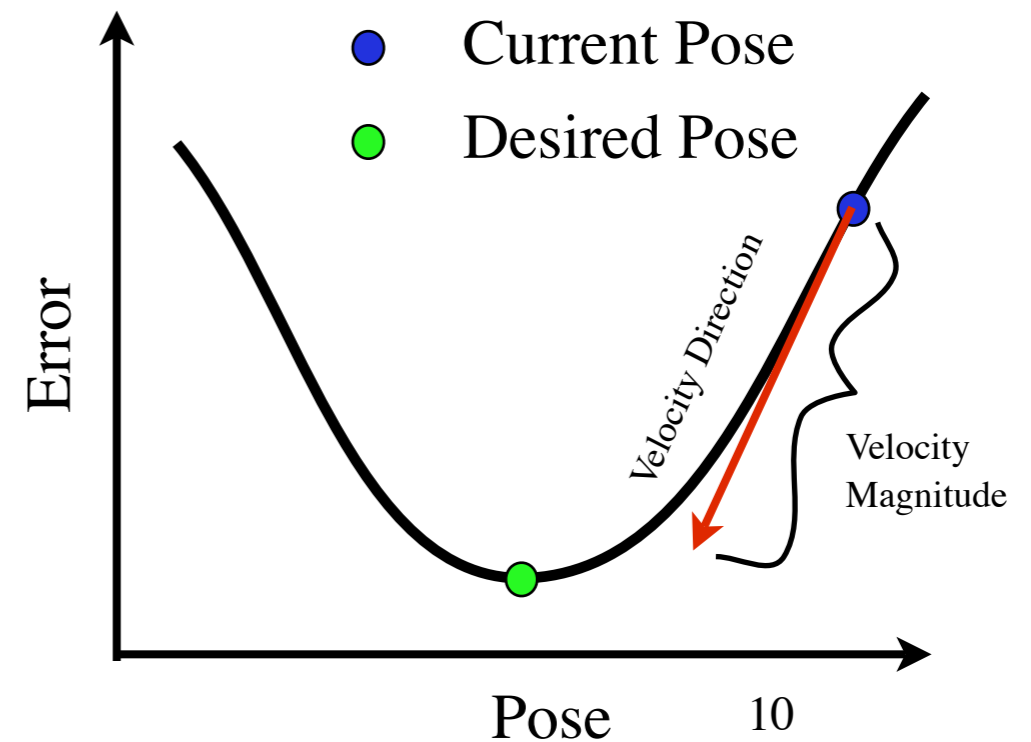
- Servoing as minimization. w.r.t. planes.





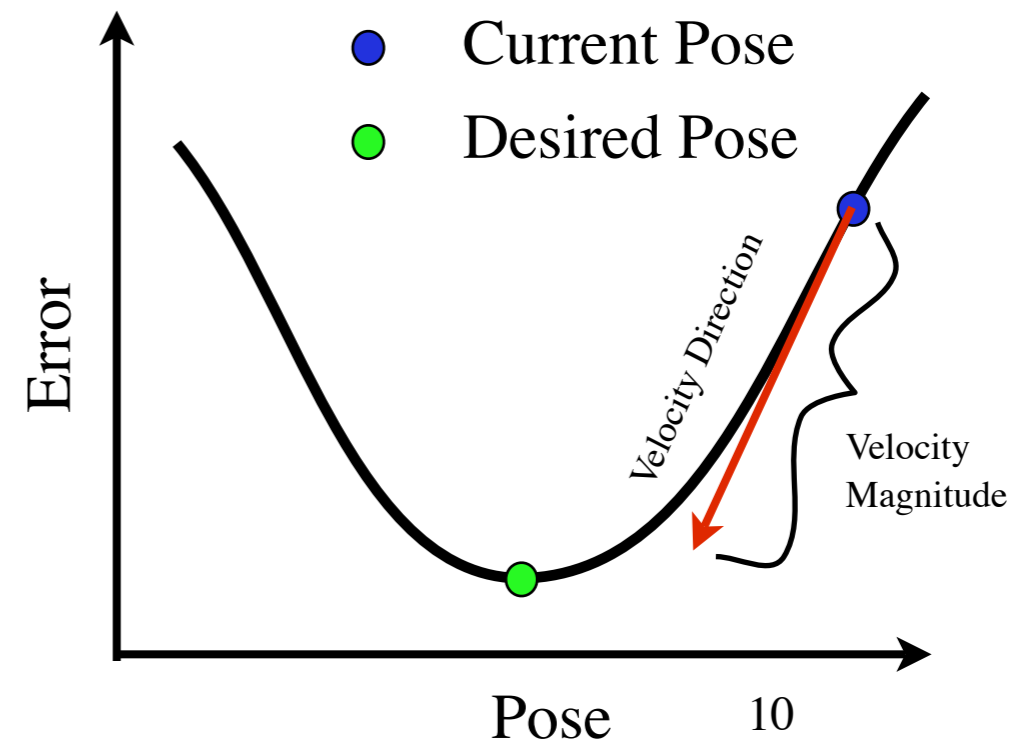
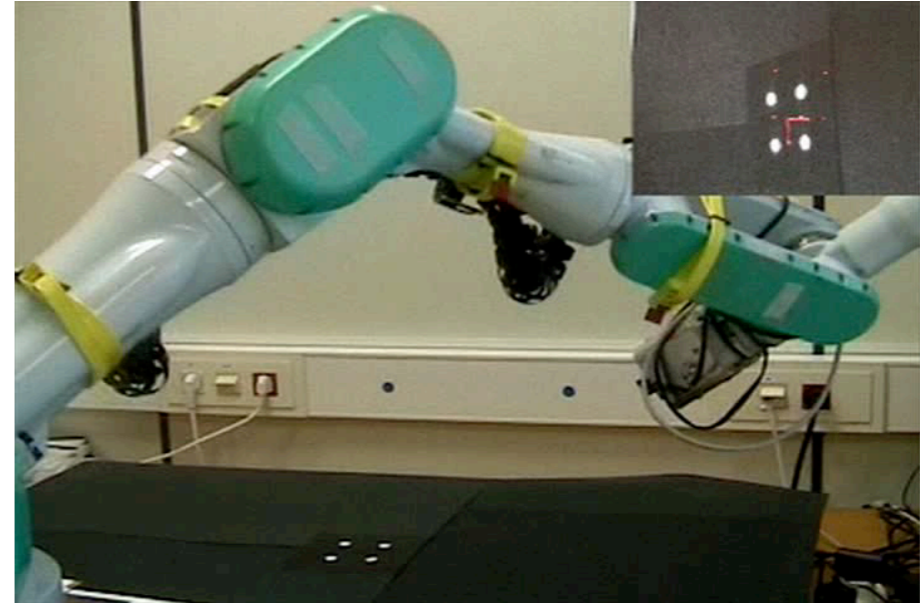
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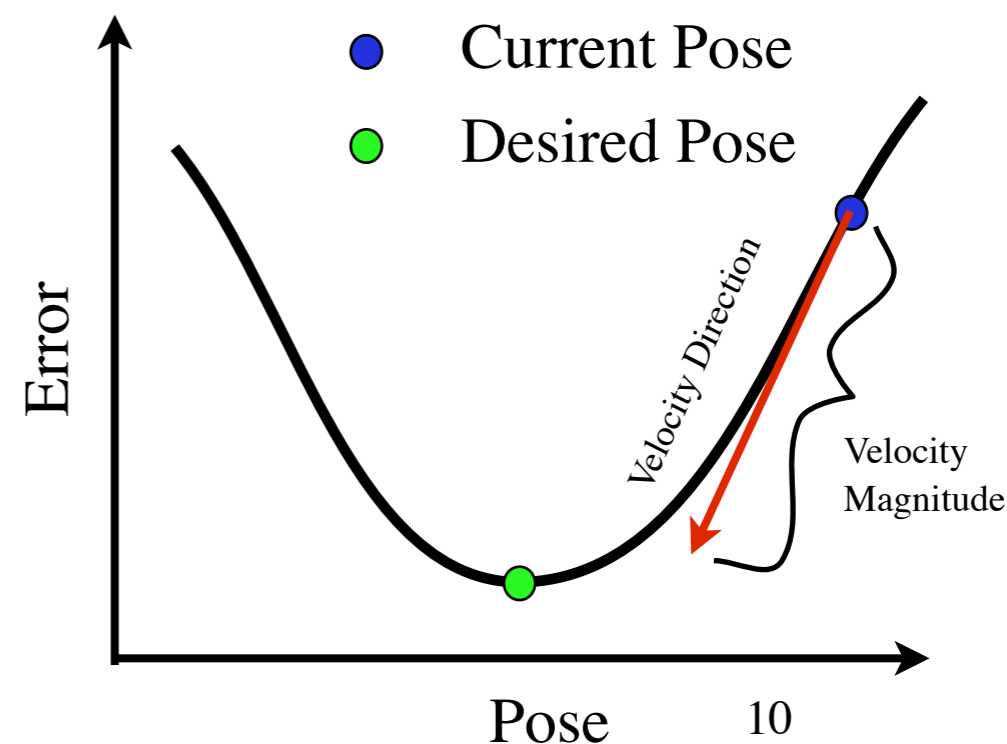
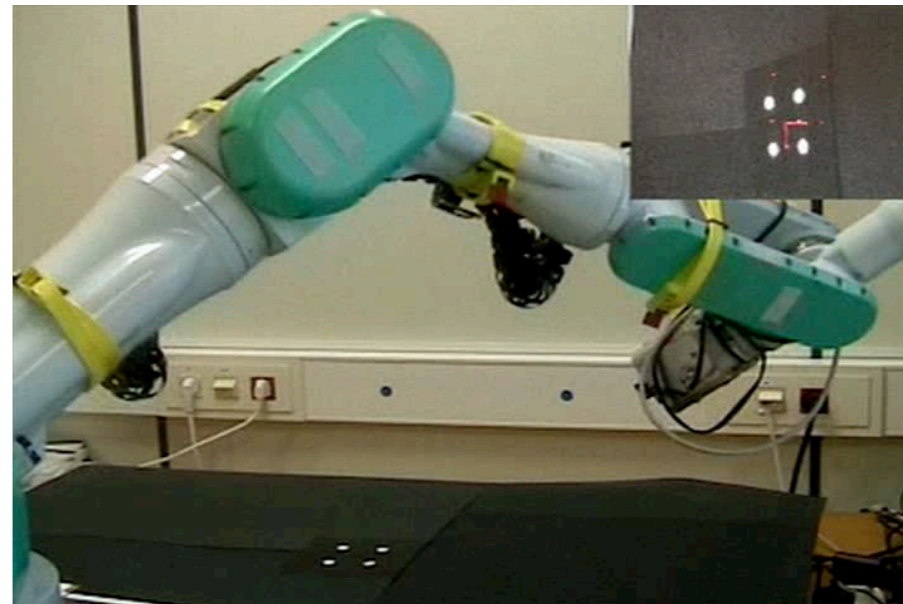
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- IBVS, PBVS, Hybrids, Moments.  
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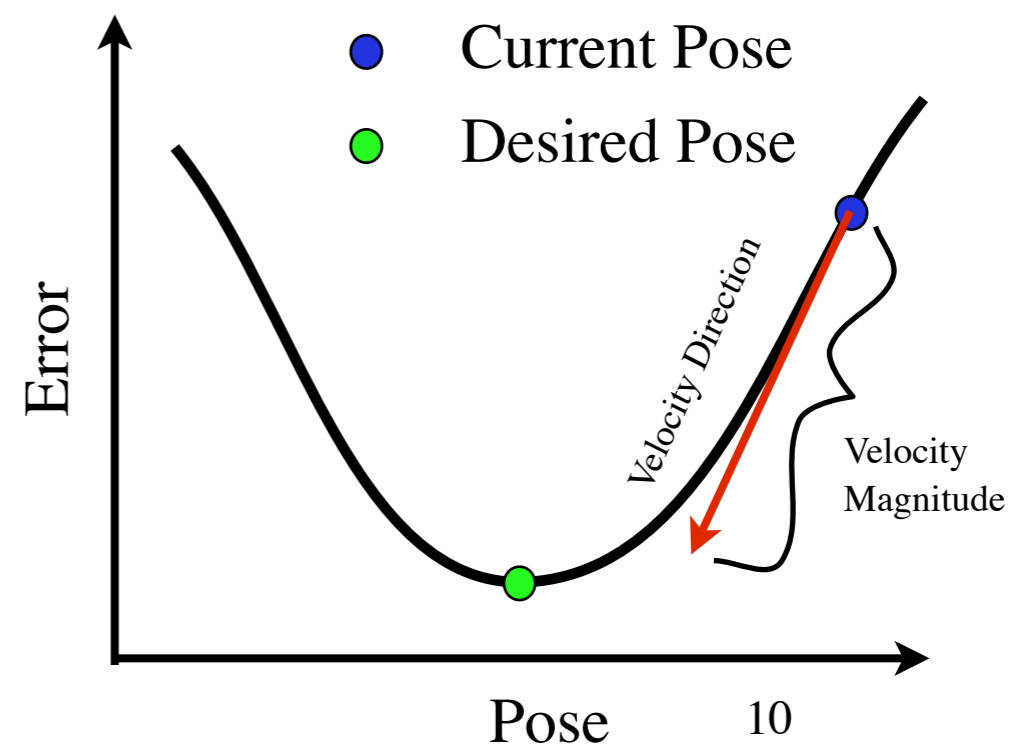
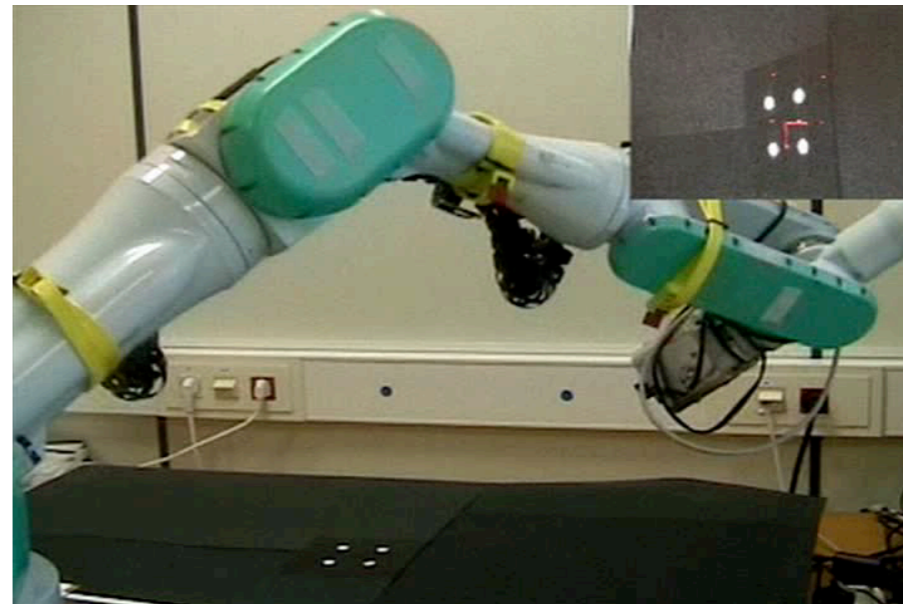
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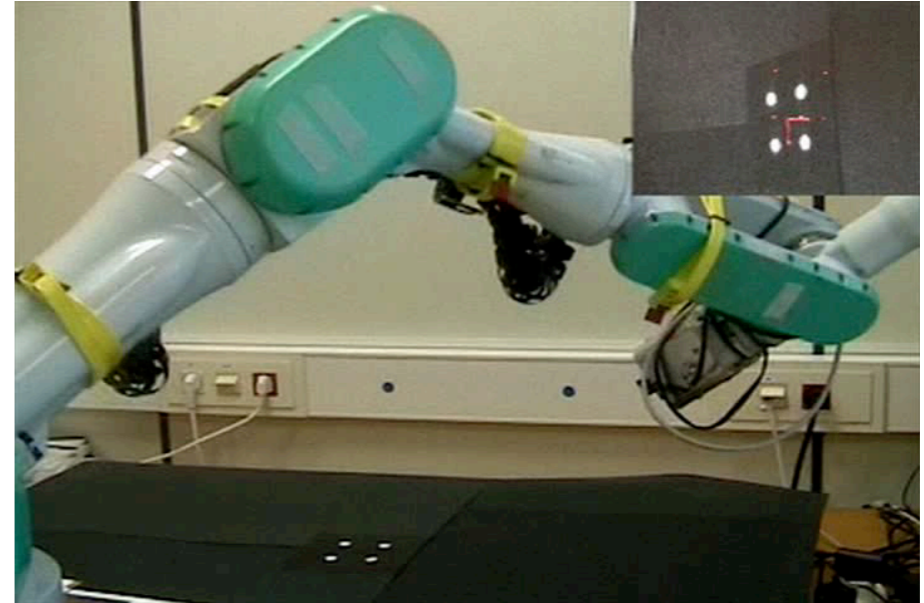
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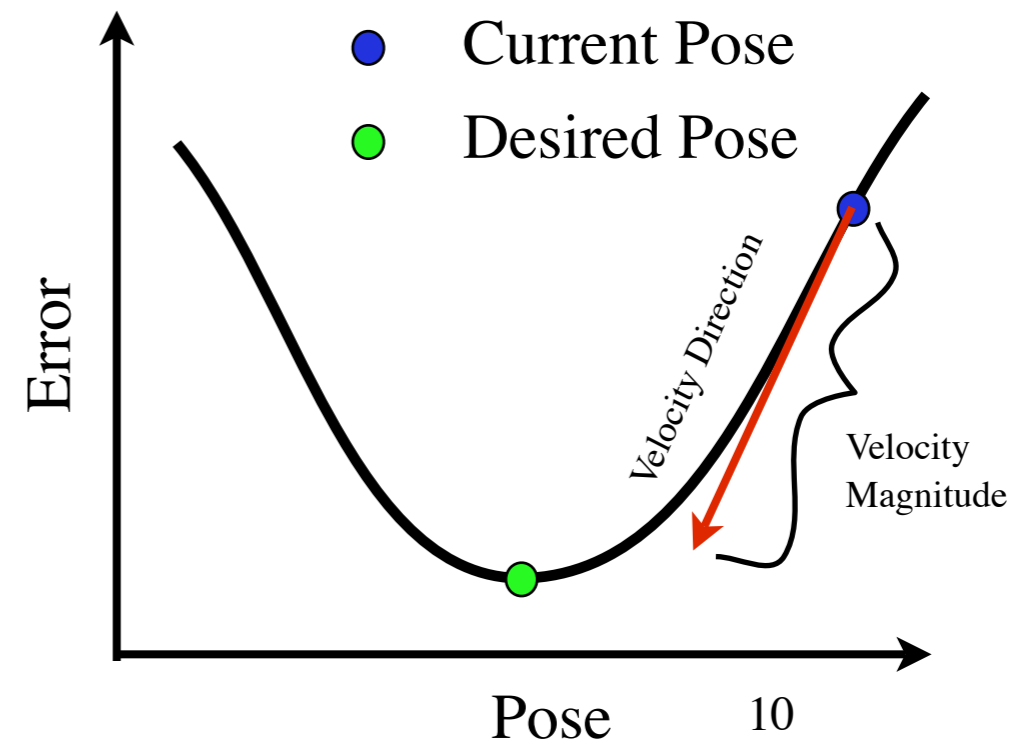


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Introduce Fourier techniques in Servoing, shows promise.



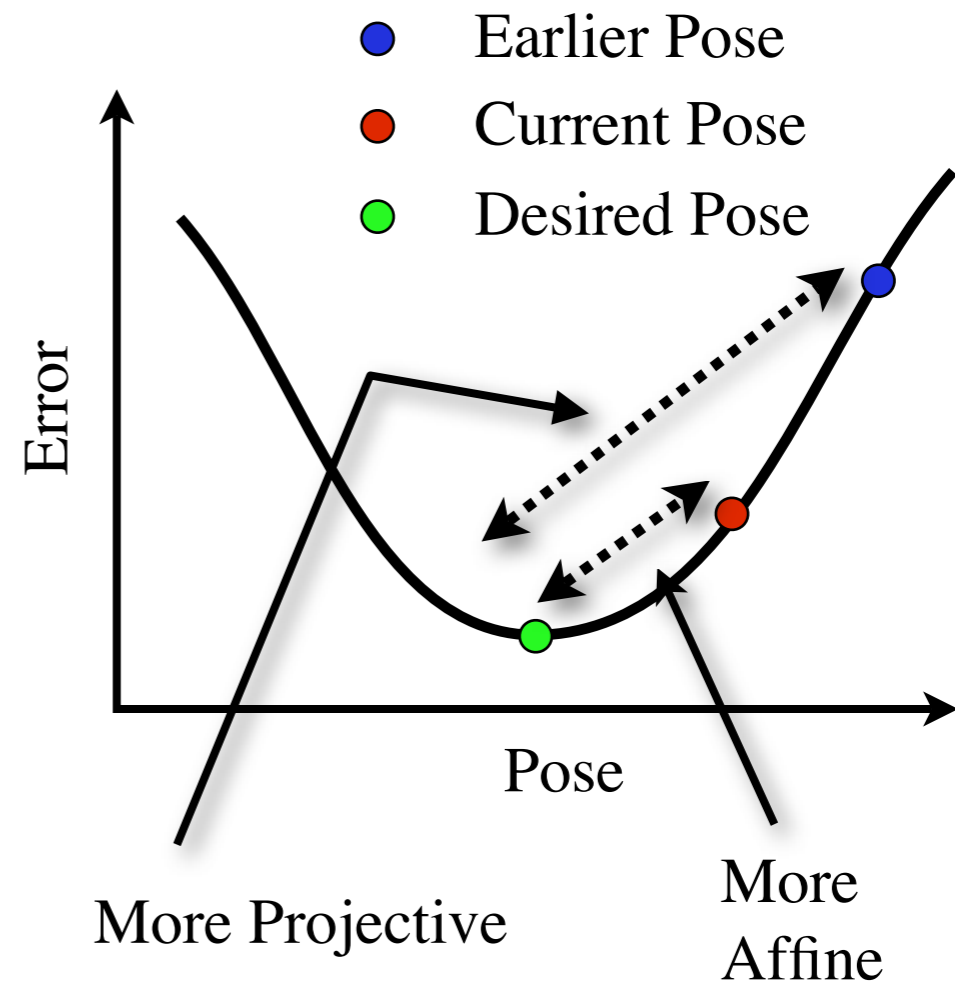


# Servoing Algorithms



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- Correspondence-less transformation estimation.

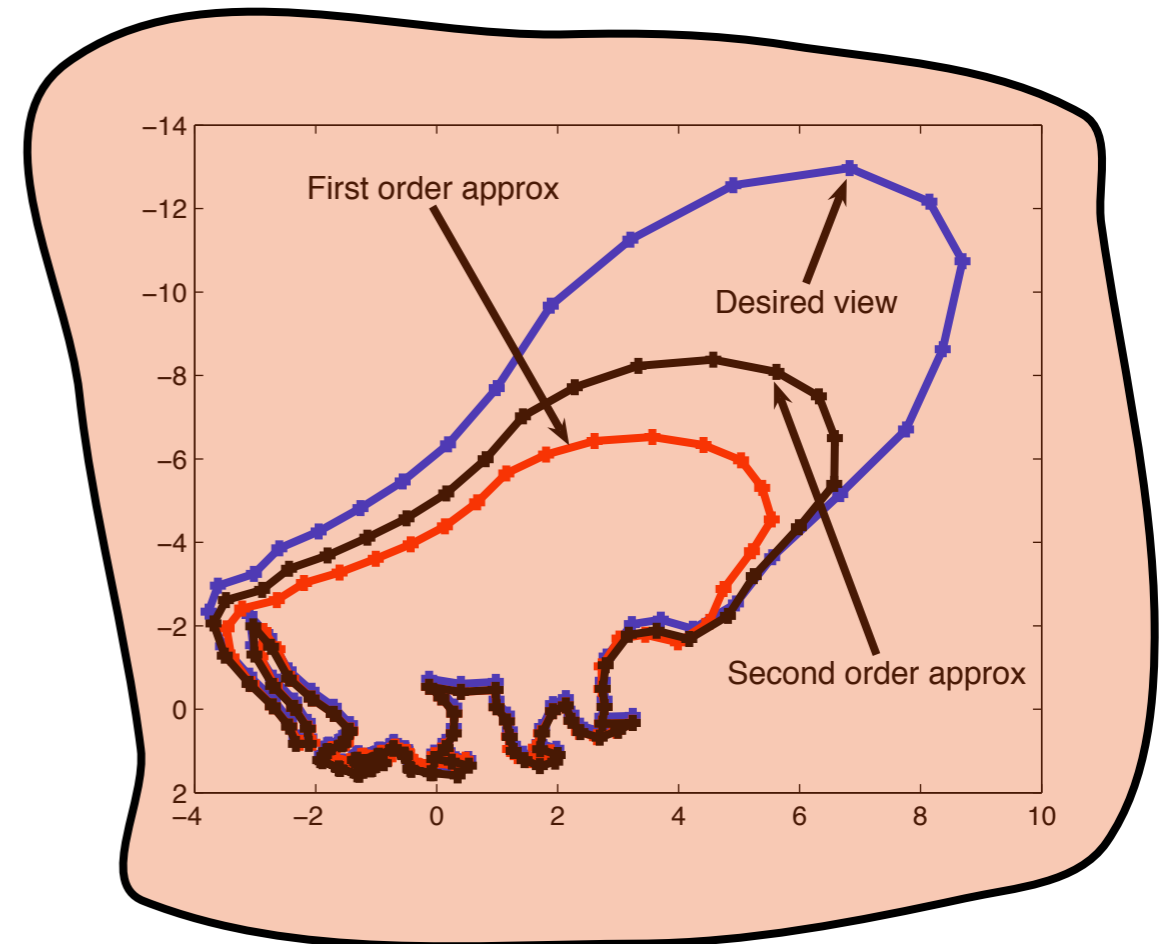




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## Fourier Transform





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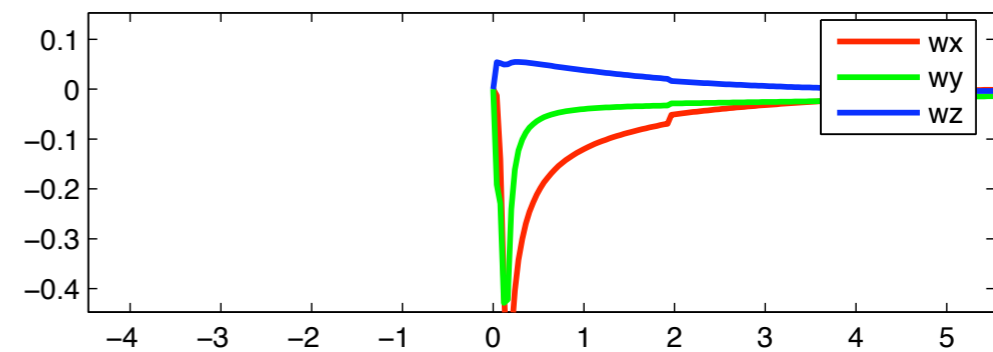
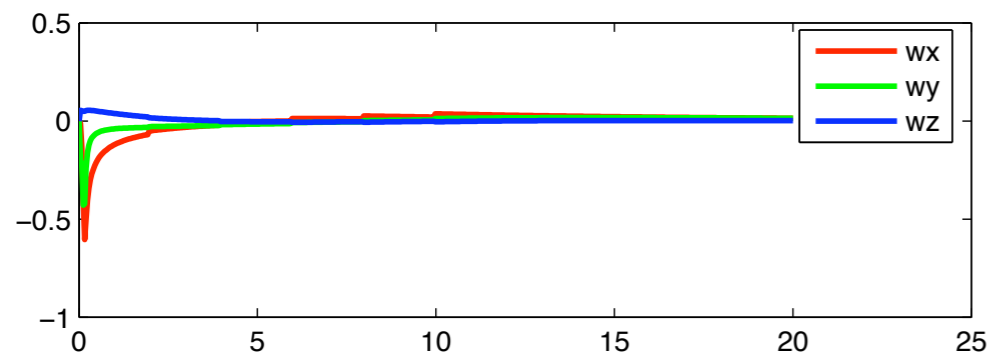
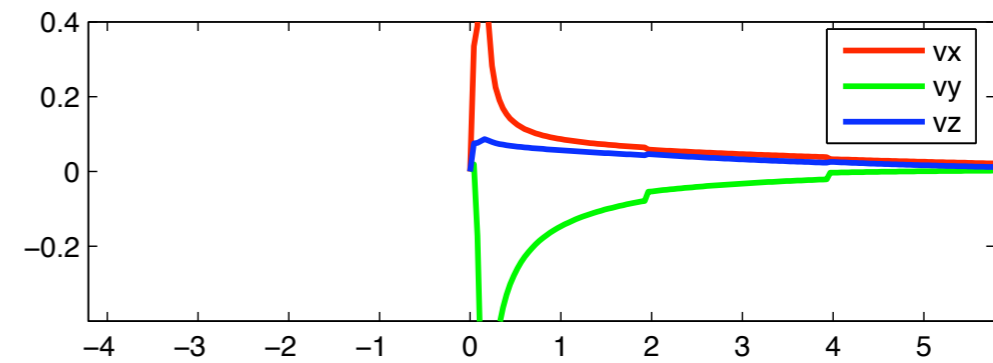
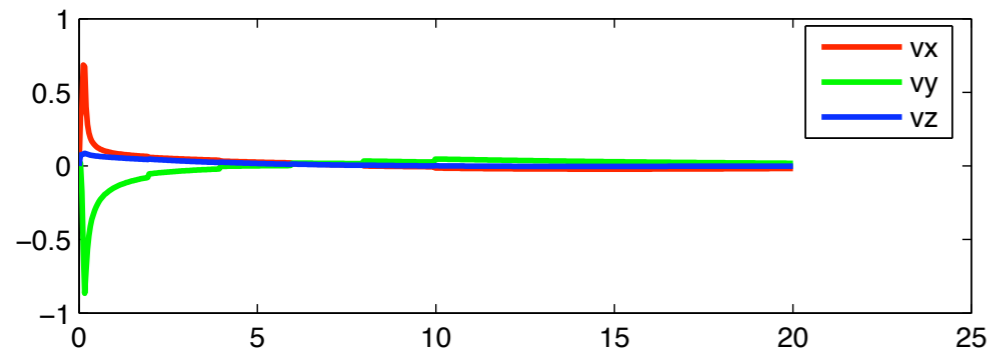
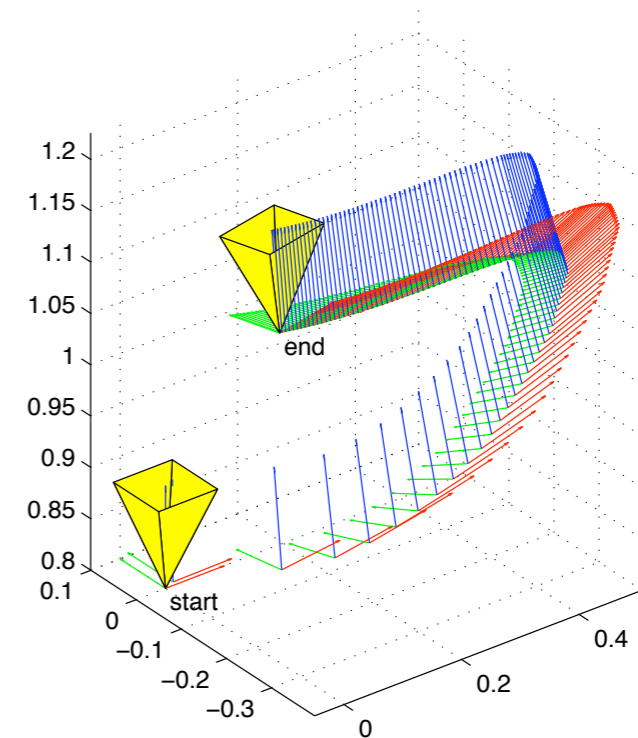
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- Path planning algorithms serve multiple purposes. Obstacle while servoing!
- Incorporate path planning output in servoing.



# Results

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- Correspondence-less servoing.





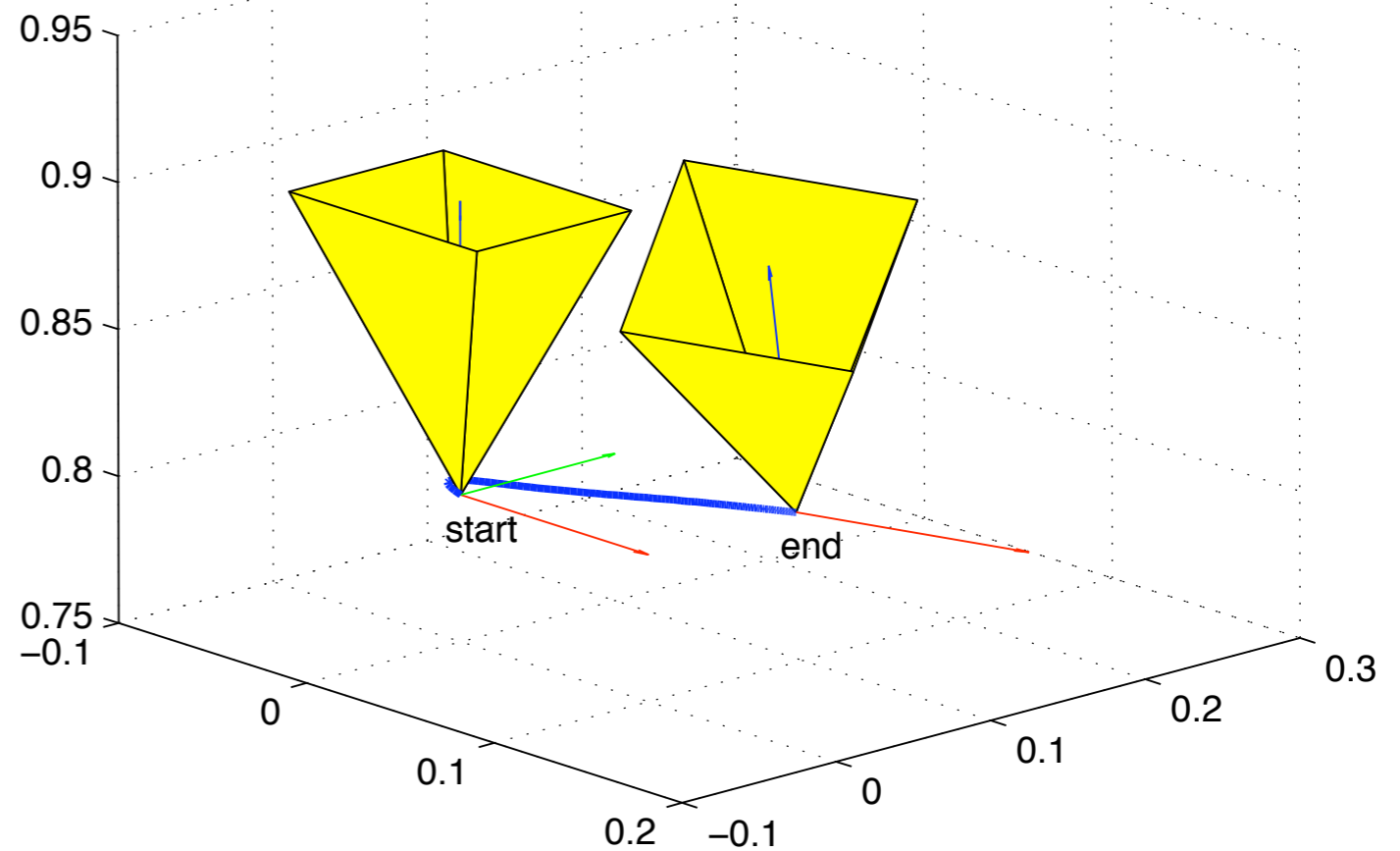
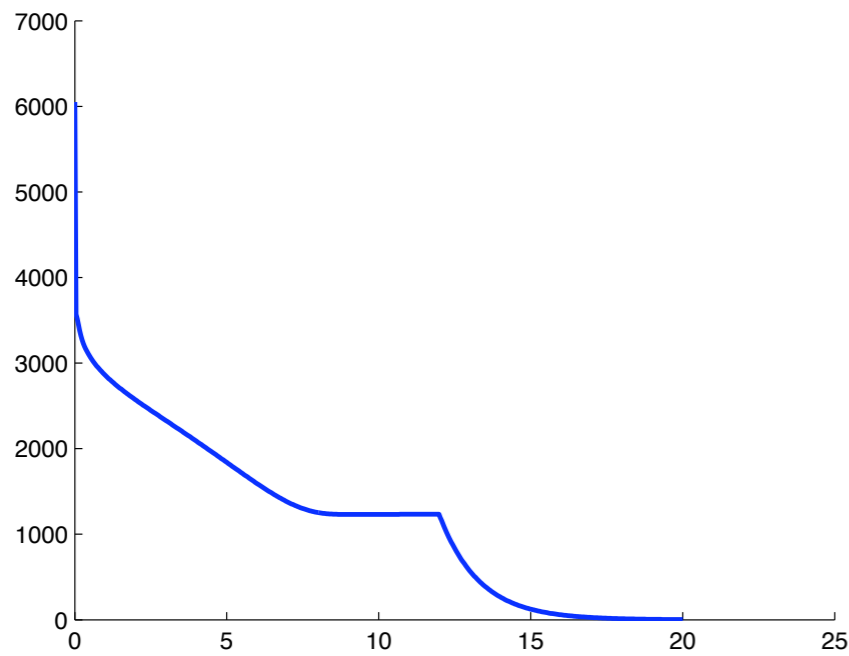
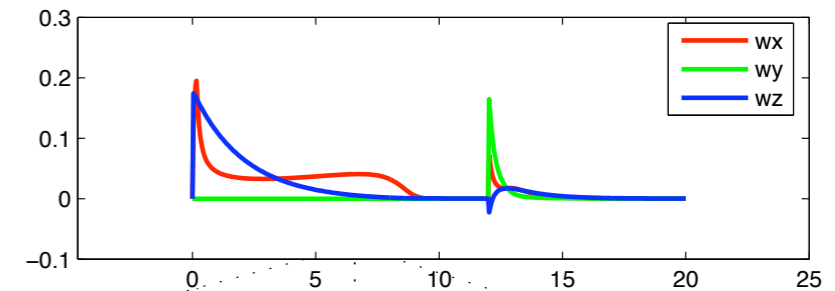
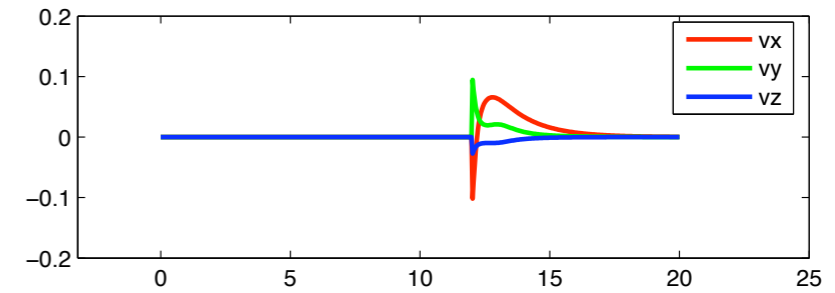
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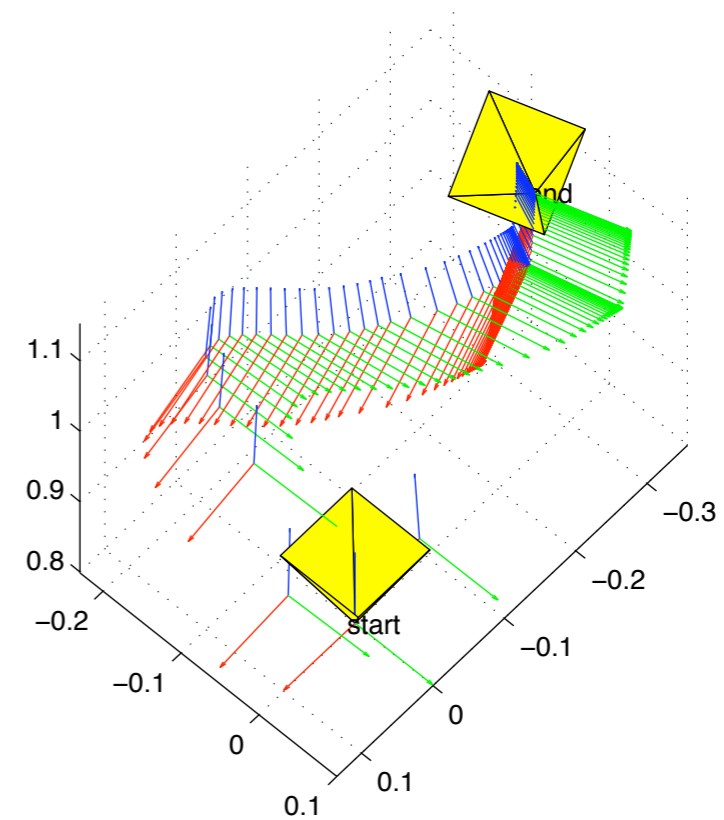
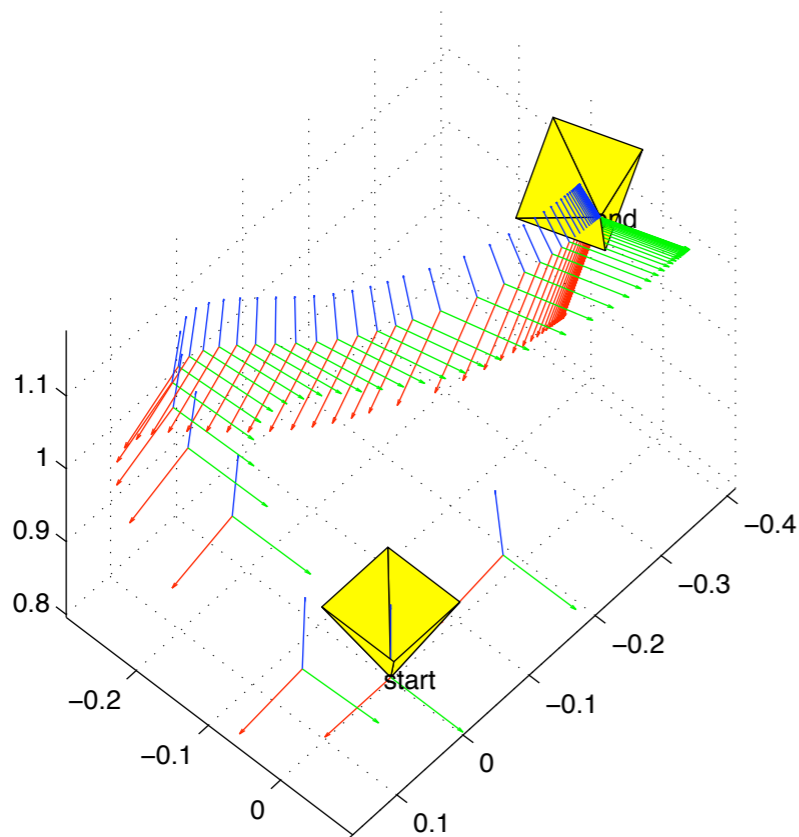


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- Straight Cartesian path.
- Path following.





# Servoing: Summary

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- Traditional IBVS errors.
- Has potential for further growth.
- Path planning algorithms.

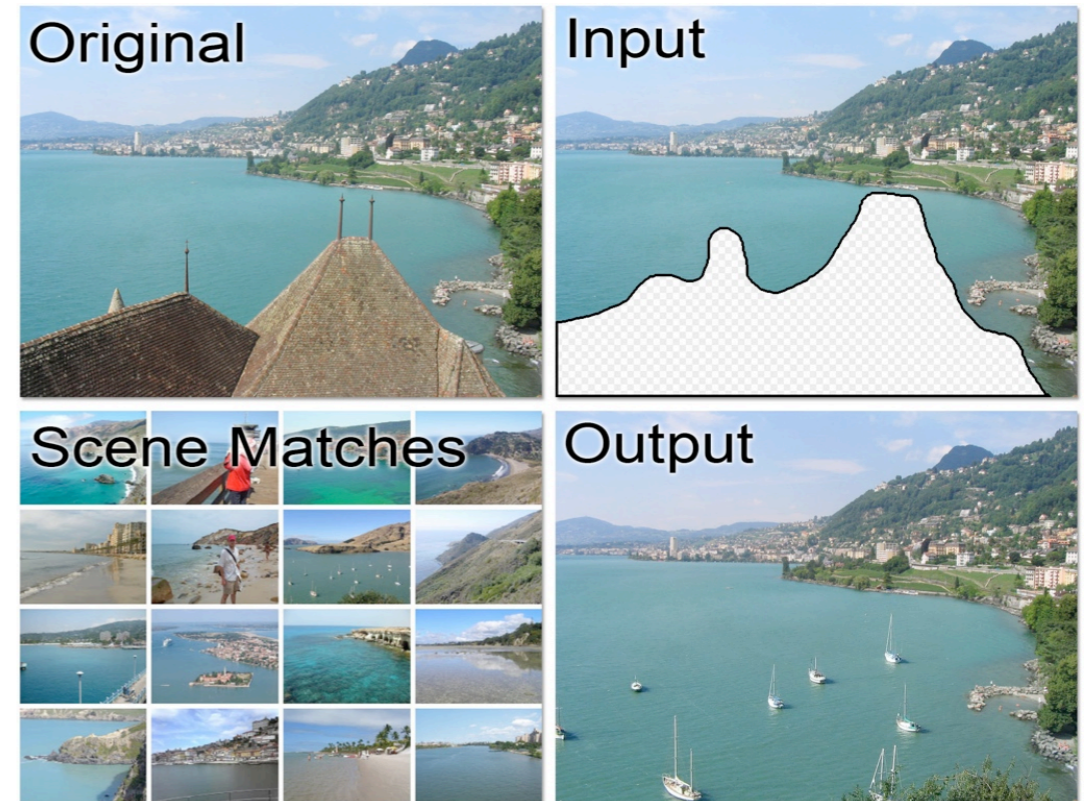


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  - When texture patches are large ?
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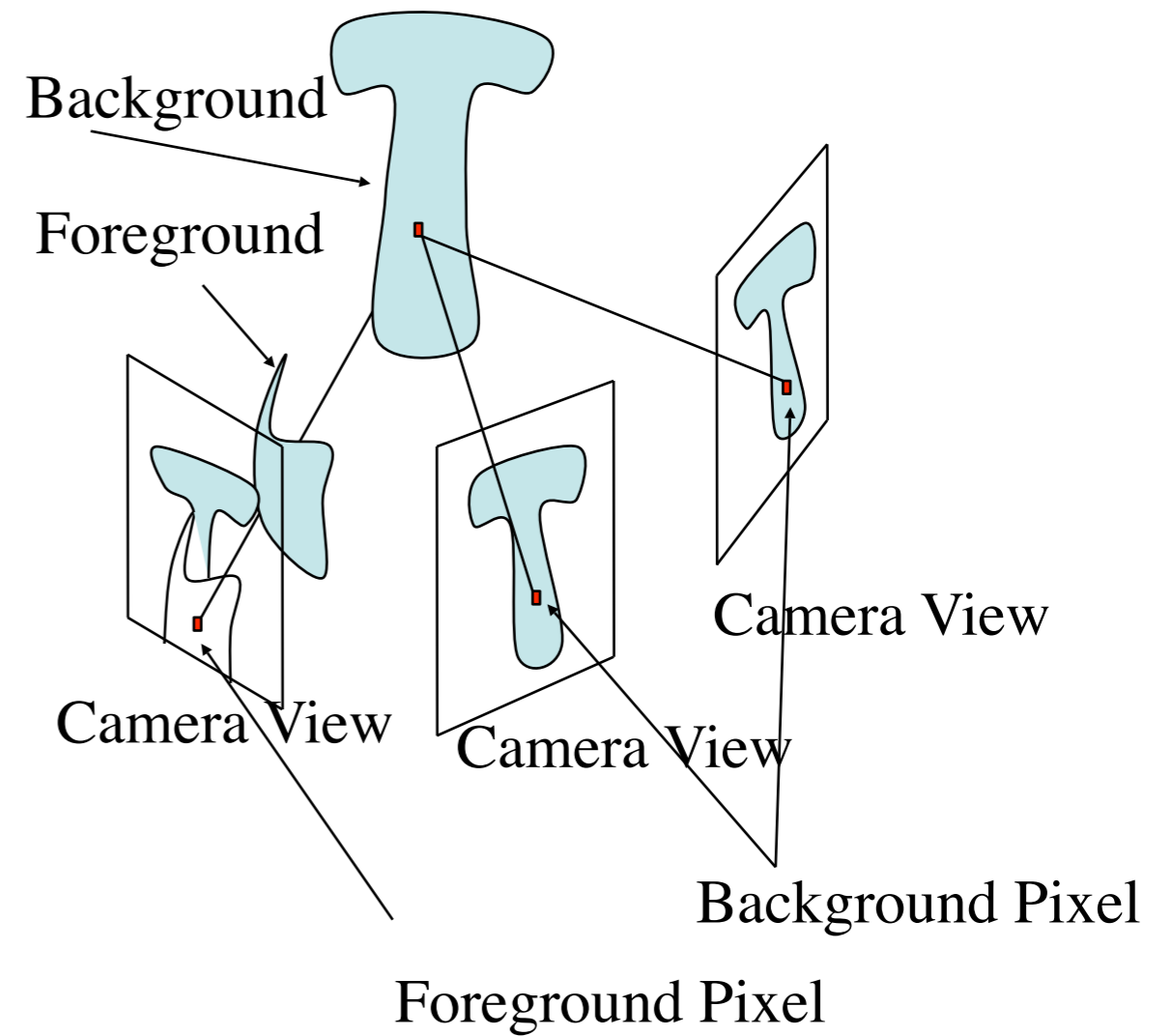


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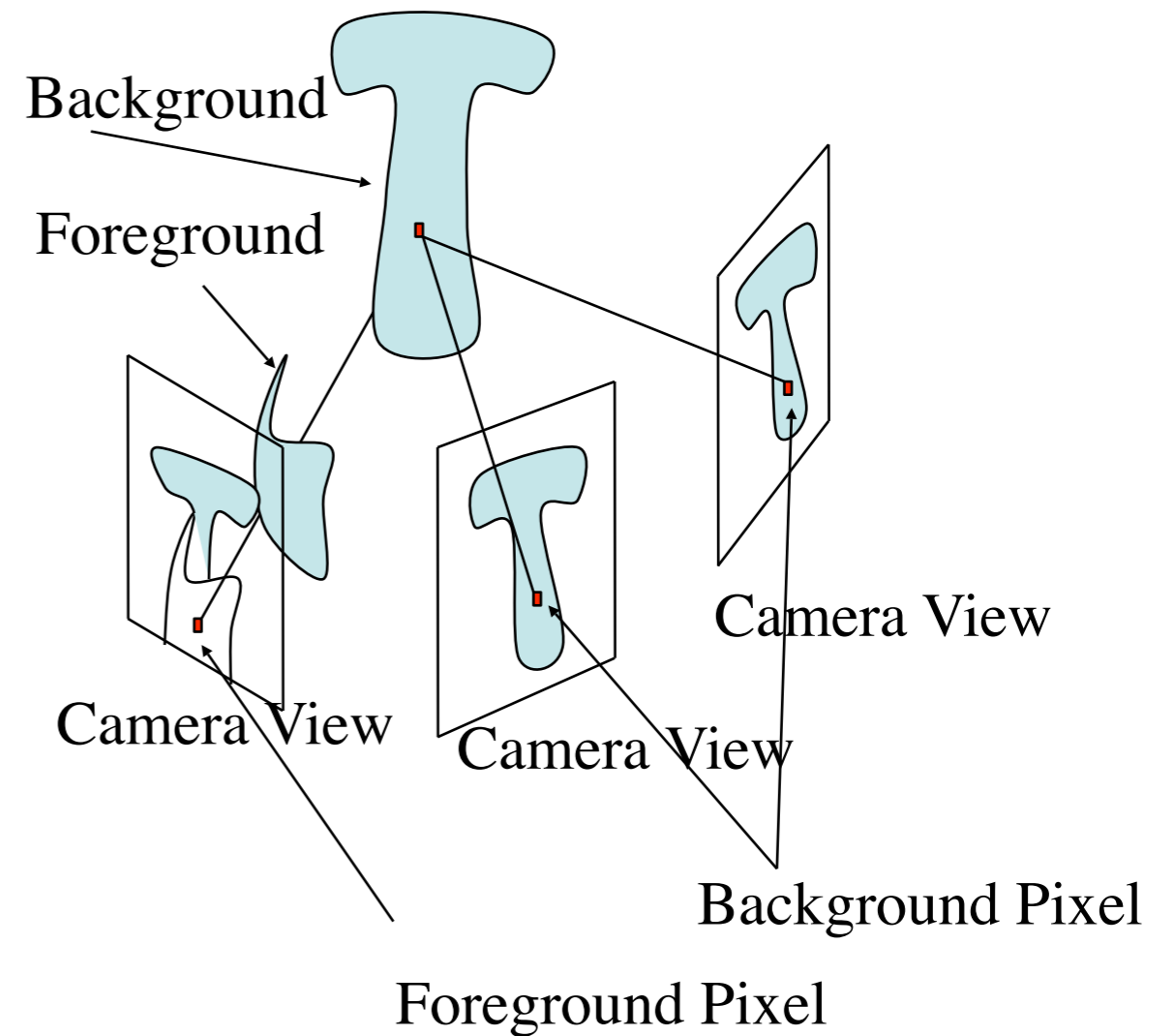
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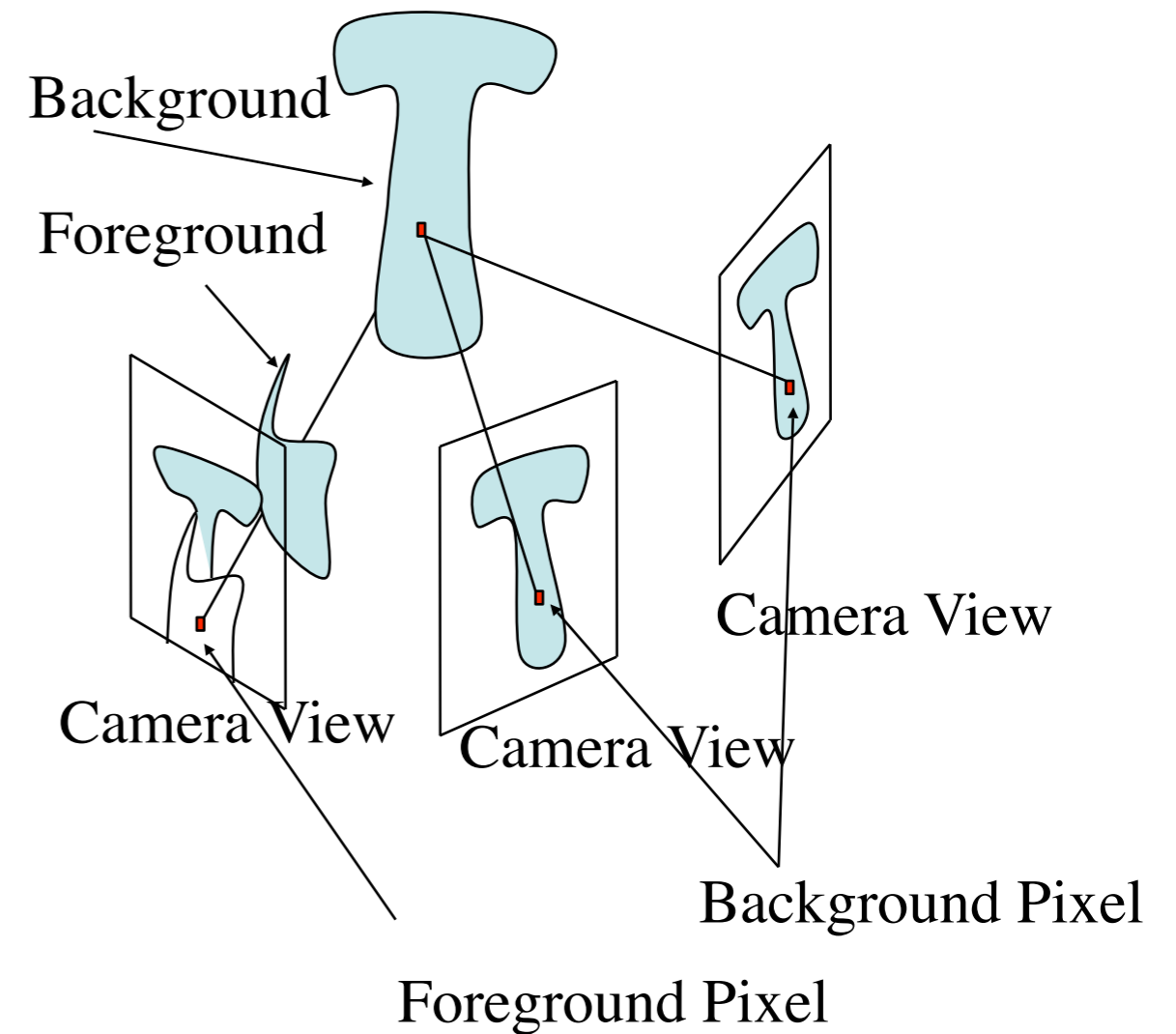
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- Transferrable characteristics - Symmetry, Texture.
- Selection from database, using semantic similarity.





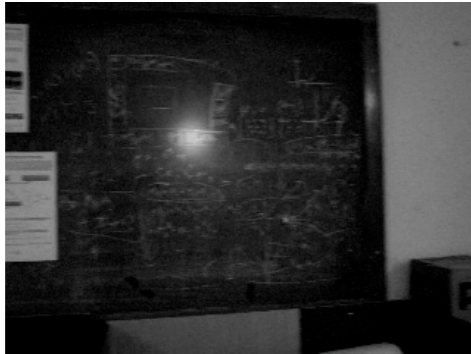
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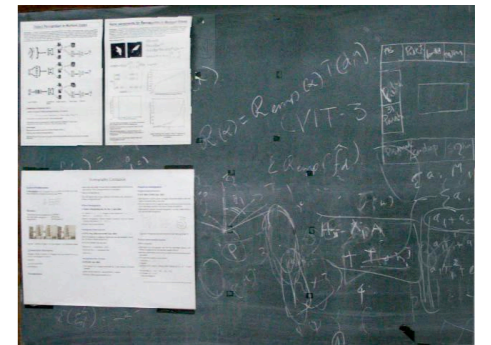
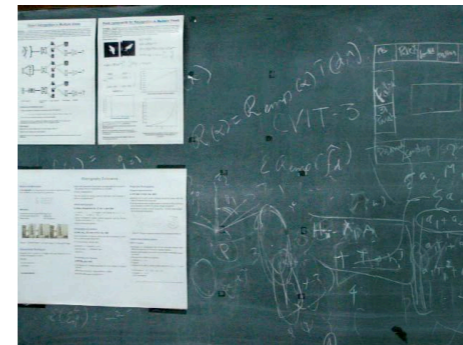
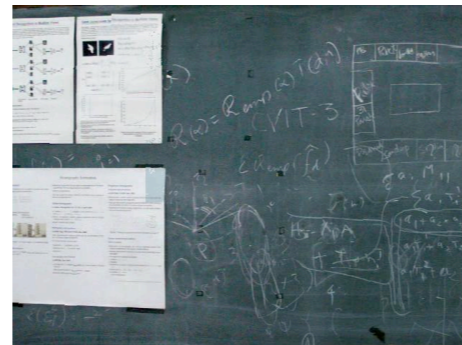
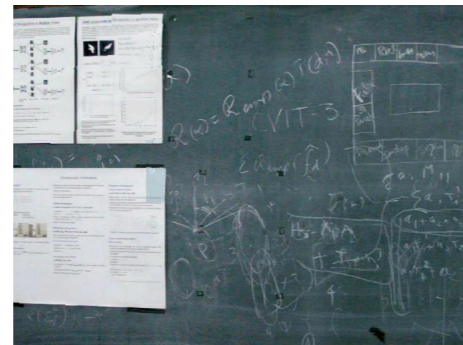
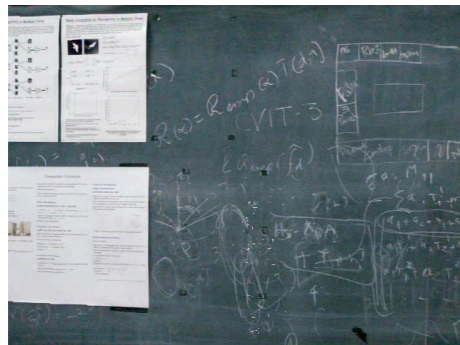
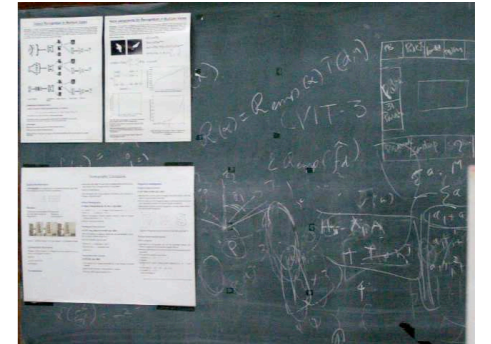
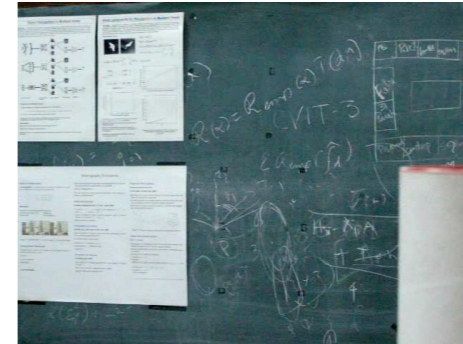
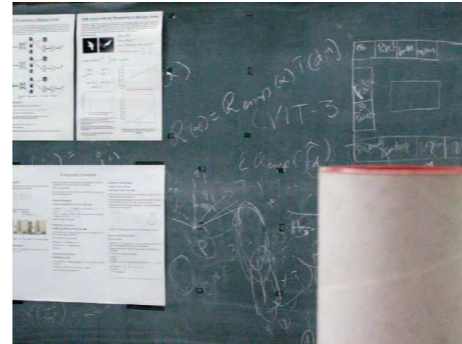
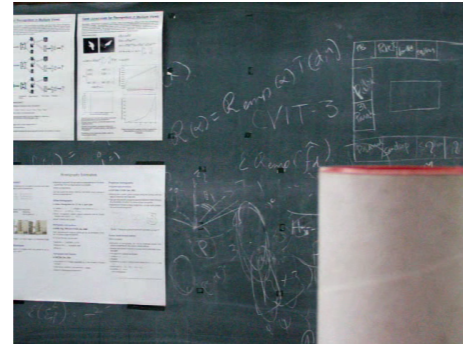
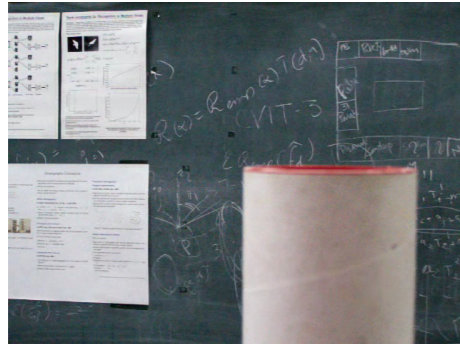


# Results





# Results





# Results

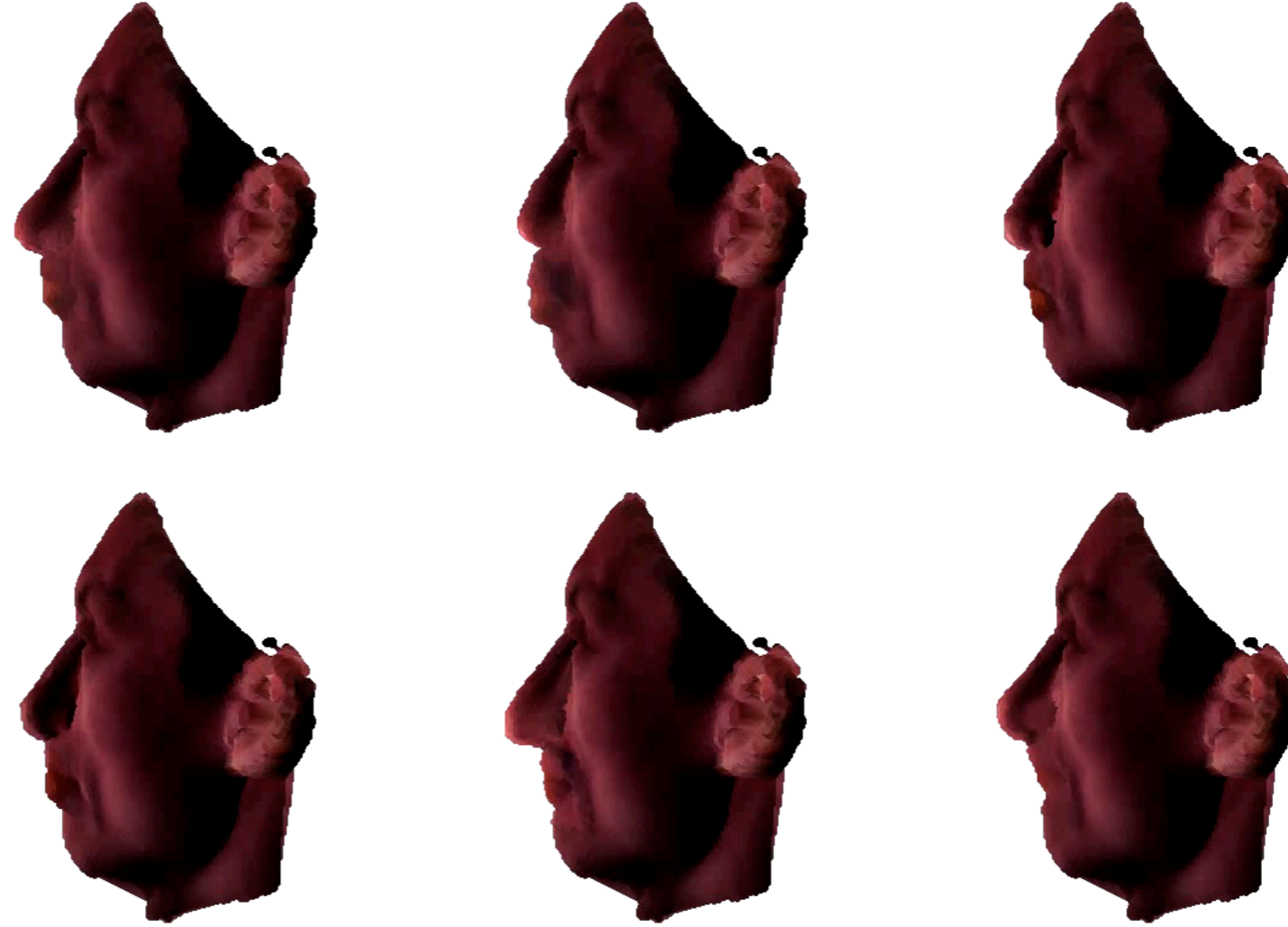


# Results





# Results





# Results





# Results



# Summary

- Inpainting and IBR.
- Complimentary.
- Voting scheme for Inpainting.
- Large texture change.
- IBR based on semantic similarity.
- Impossible views. Many variations.



# Conclusion

- MVG is very mature.
- Applications to Robotics and Video Manipulation.
- Traditional problems in these areas overcome.
- Rich MVG literature makes future interesting.



Thank You.  
Questions ?

# KLT Tracker for Illumination and Occlusion



(a)



(b) Illumination change



(c)



(d)



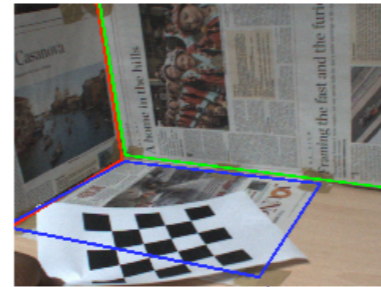
(e)



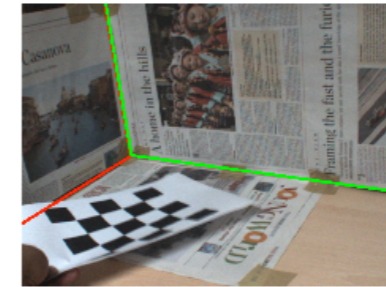
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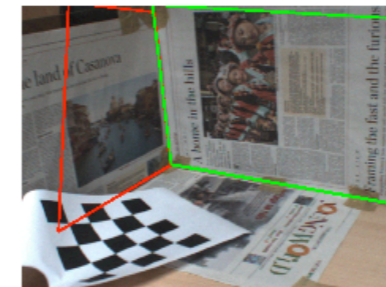
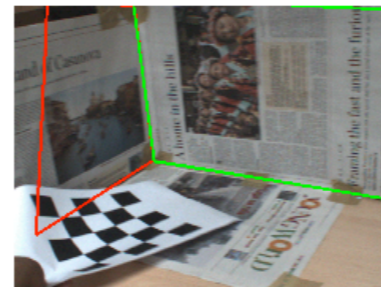
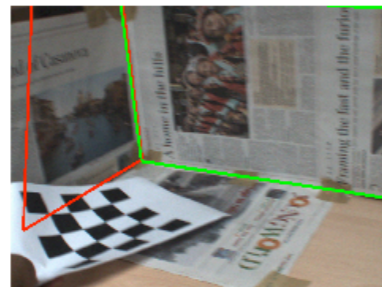
(g)



(h)



(i)





# Robotic Manipulation

# Robotic Manipulation

- Traditional sense.





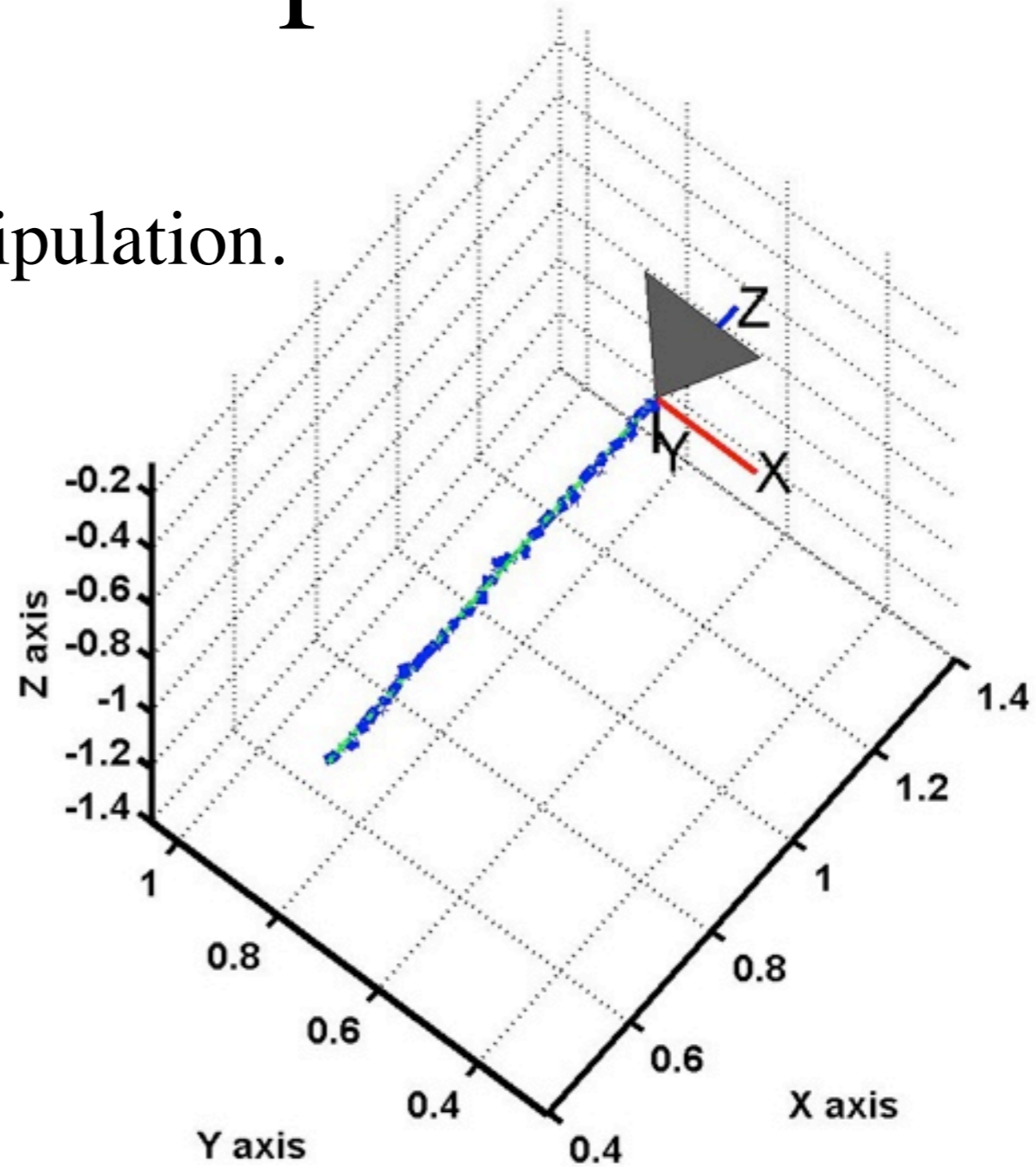
# Robotic Manipulation

- Traditional sense.



# Robotic Manipulation

- Traditional sense.
- Navigation - self manipulation.



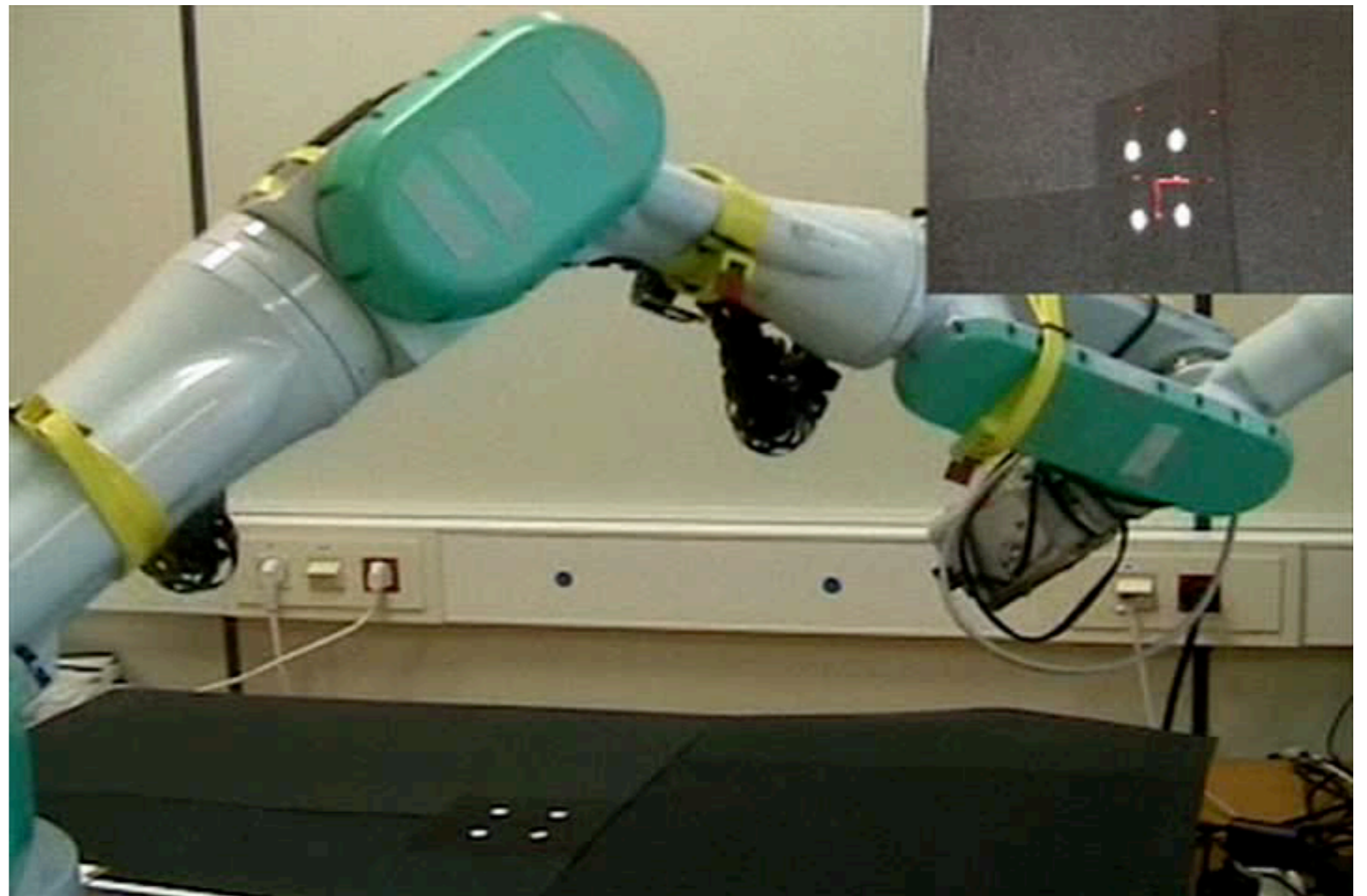


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- Traditional sense.
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- Traditional sense.
- Navigation - self manipulation.
- Visual Servoing.





# Robotic Manipulation

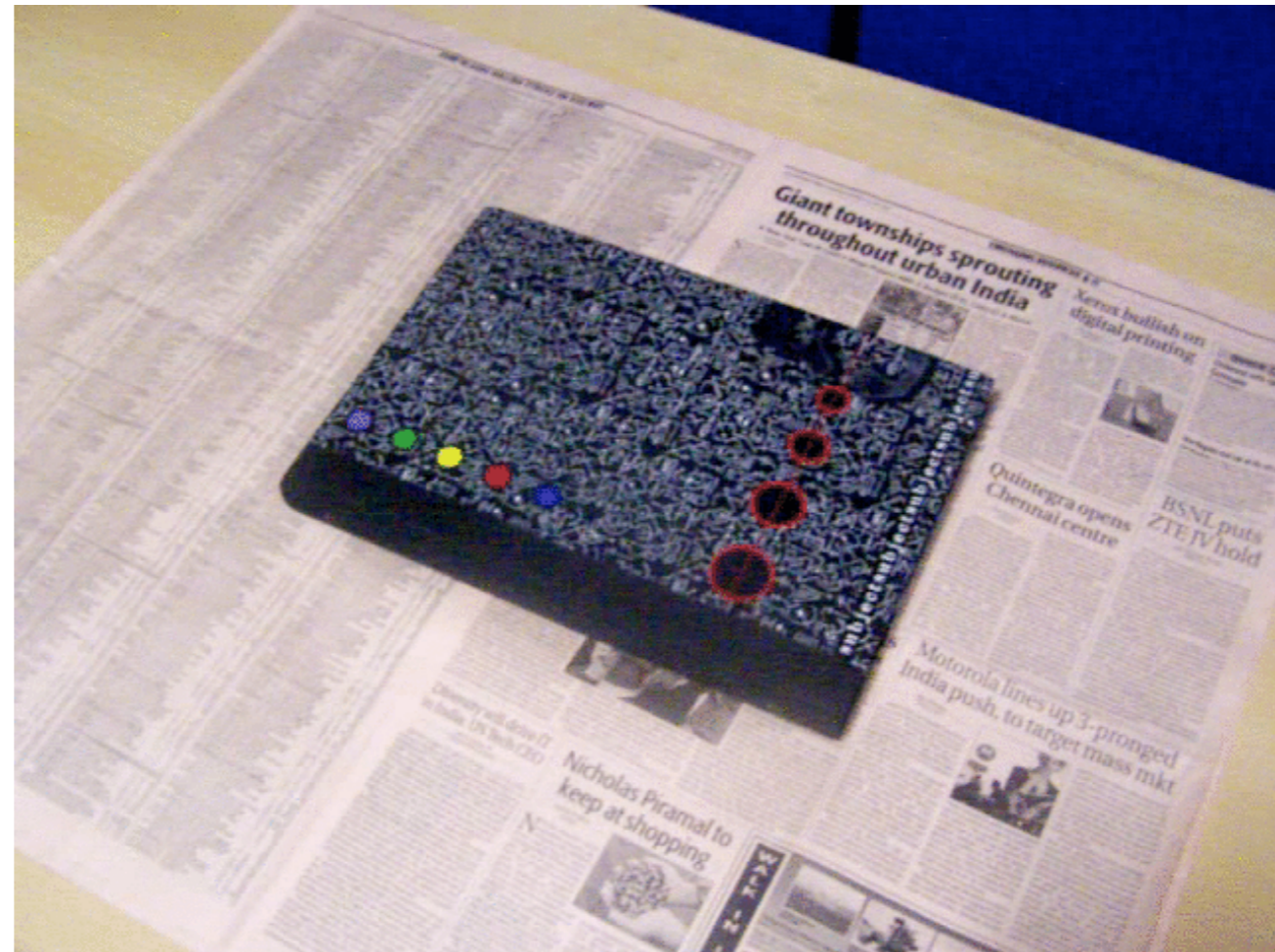
- Traditional sense.
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# Tracking Challenges

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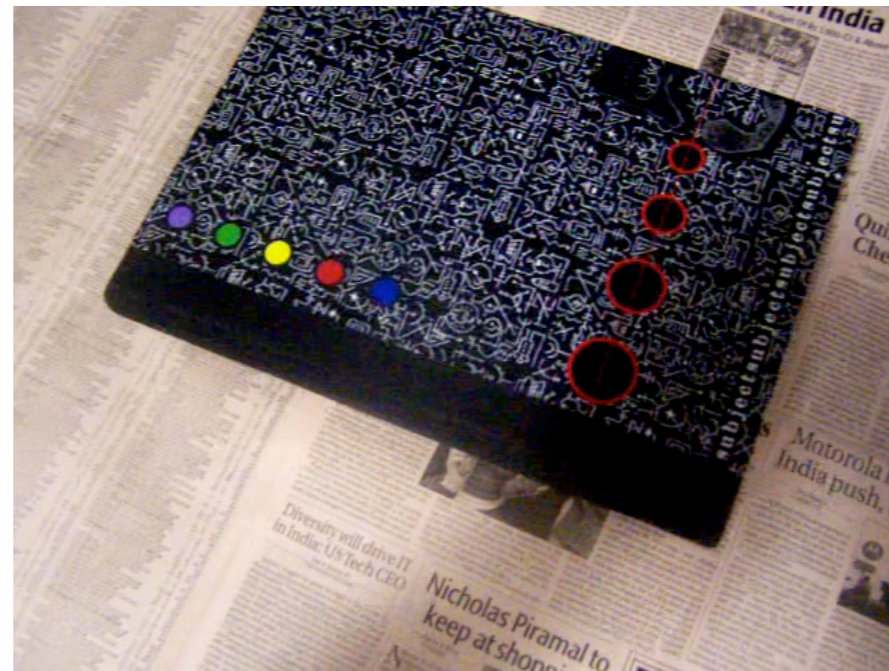
- Motion





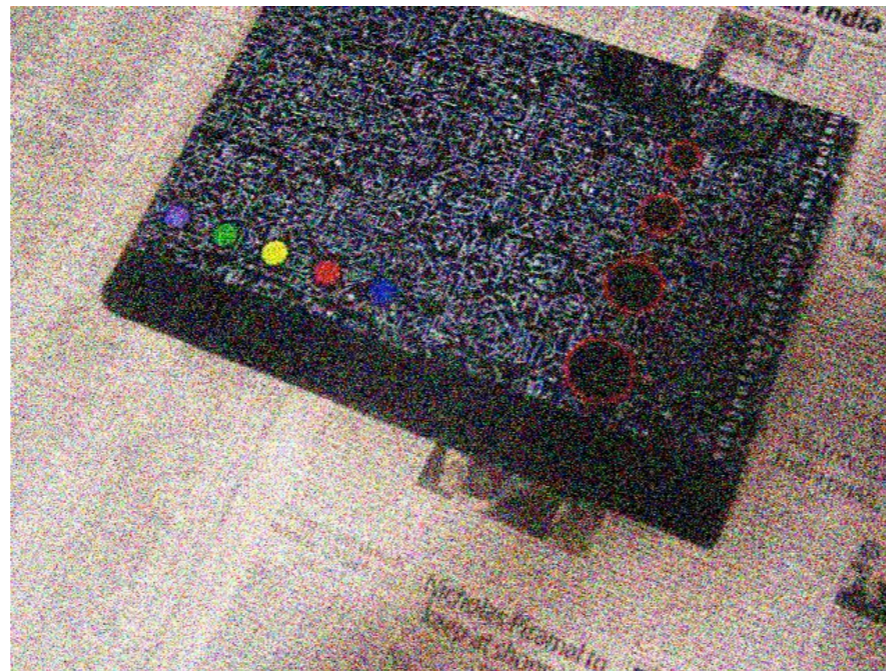
# Tracking Challenges

- Motion
- Illumination



# Tracking Challenges

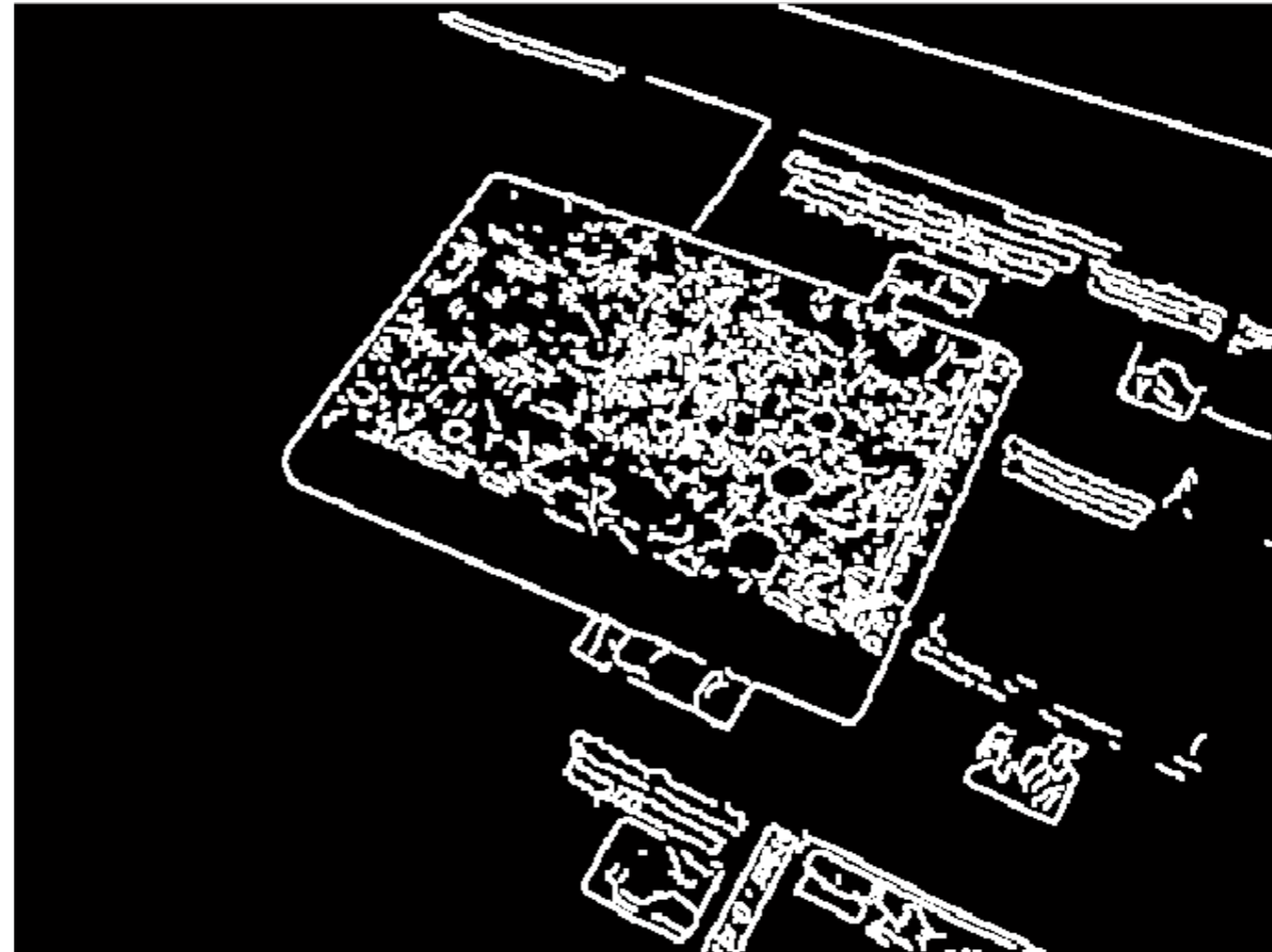
- Motion
- Illumination
- Noise and Blur



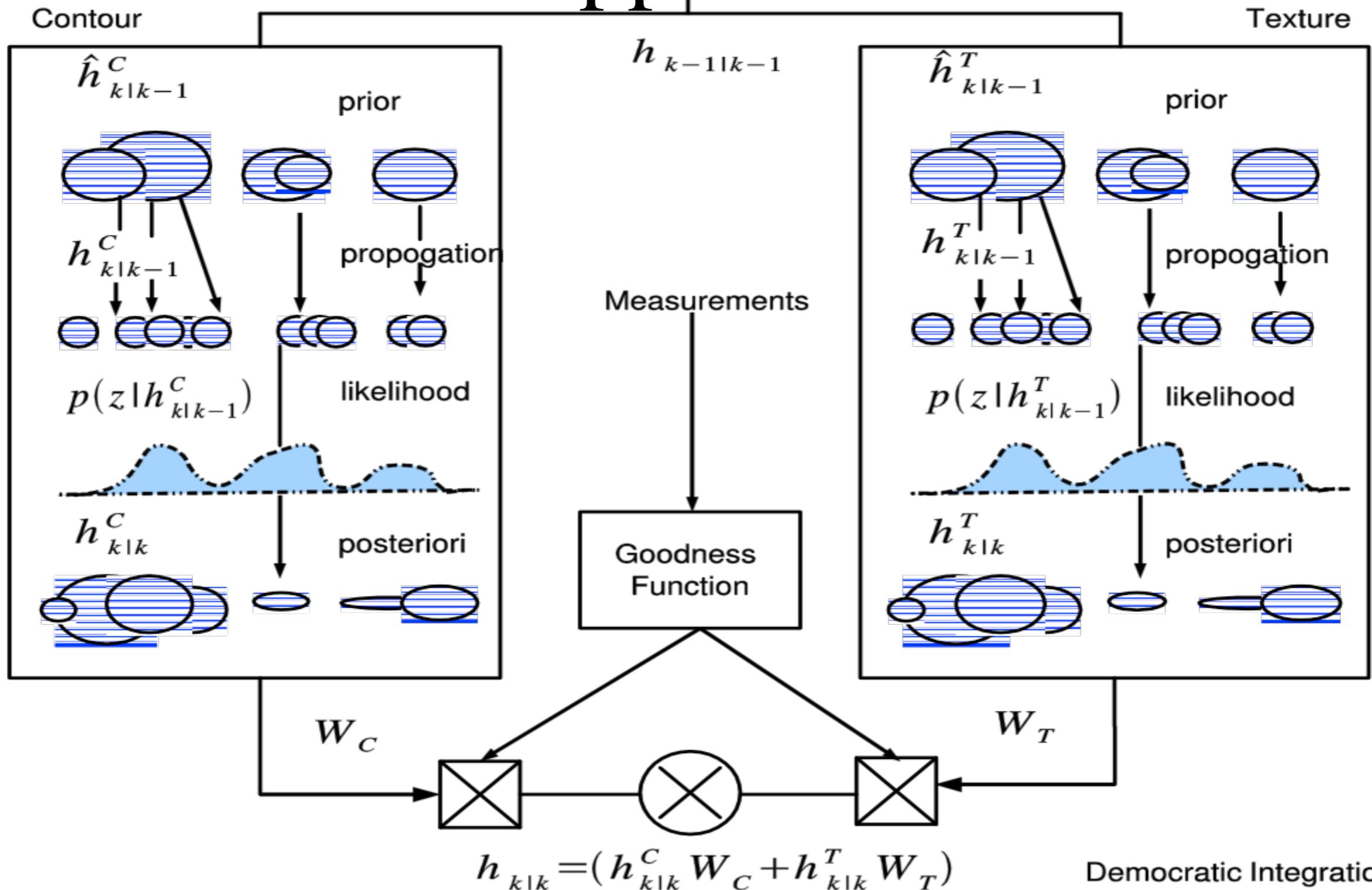


# Tracking Challenges

- Motion
- Illumination
- Noise and Blur
- Clutter



# Approach

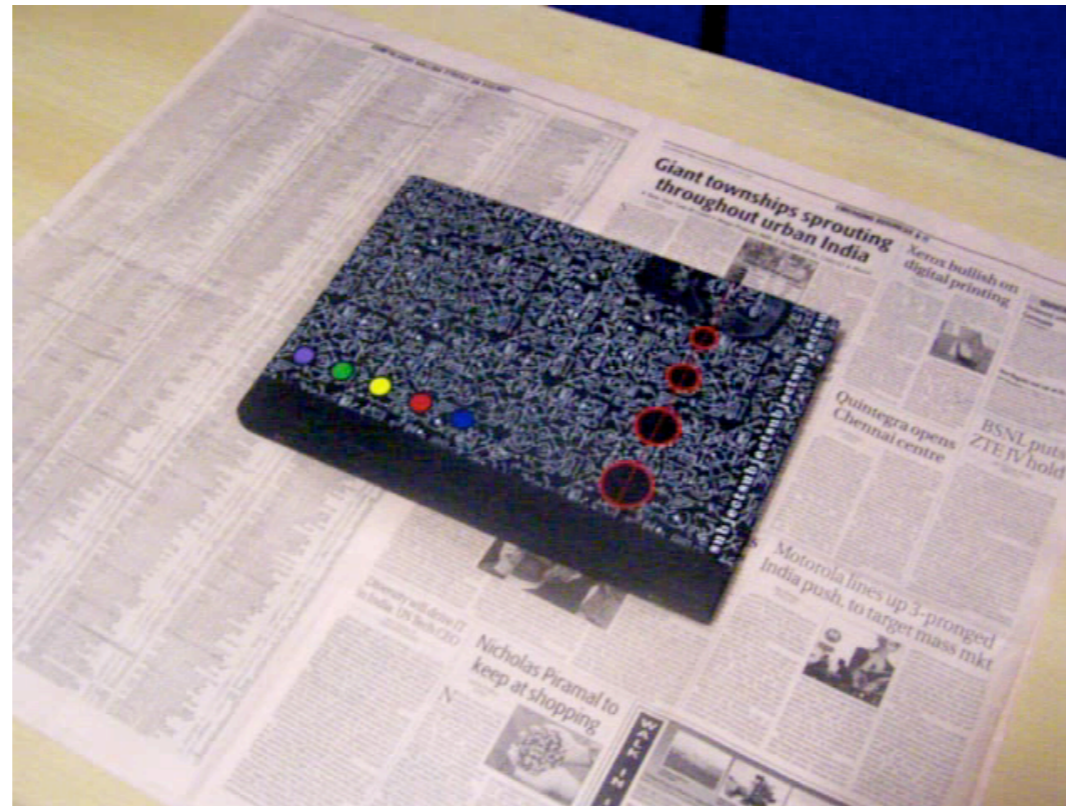




# Texture information

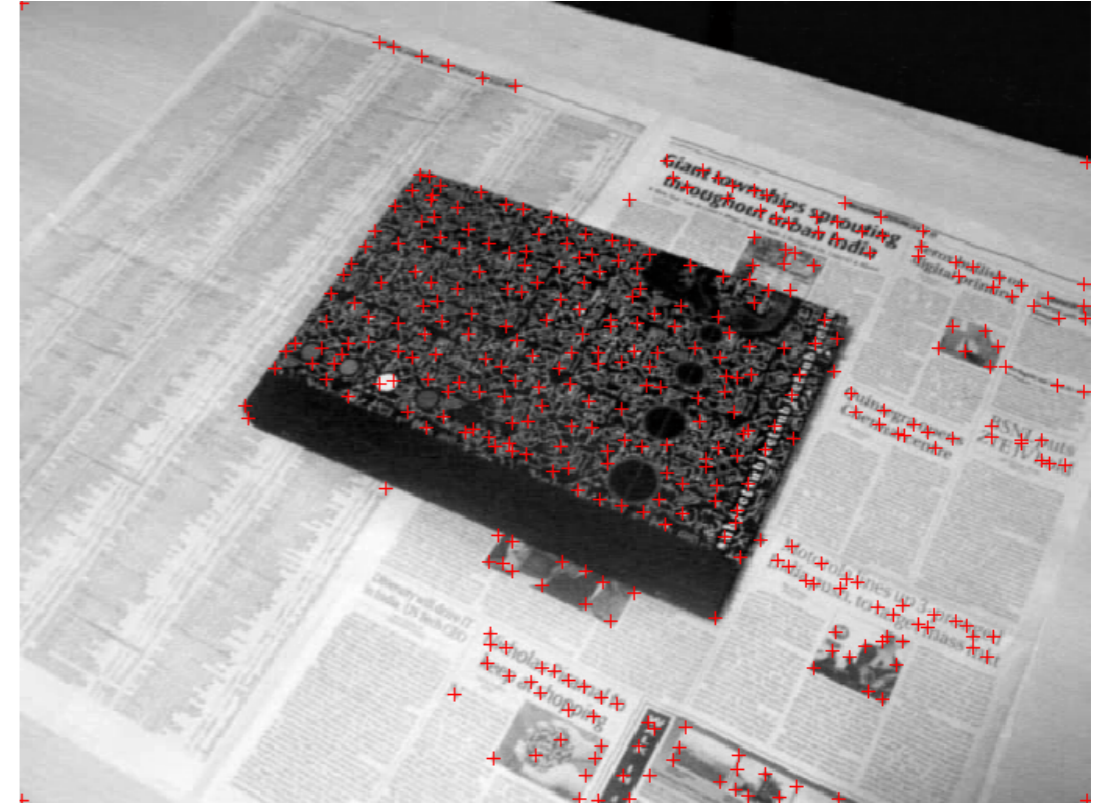


# Texture information



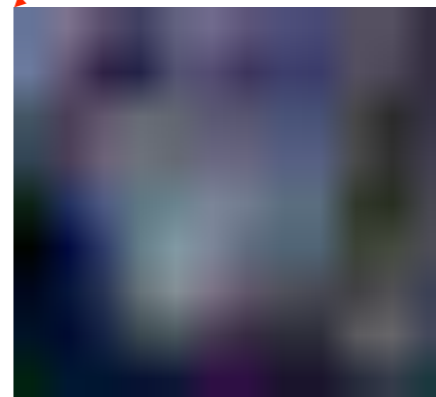
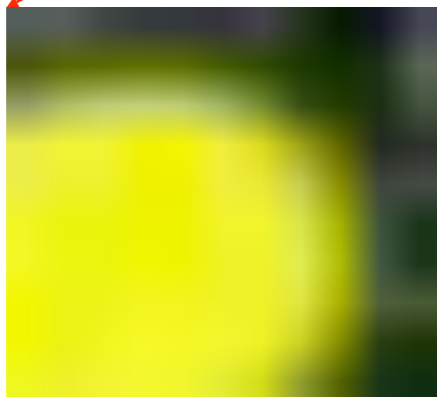
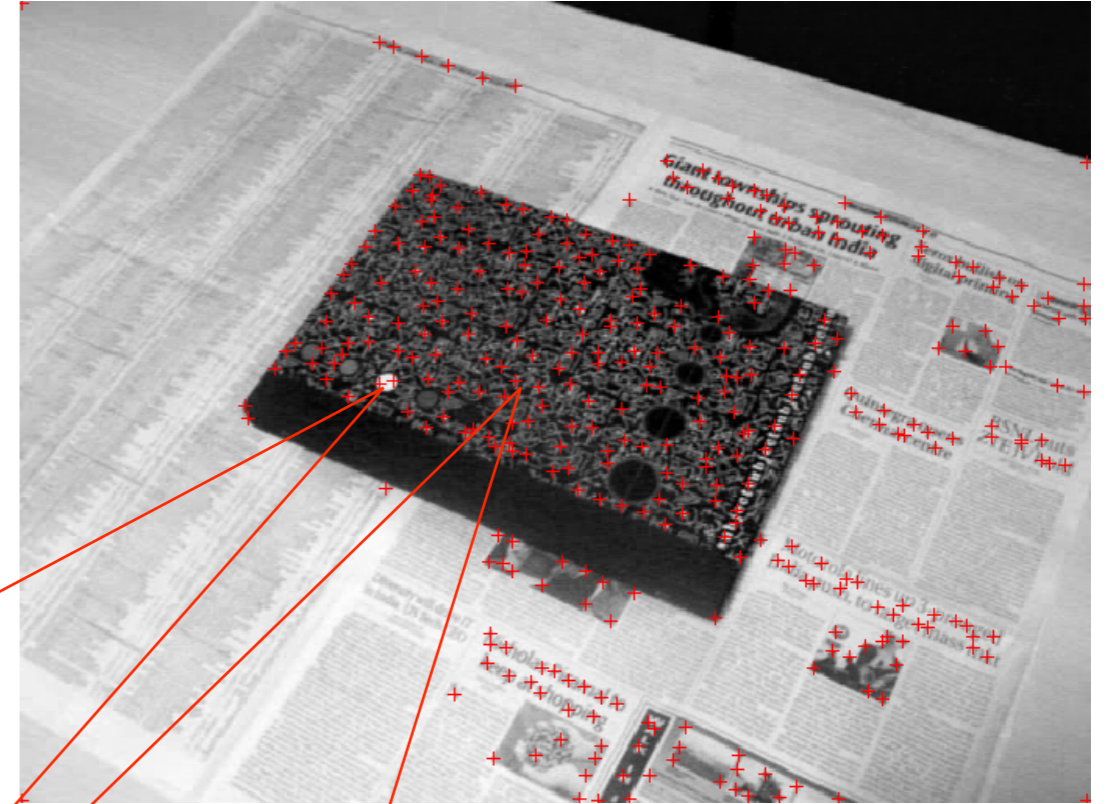
# Texture information

- Texture points.



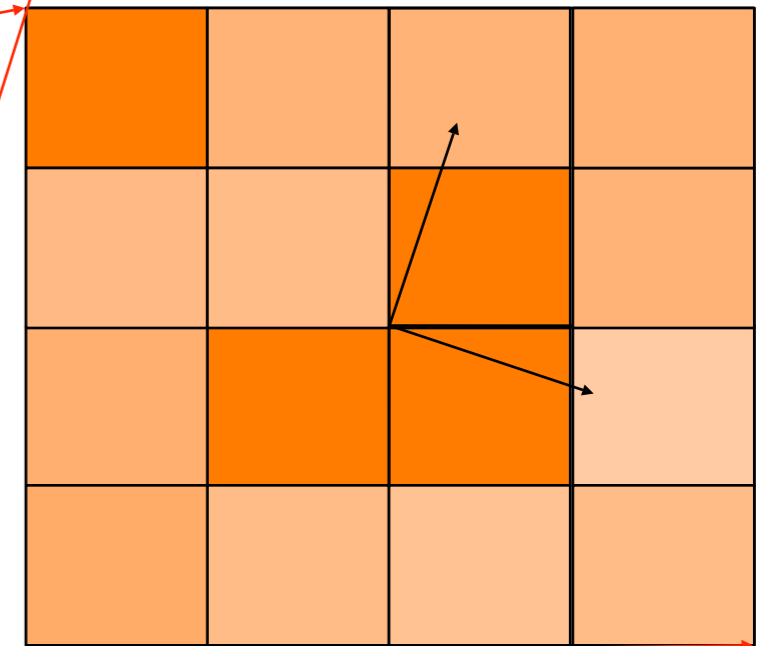
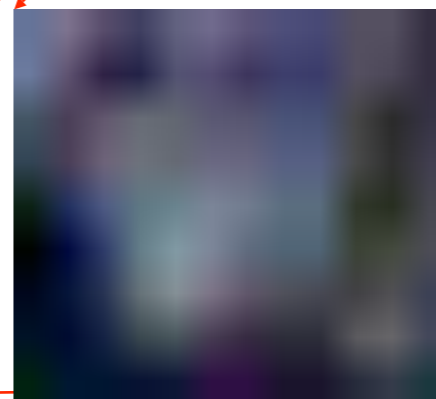
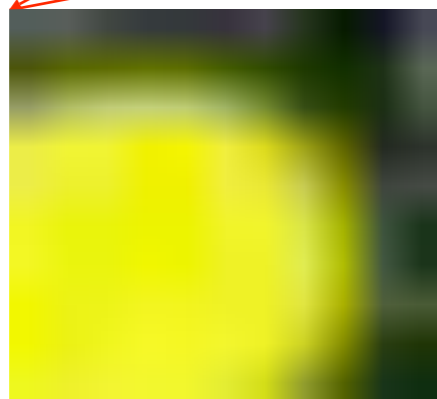
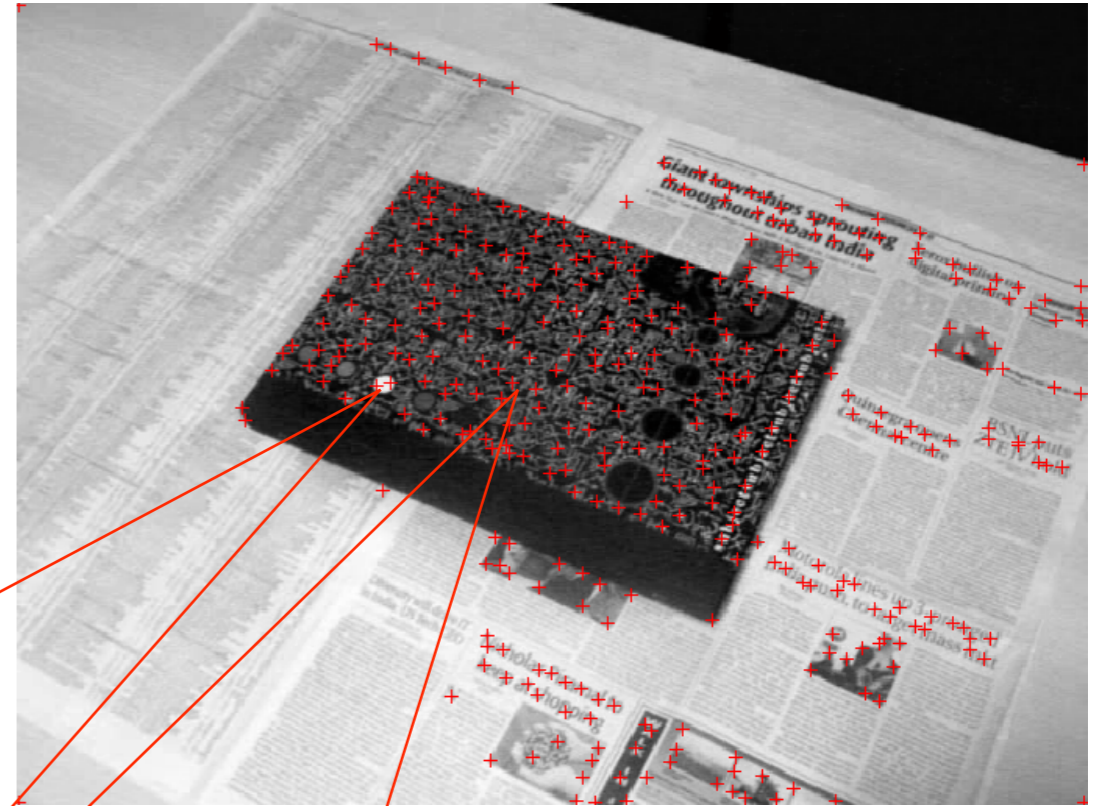
# Texture information

- Texture points.
- Consider image patches.



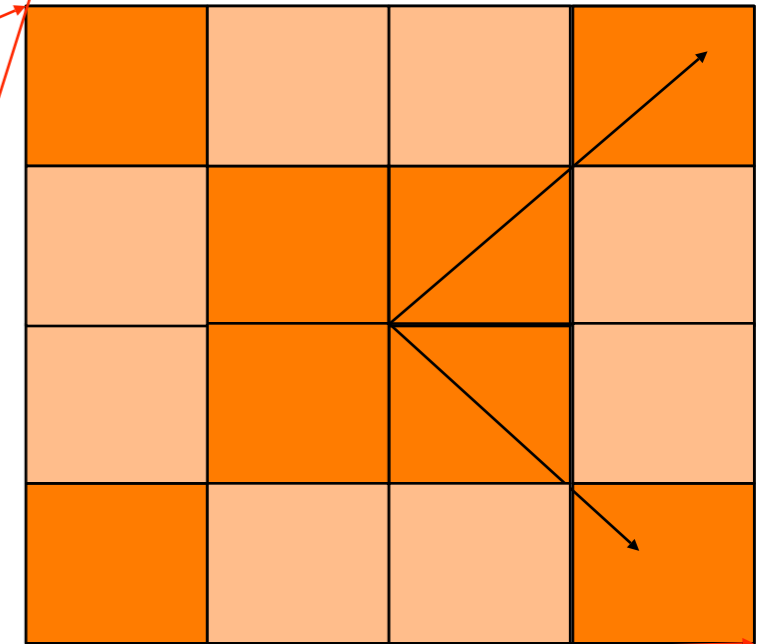
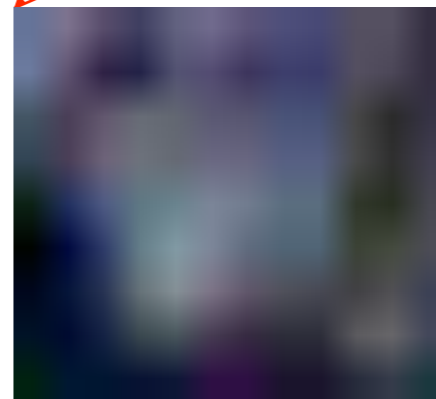
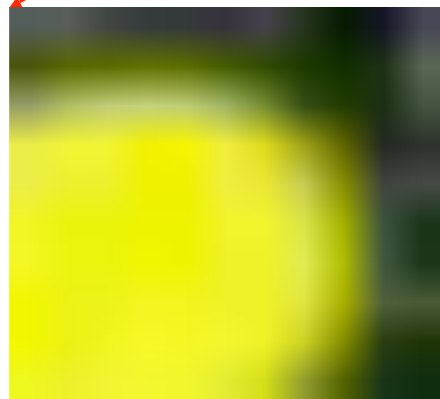
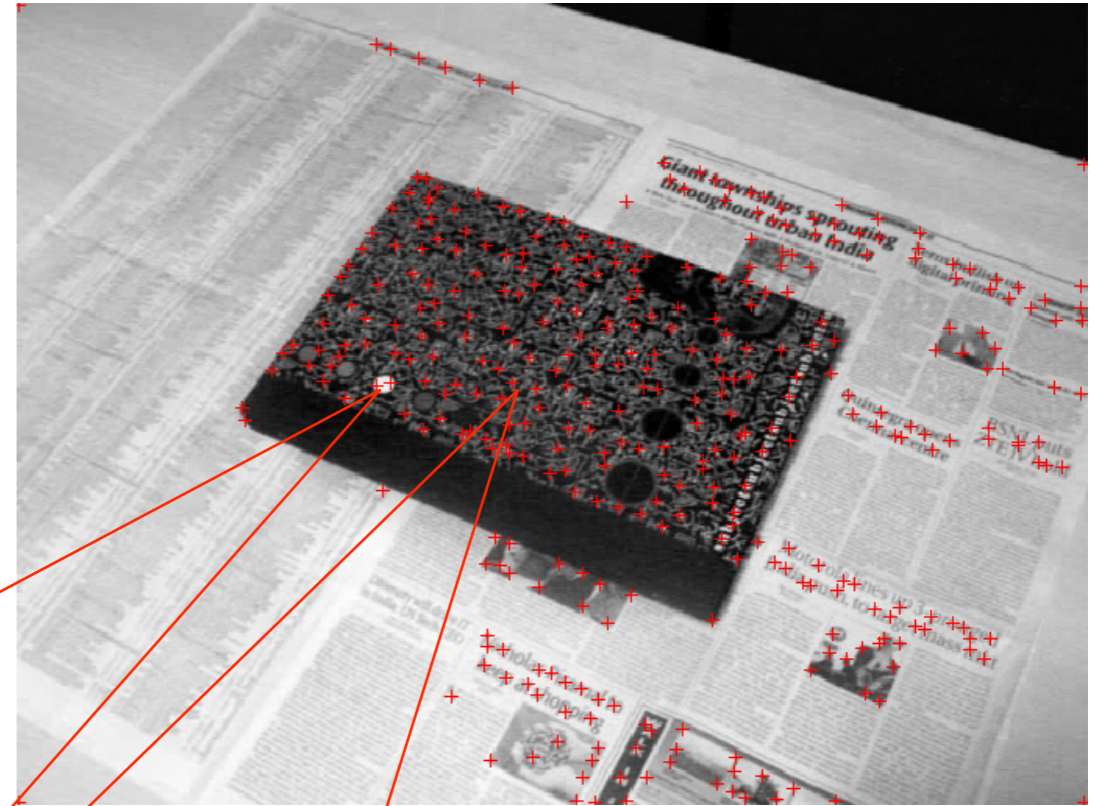
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- Consider image patches.
- Good/Bad features.



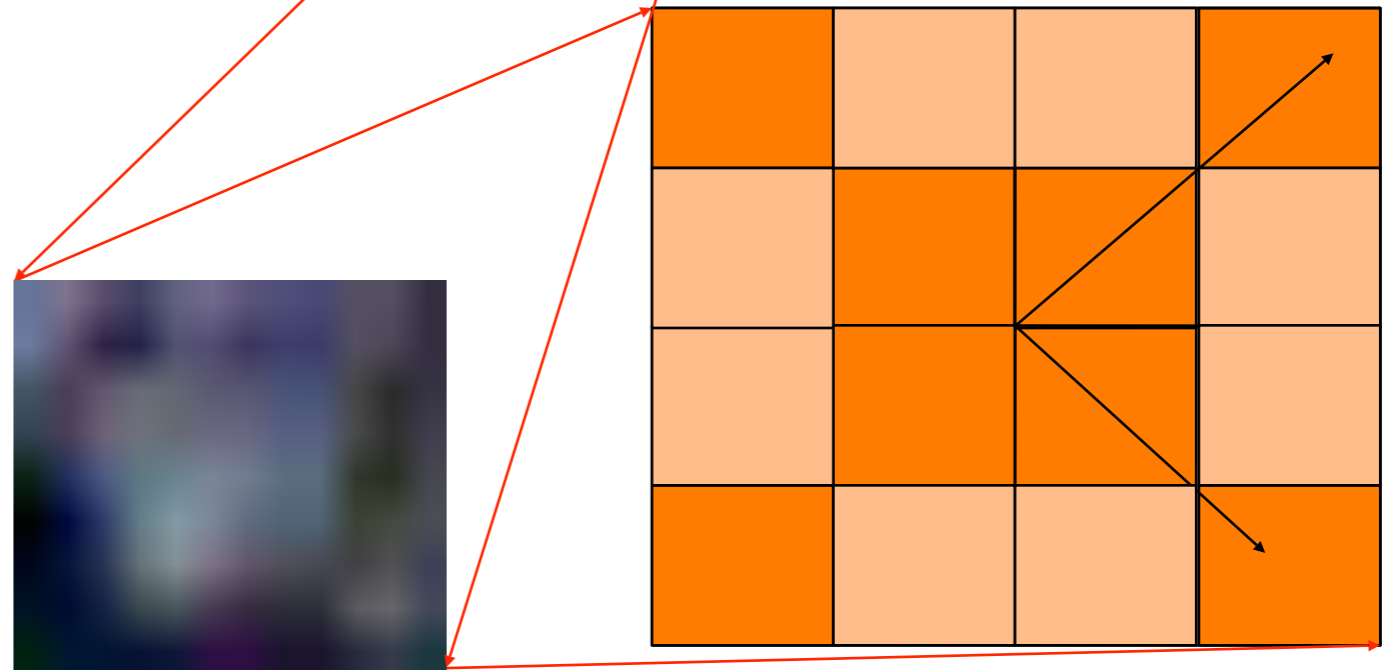
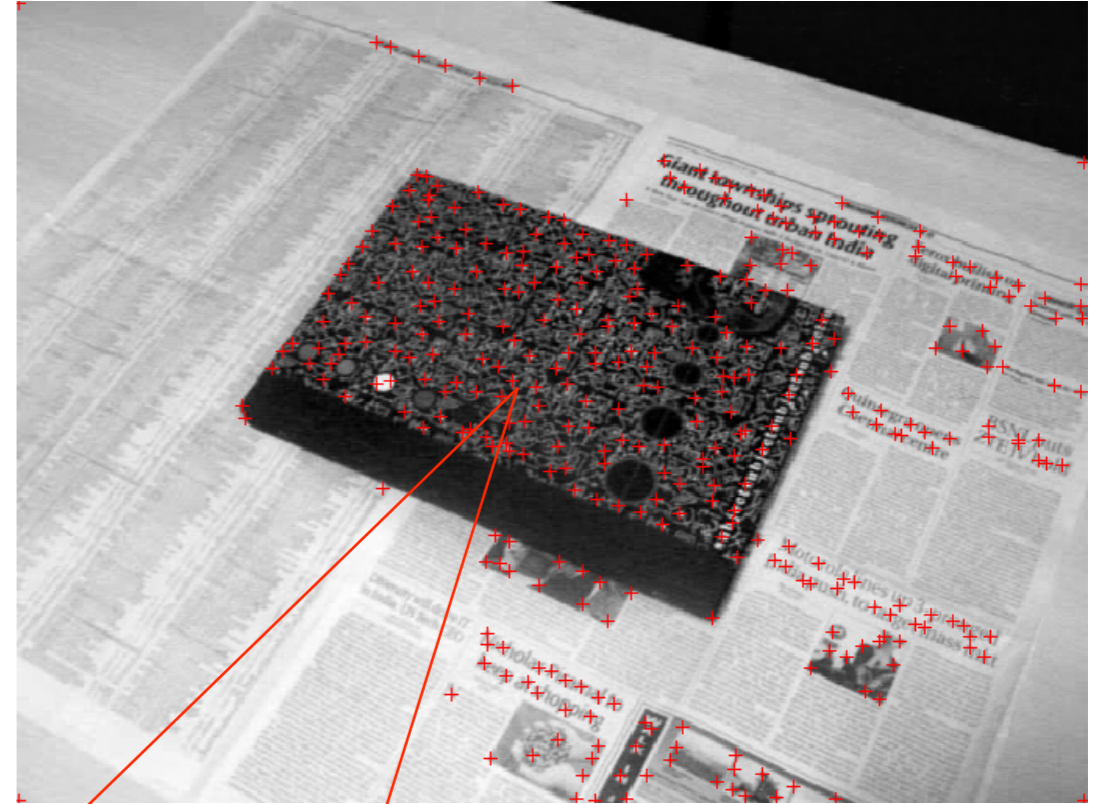
# Texture information

- Texture points.
- Consider image patches.
- Good/Bad features.
- Represented by large eigenvalues of covariance matrix.
- Condition for good texture.



# Texture information

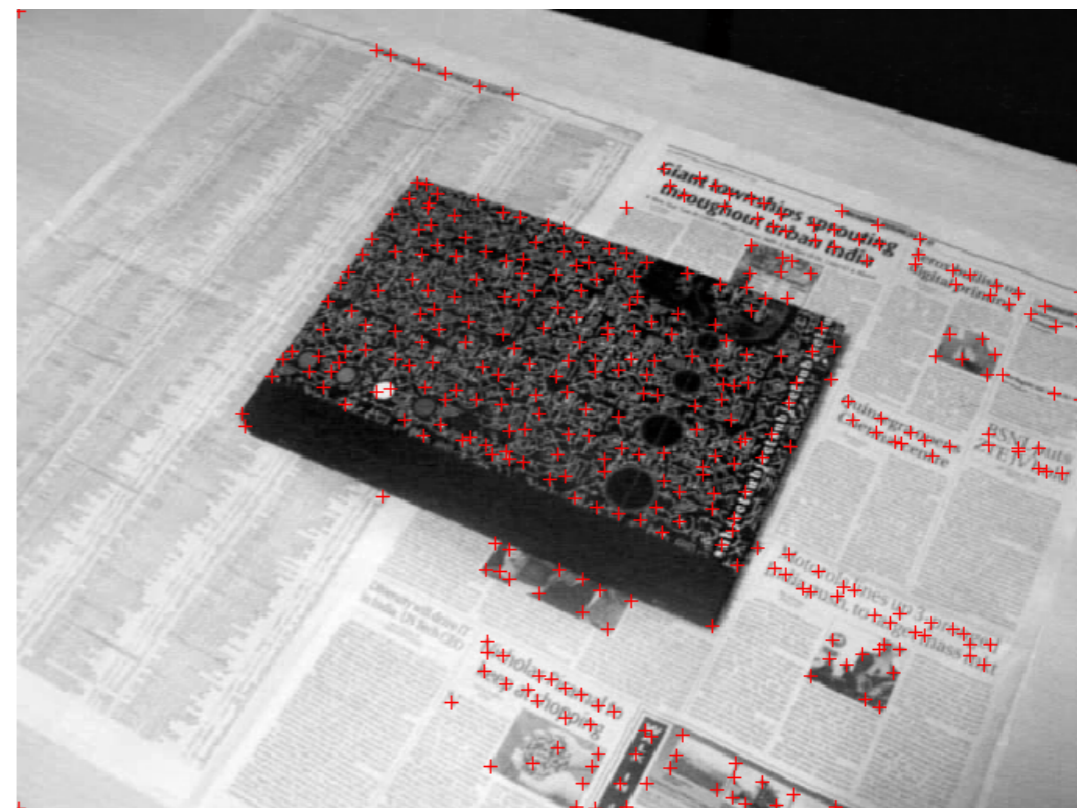
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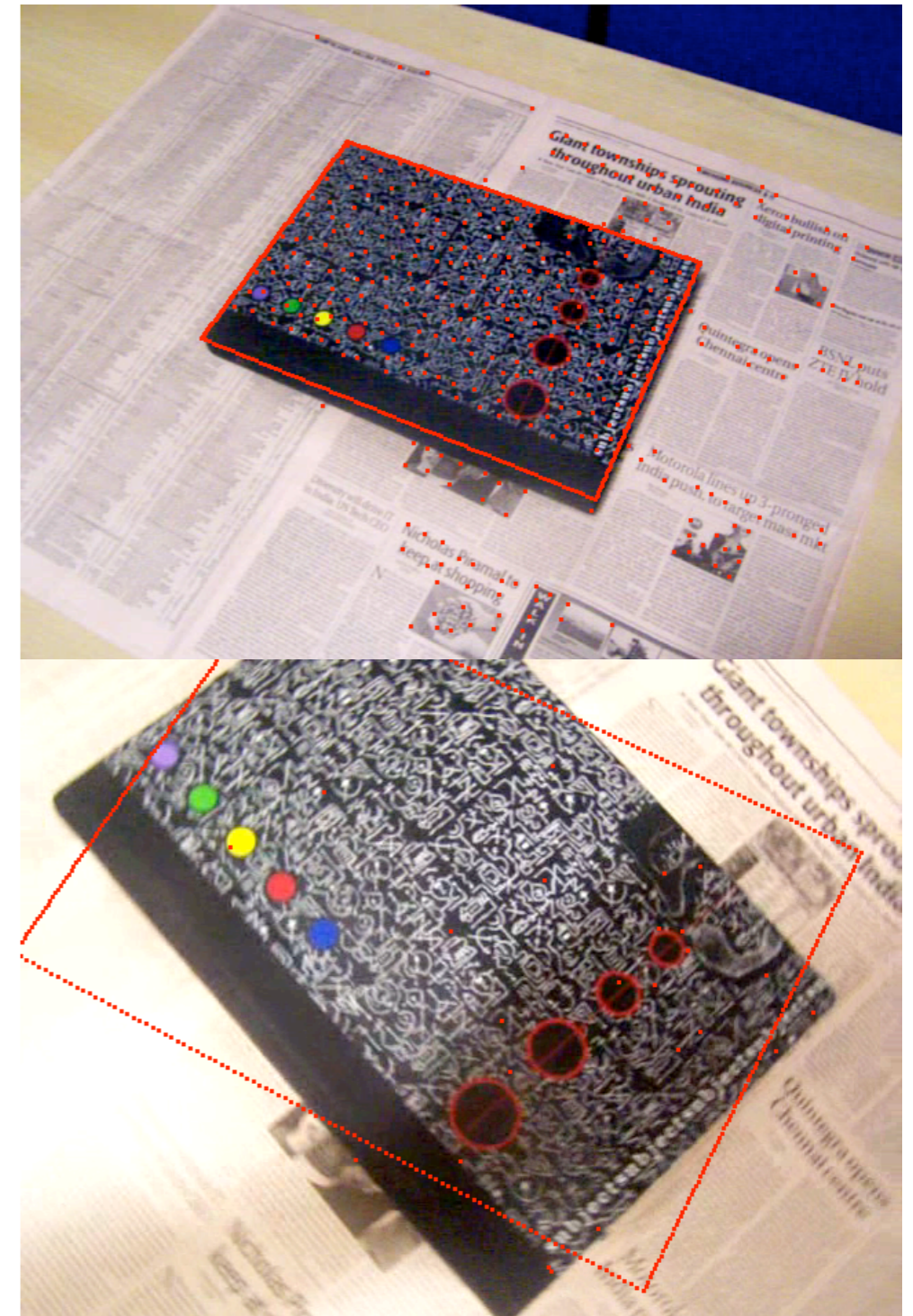
$$\min(\lambda_1, \lambda_2) > t$$



# Texture - Drawbacks

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Loss/Inaccuracy in tracking may result because of :-



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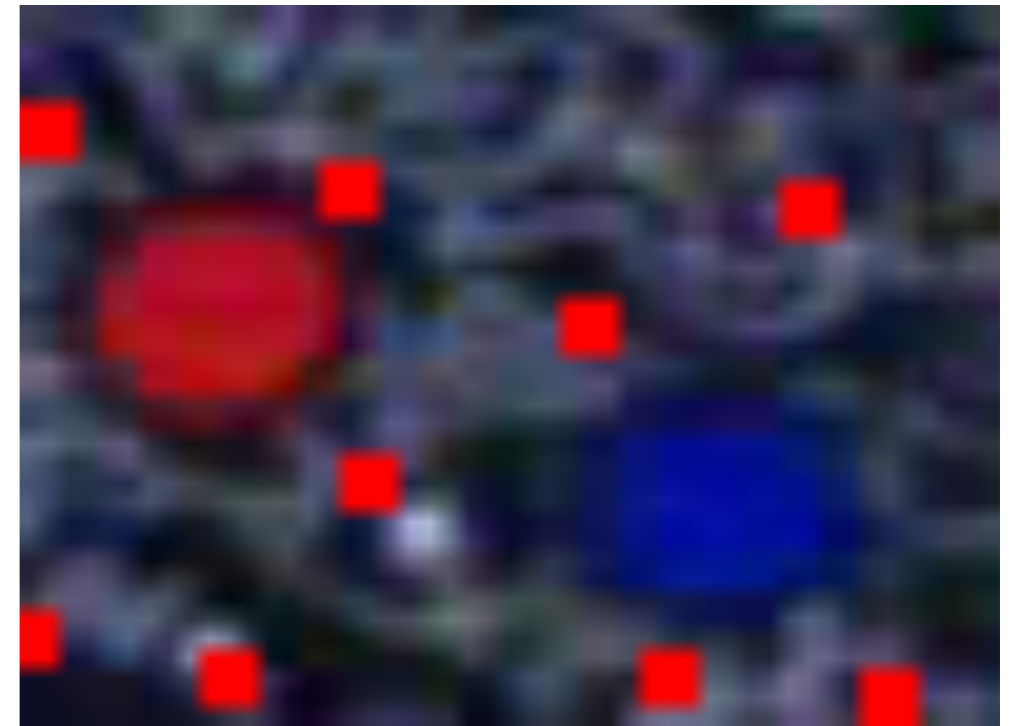
- Large motion.



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Loss/Inaccuracy in tracking may result because of :-

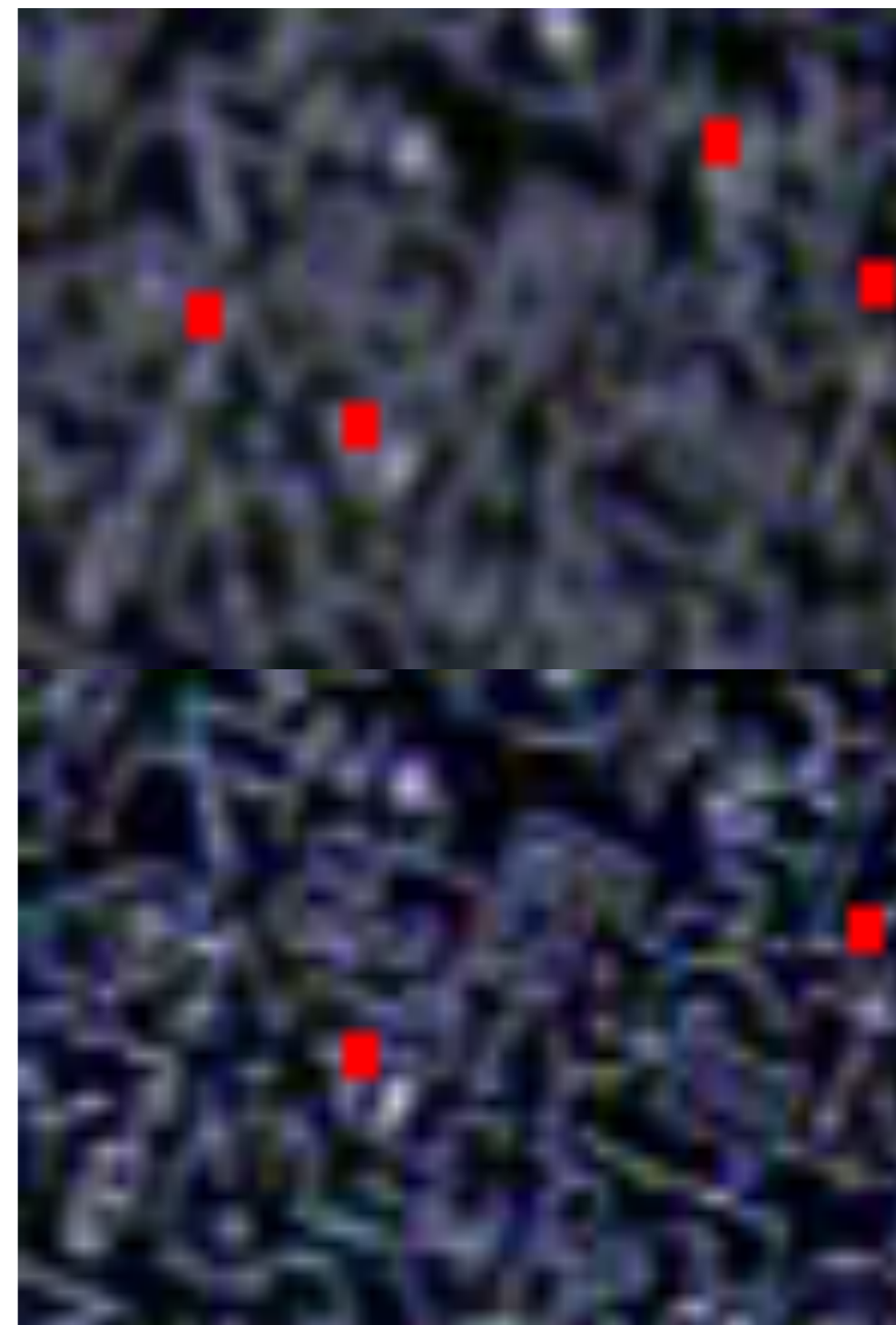
- Large motion.
- Large illumination change.



# Texture - Drawbacks

Loss/Inaccuracy in tracking may result because of :-

- Large motion.
- Large illumination change.
- Noise / Blur.





# Contour Information

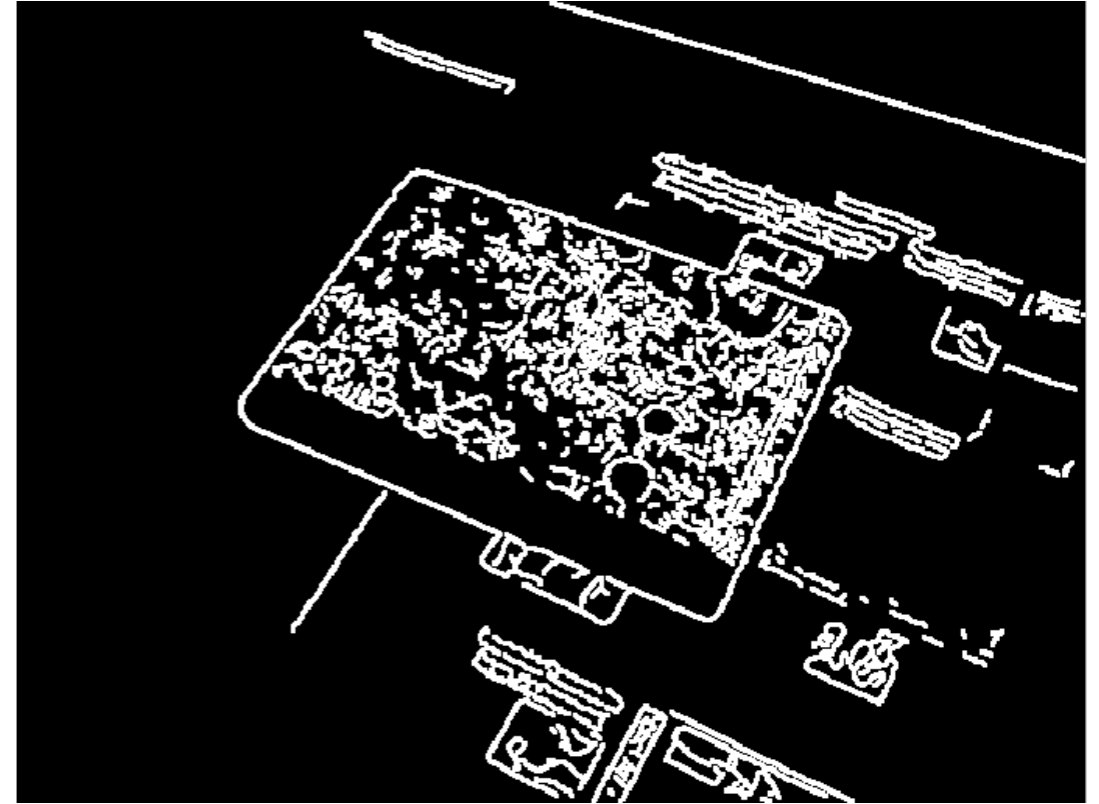


# Contour Information



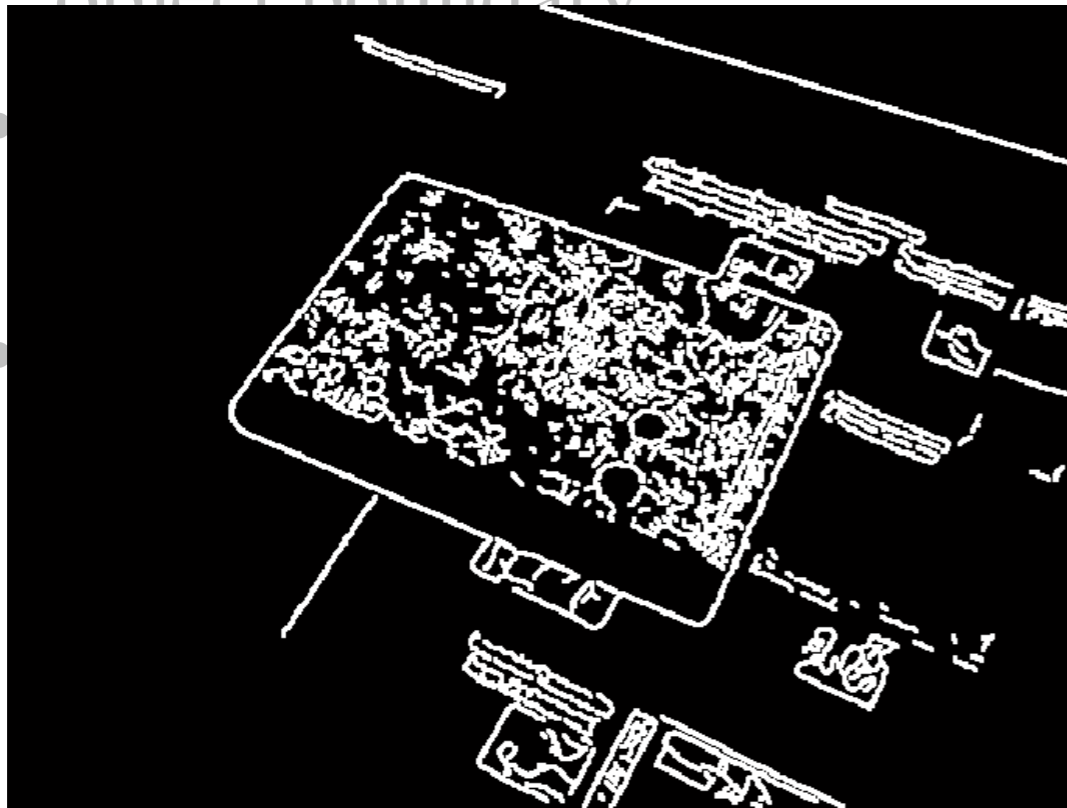
# Contour Information

- Represent edge information of object boundary.



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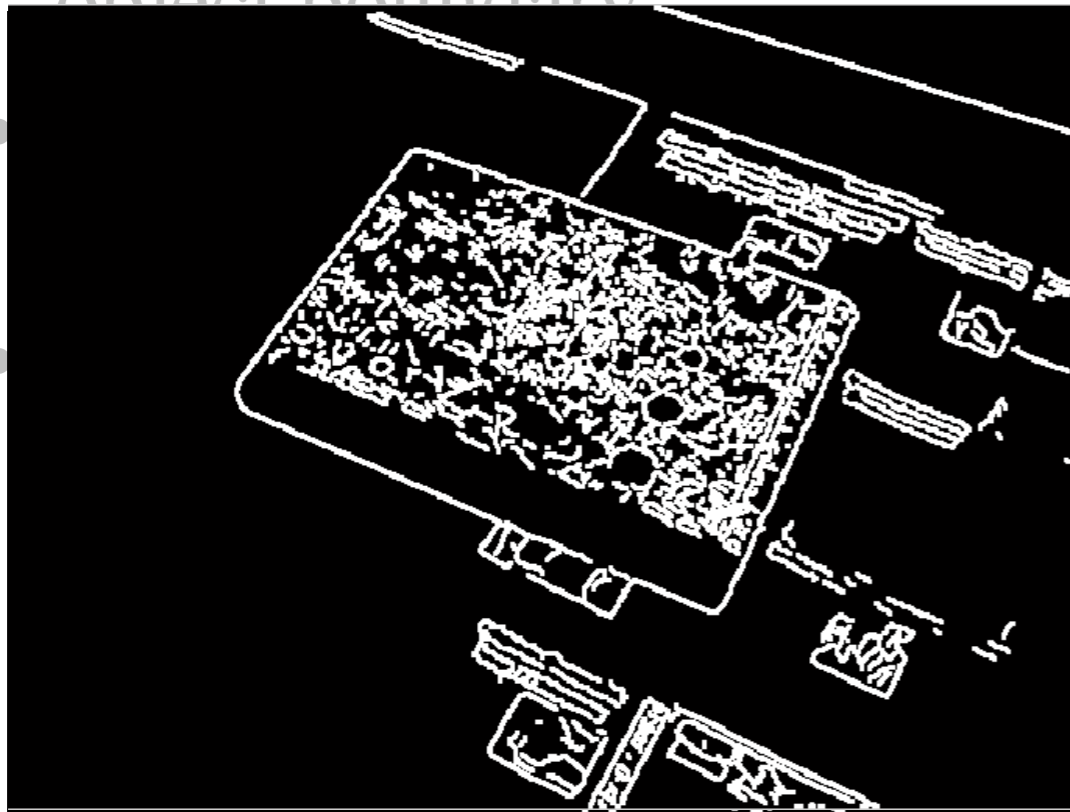


rst

h

# Contour Information

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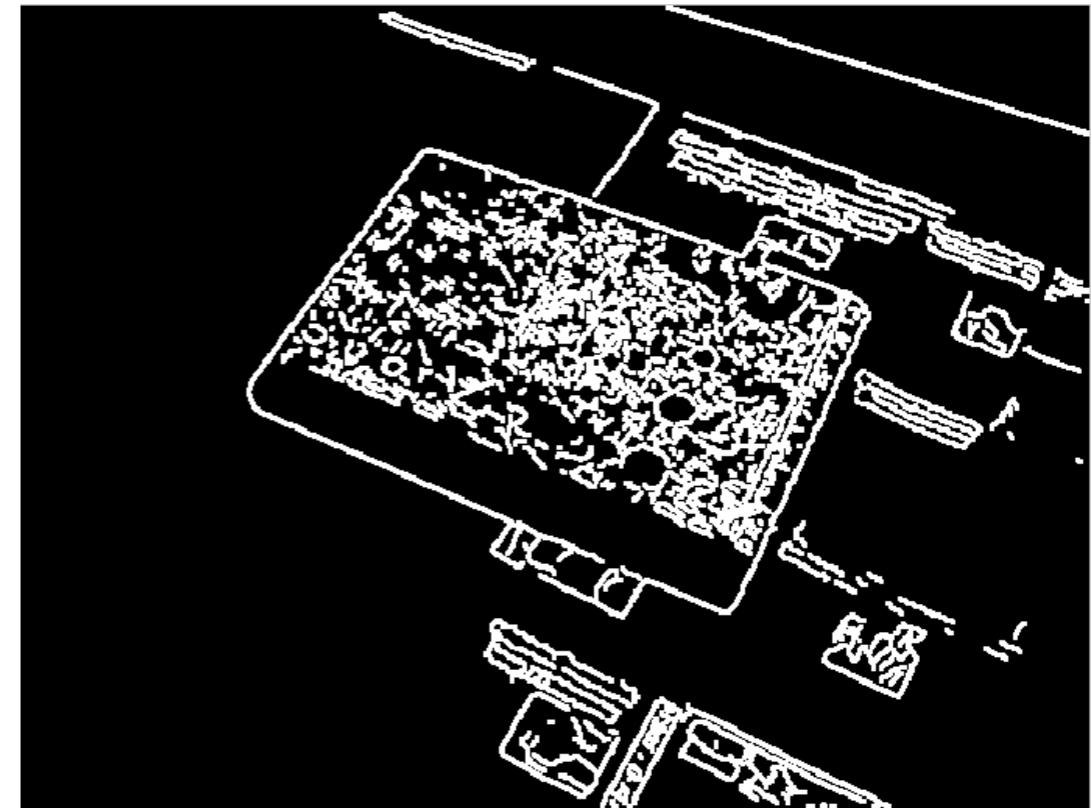
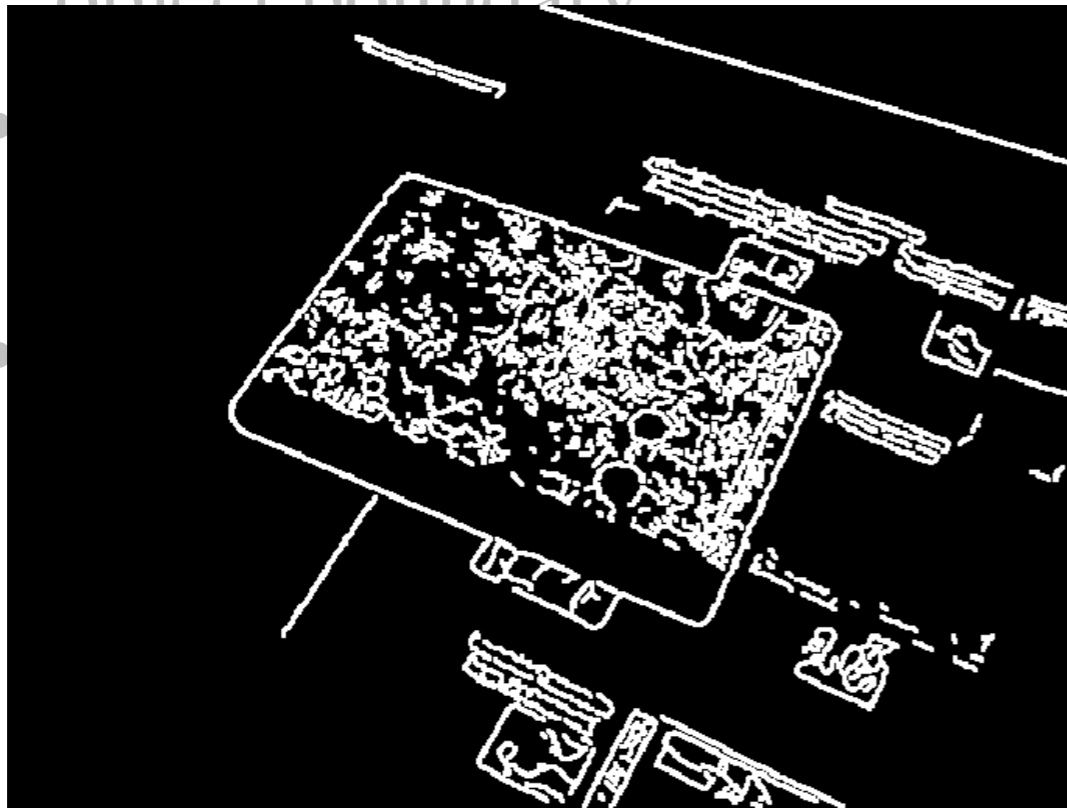


rst

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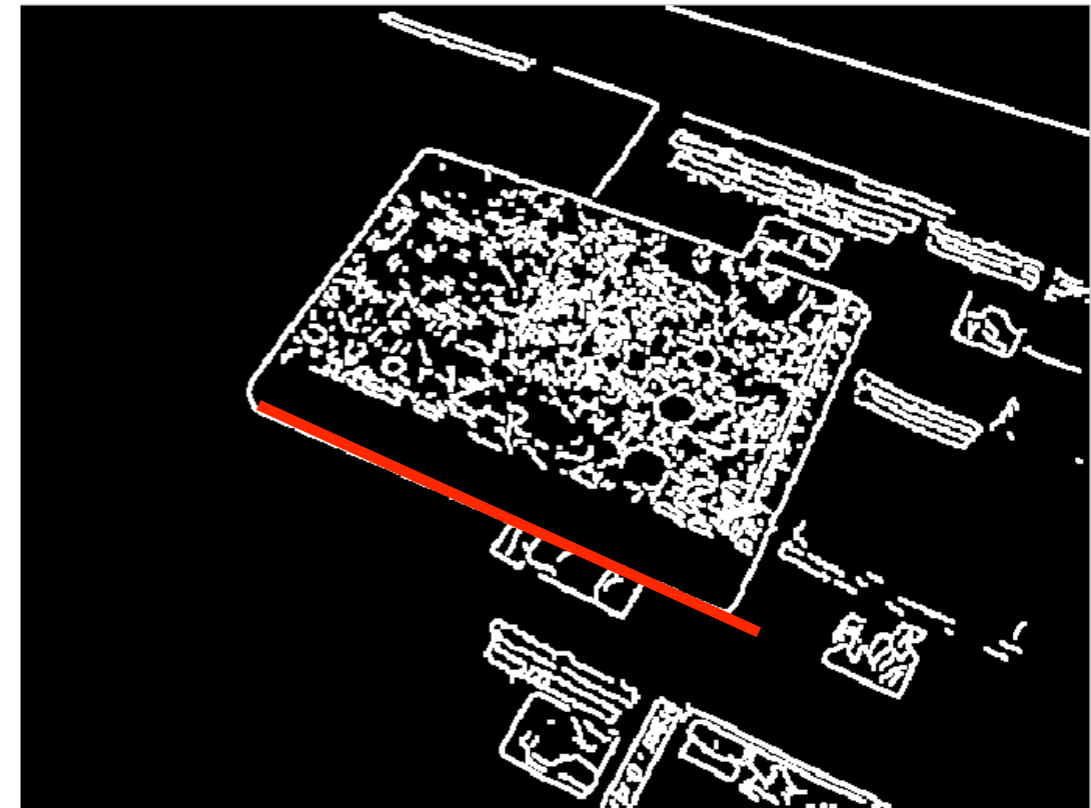
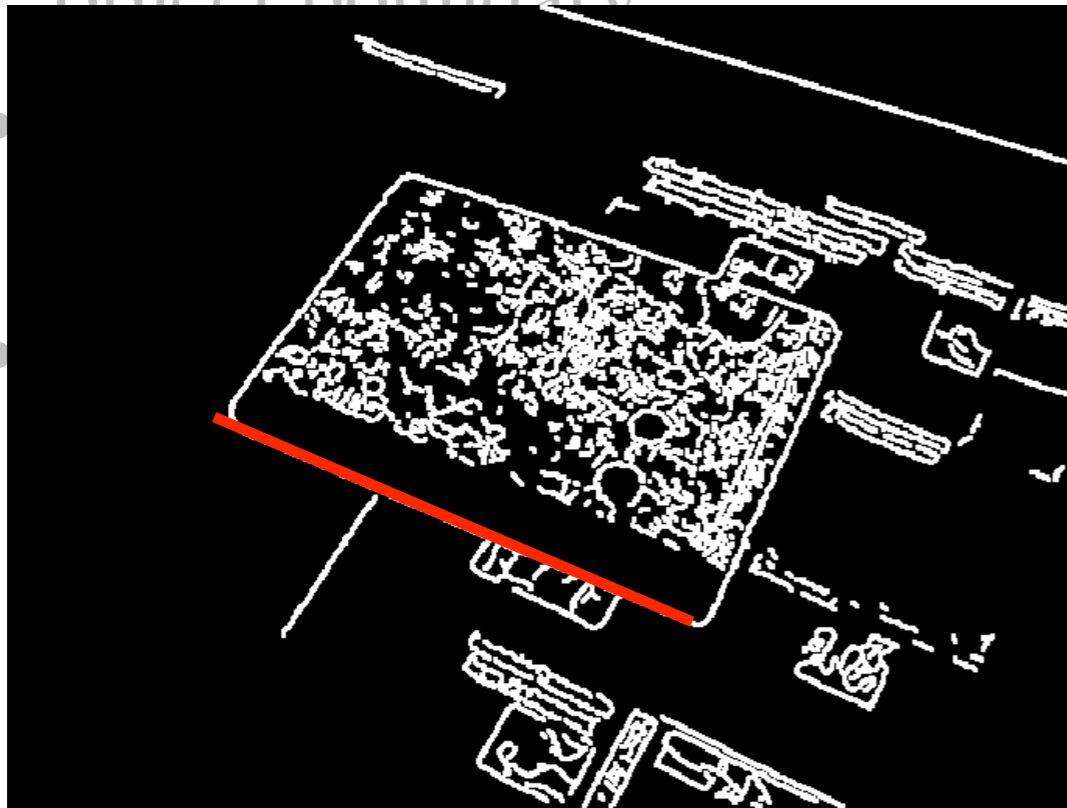


rst

h

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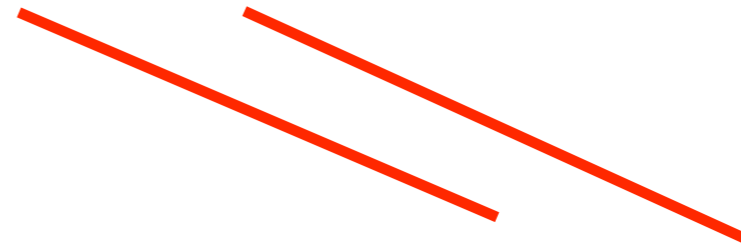


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# Contour Information

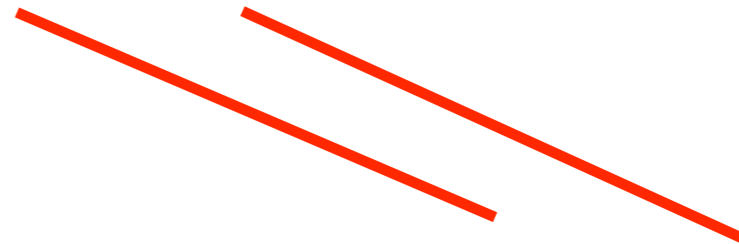
- Represent edge information of object boundary.
- Select certain points along first contour.





# Contour Information

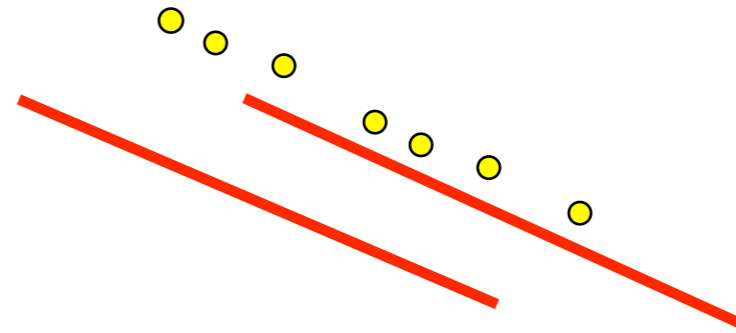
- Represent edge information of object boundary.
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- Find correspondence through search along normal





# Contour Information

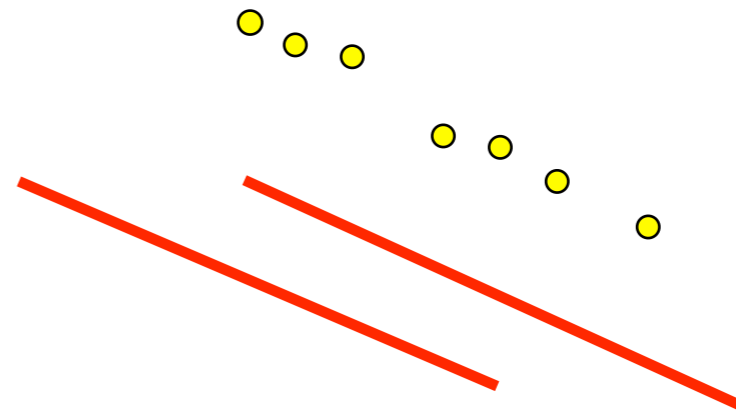
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# Contour - Drawbacks



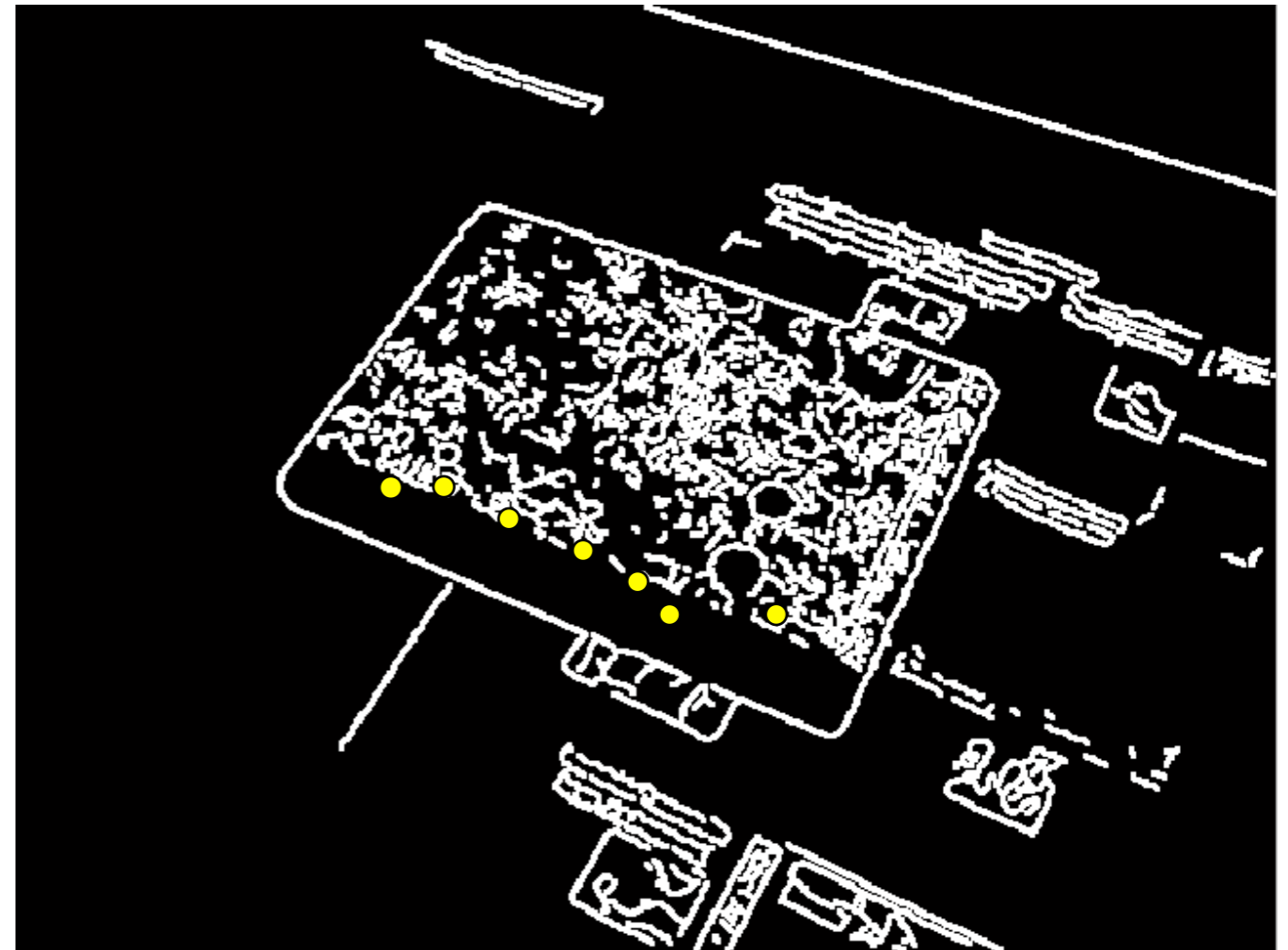
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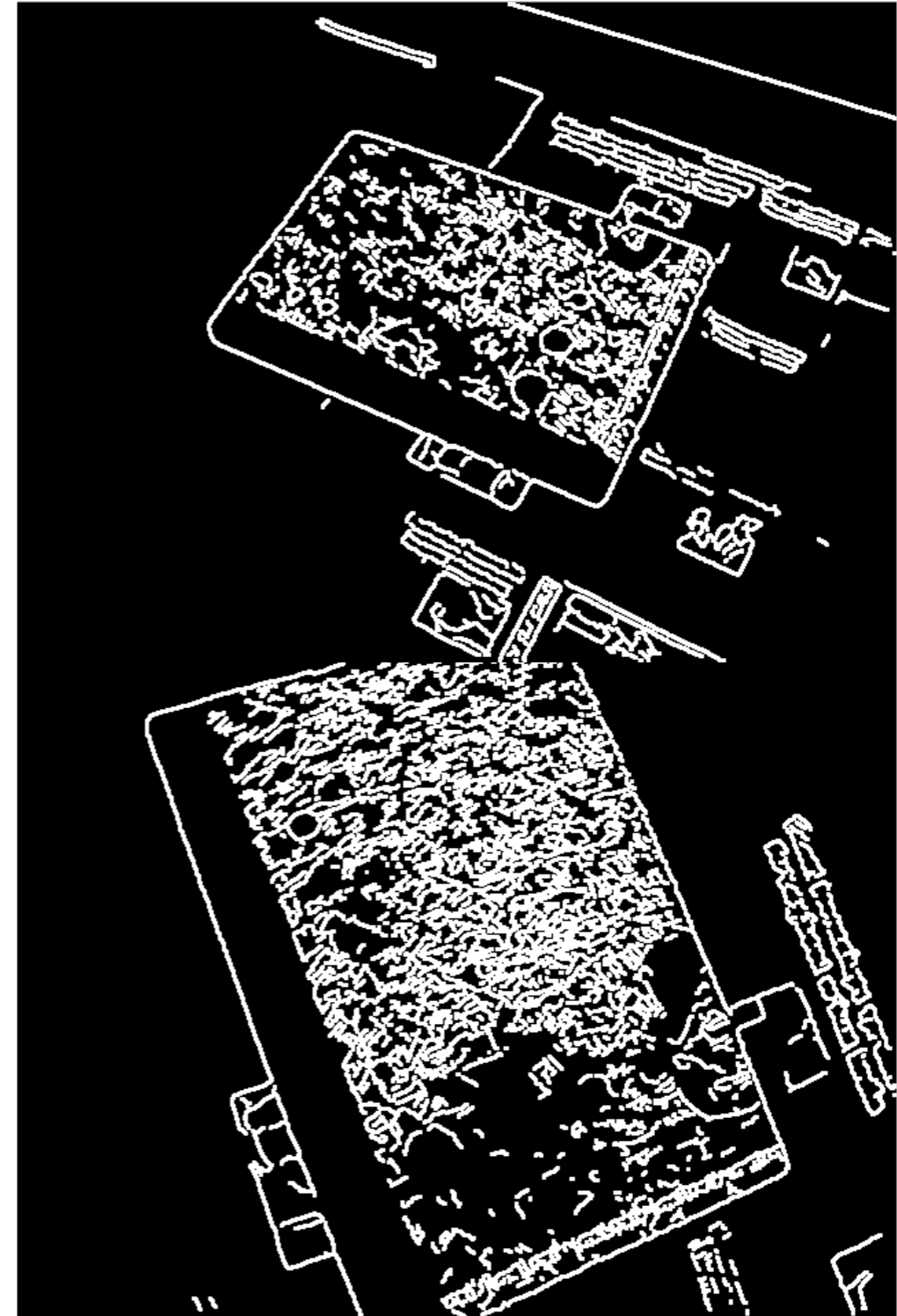
- Background clutter.



# Contour - Drawbacks

Loss/Inaccuracy in tracking may result because of :-

- Background clutter.
- Shadow/illumination – edge might be lost.



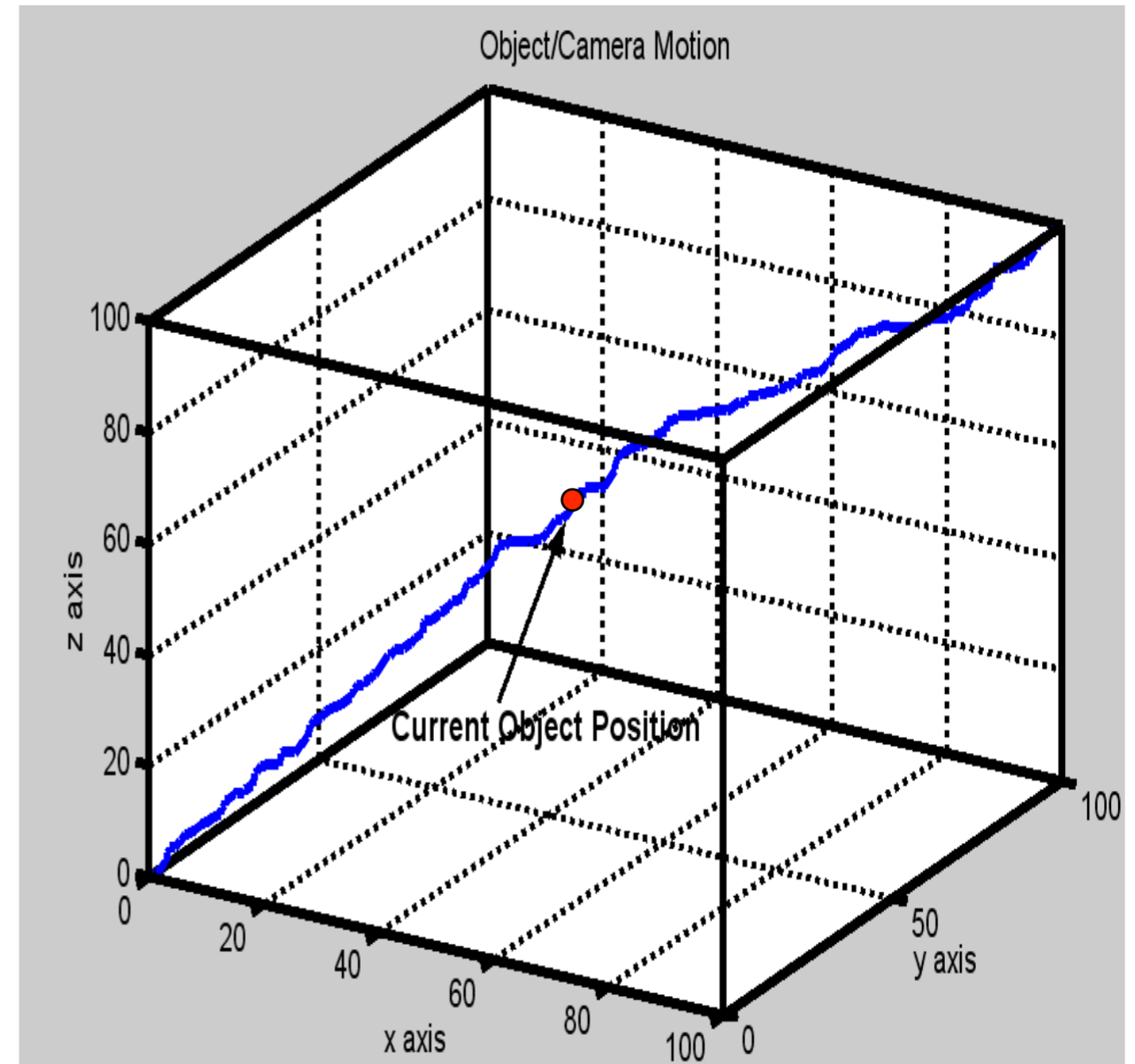


# Condensation



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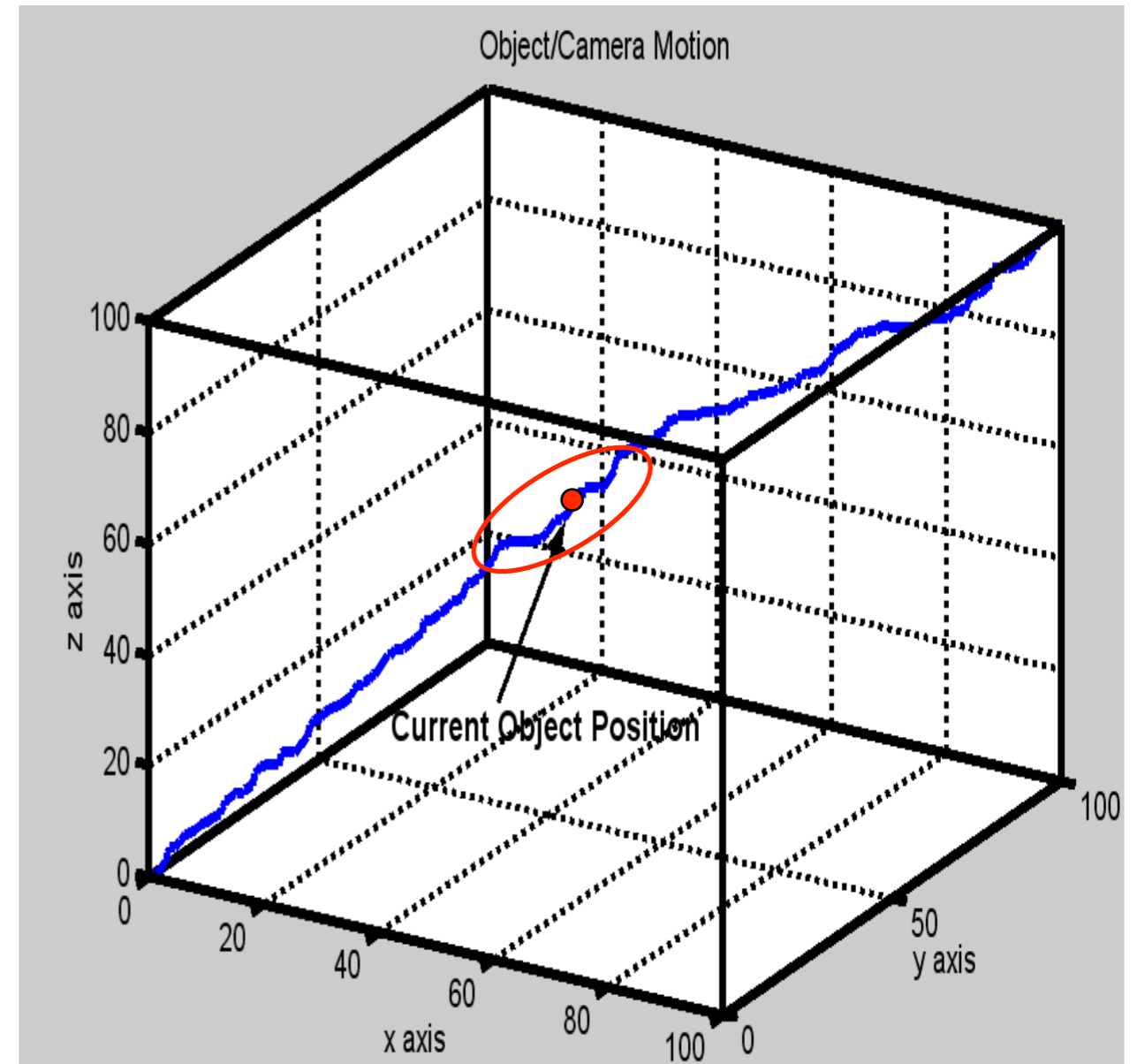
- Homography pose relationship.





# Condensation

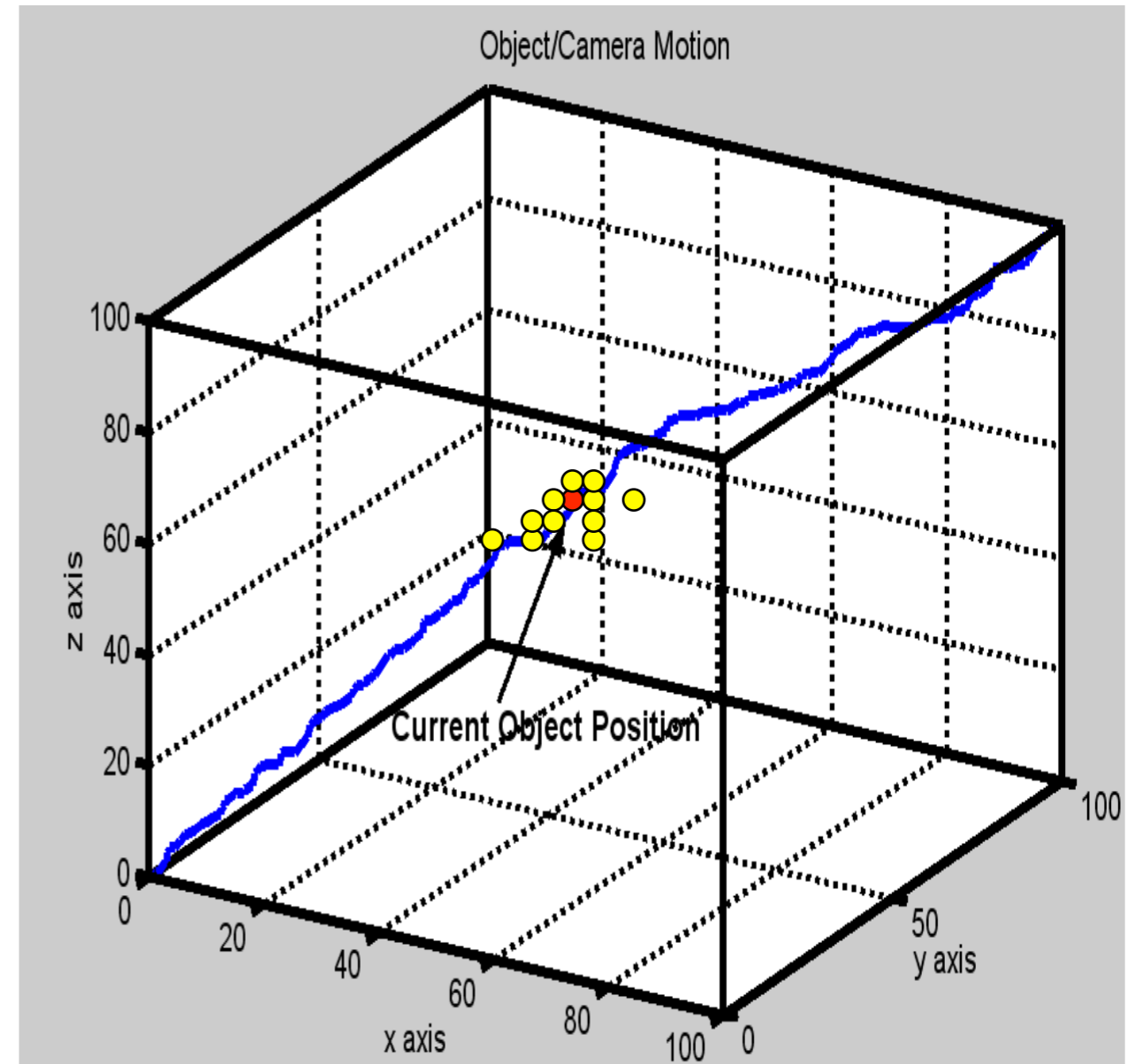
- Homography pose relationship.
- Prior condenses search space.





# Condensation

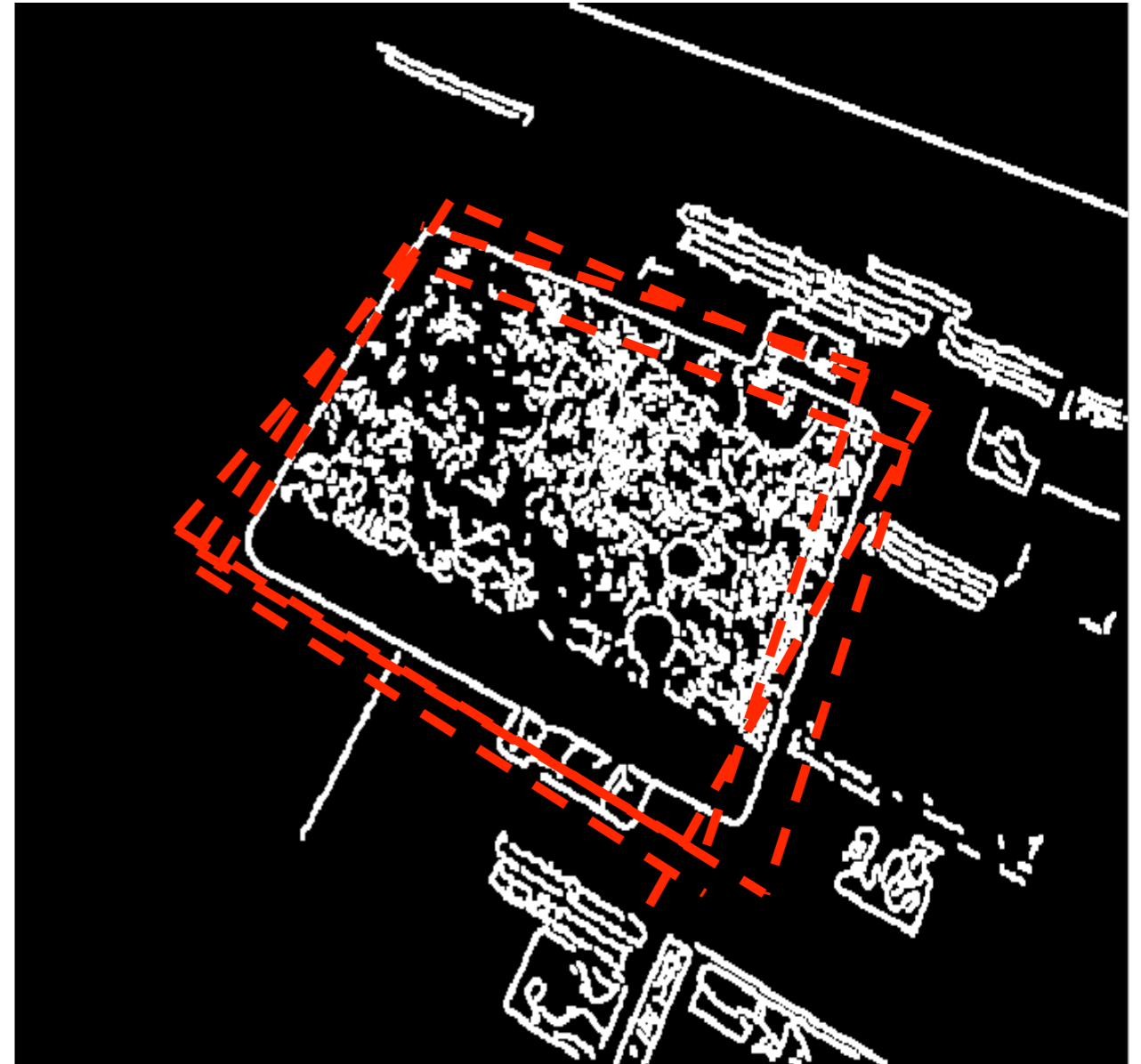
- Homography pose relationship.
- Prior condenses search space.
- Particles are drawn, and transform to homographies.





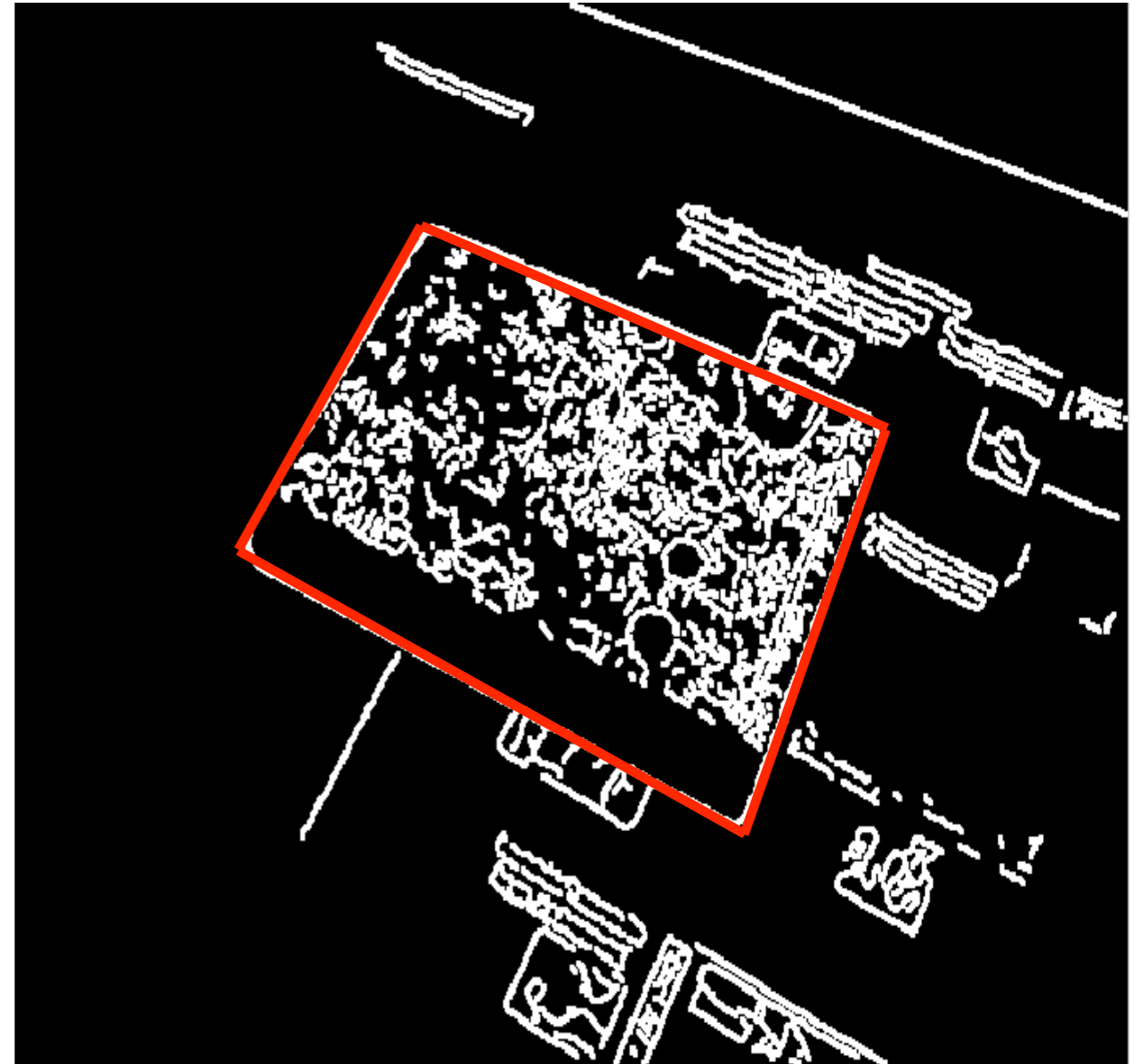
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- Homography pose relationship.
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- Weighted posterior combines advantages while suppressing drawbacks



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# Why Particle Filters



# Why Particle Filters

- Any tracking algorithm must consider non-linearity of the process dynamics and non-Gaussian nature of noise.



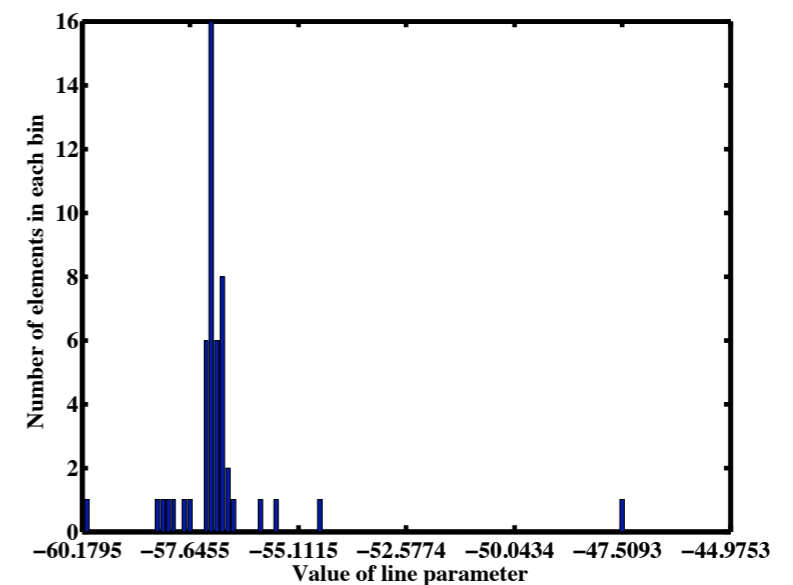
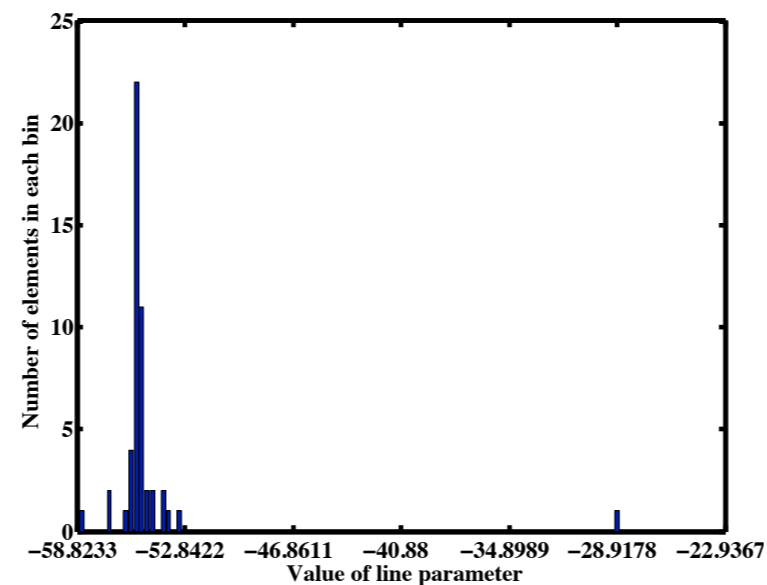
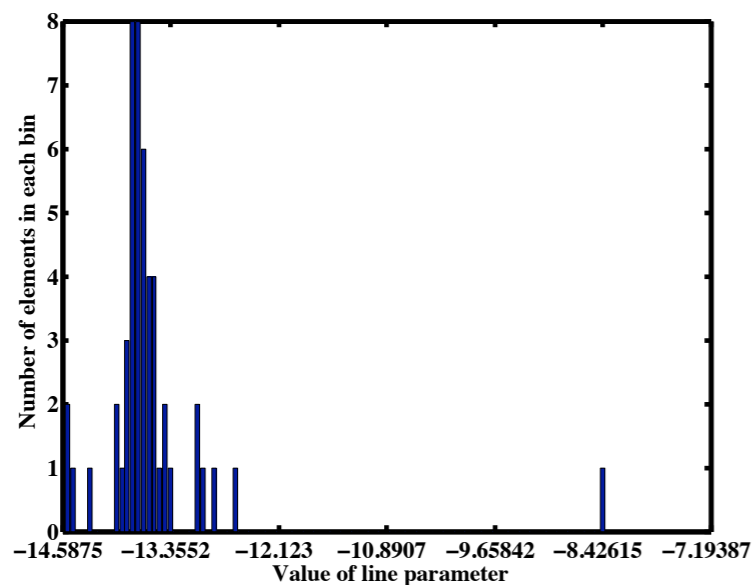
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- Any tracking algorithm must consider non-linearity of the process dynamics and non-Gaussian nature of noise.
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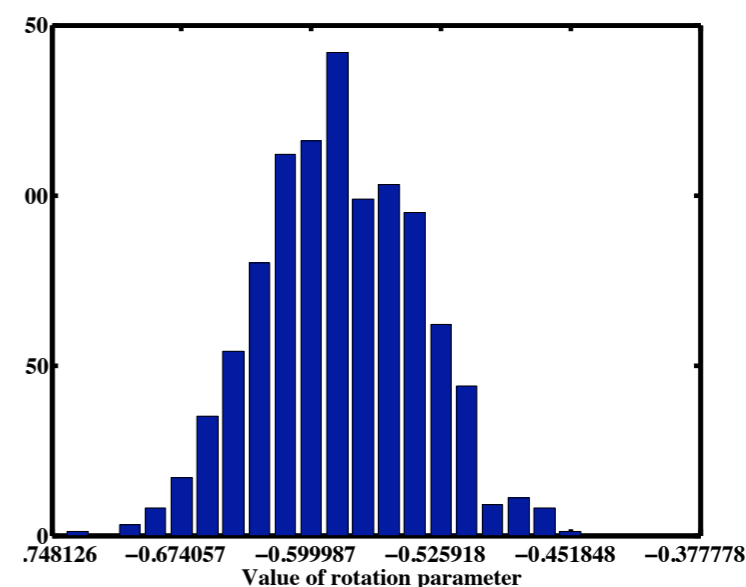
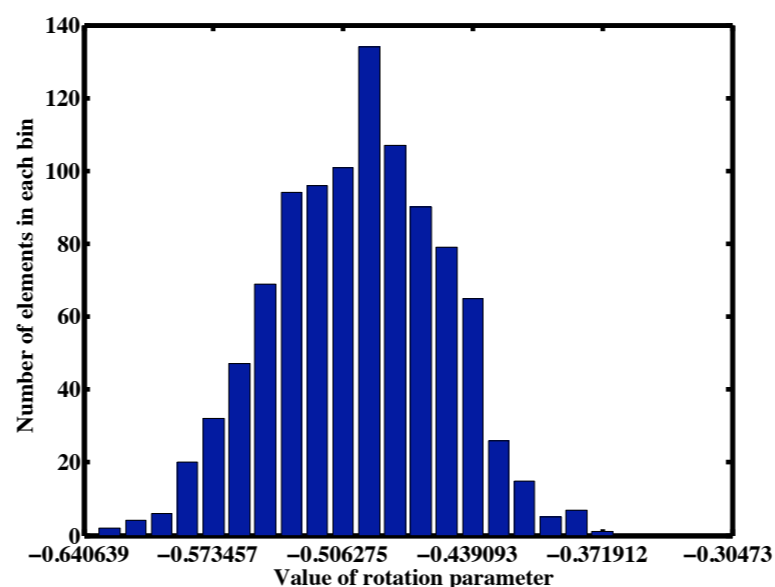
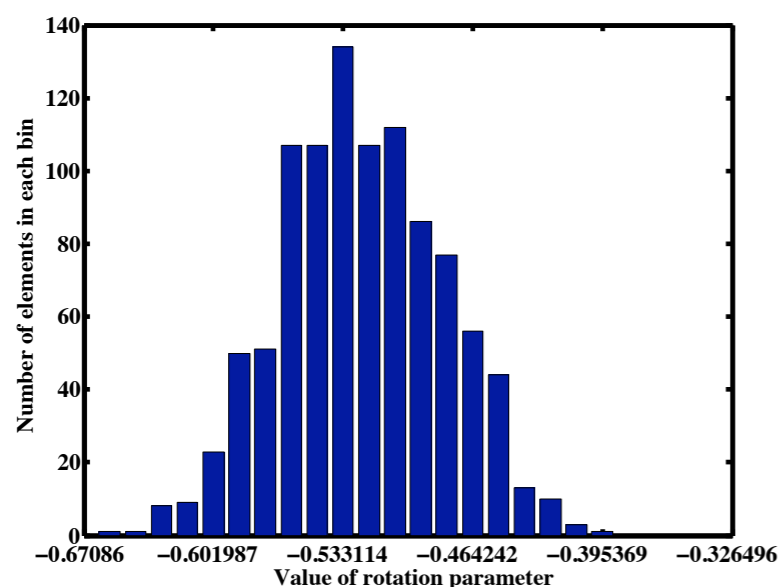
- Any tracking algorithm must consider non-linearity of the process dynamics and non-Gaussian nature of noise.
- In this case, non-linearity is introduced in line/contour measurements.
- Homography space highly non-linear when considering line transfer.





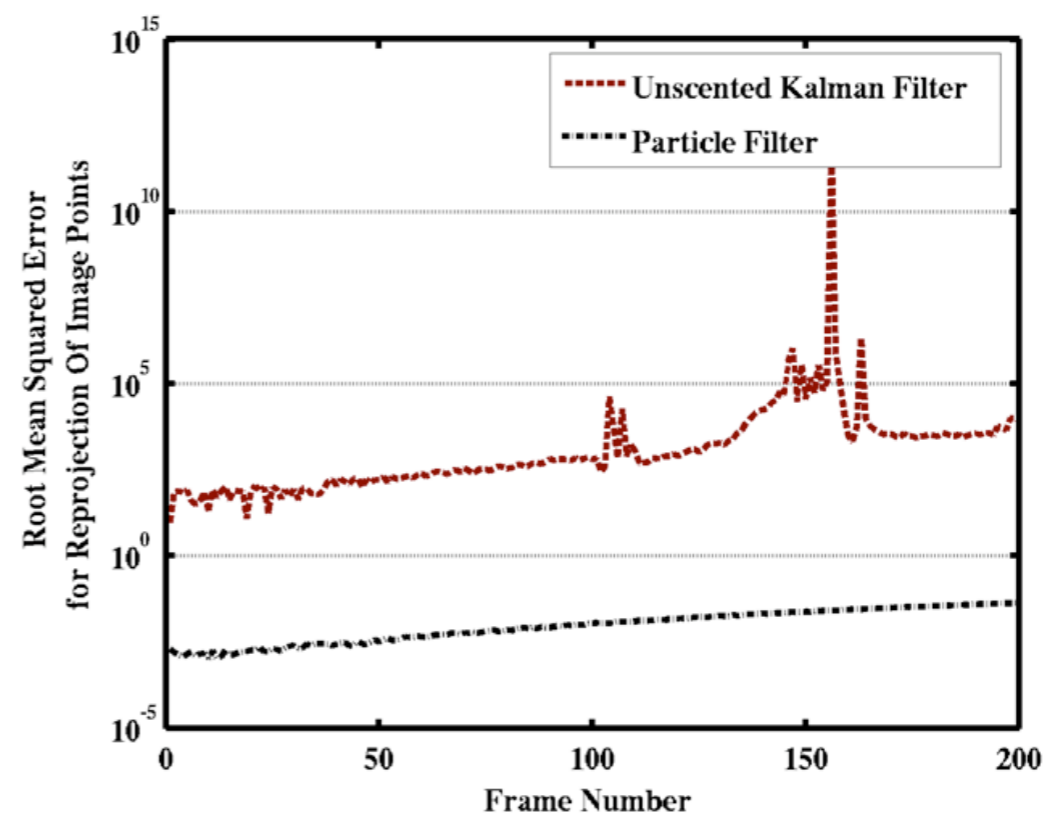
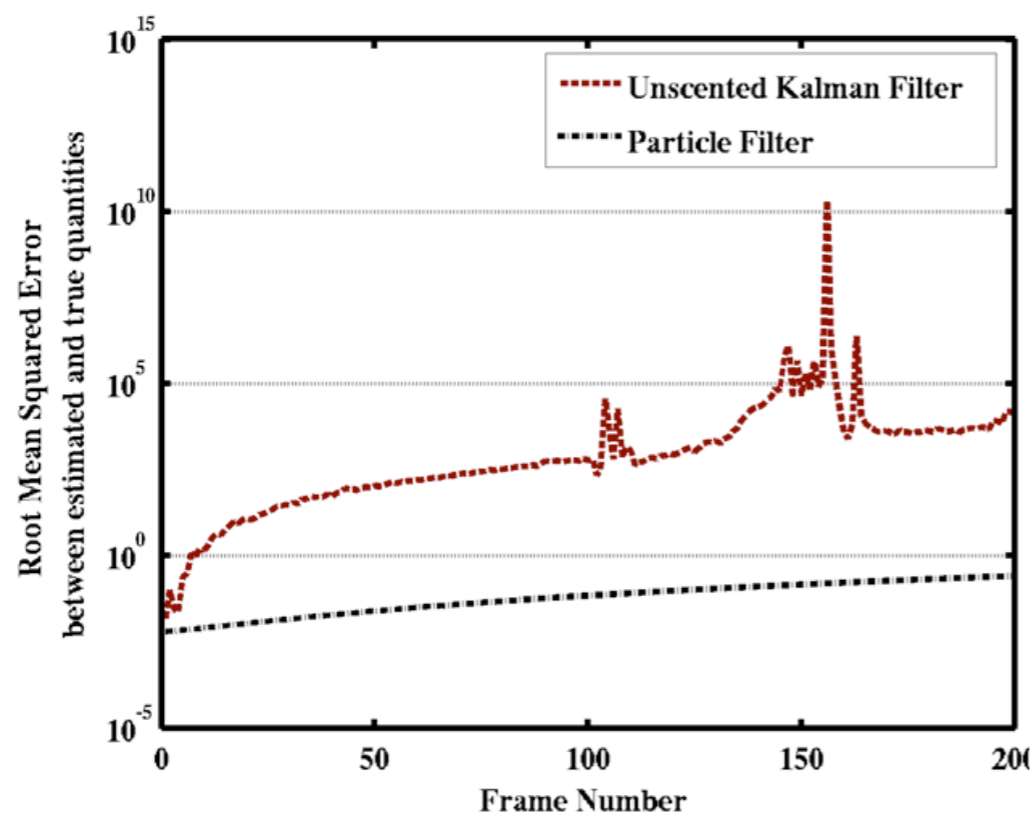
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# Why Particle Filters

- Comparison of particle vs unscented kalman filter.
- Case evaluated for estimating homography, while considering contour/line measurements.

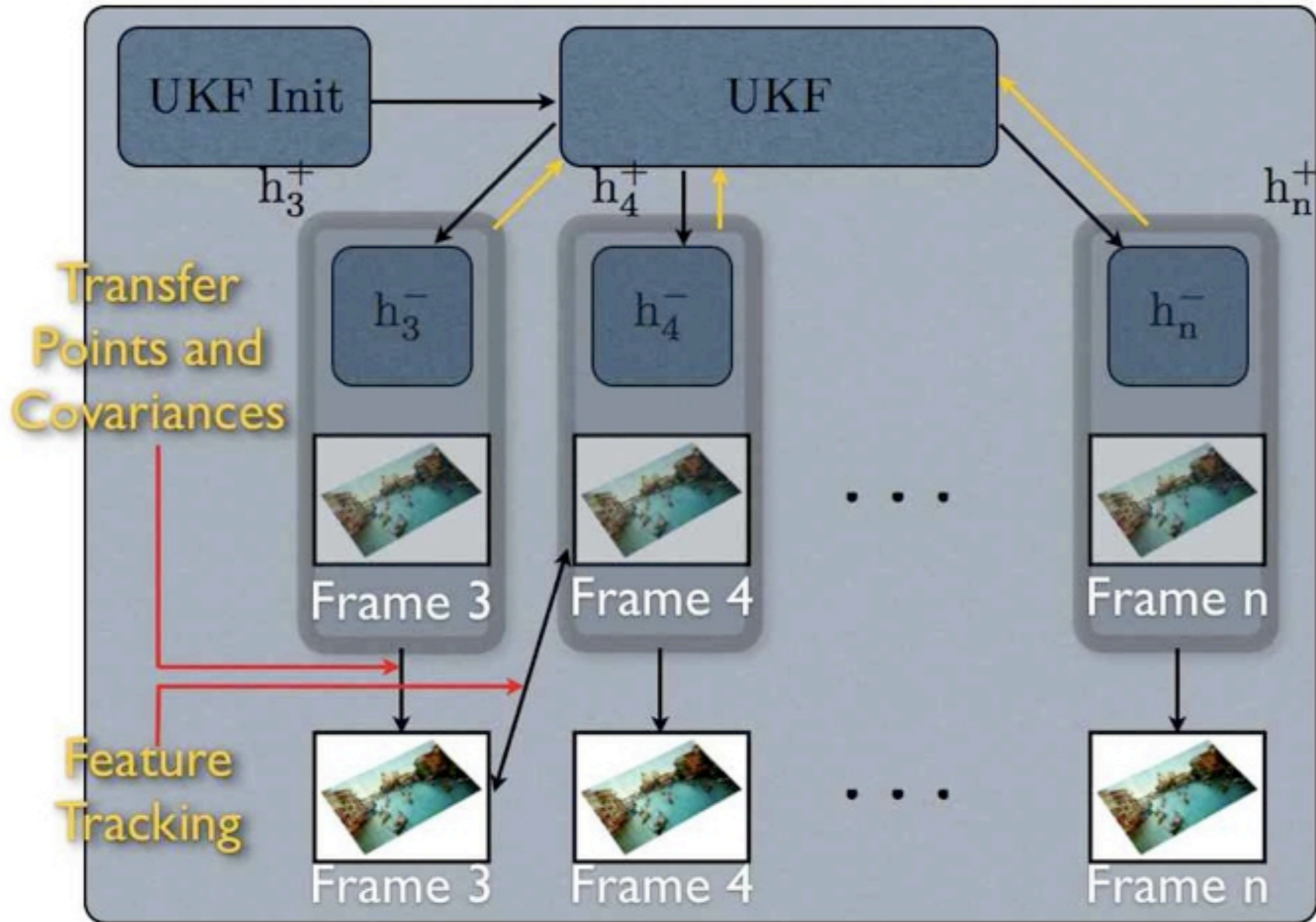




# Conclusions

- Particle Filter Framework for integrating edge and texture cues for planar tracking.
- The tracker is robust to large change of perspective and illumination.
- Analysis and Justification for choosing particle filter for tracking purposes.
- Comparison with Unscented Kalman Filter with edge cues for homography computation.

# Approach



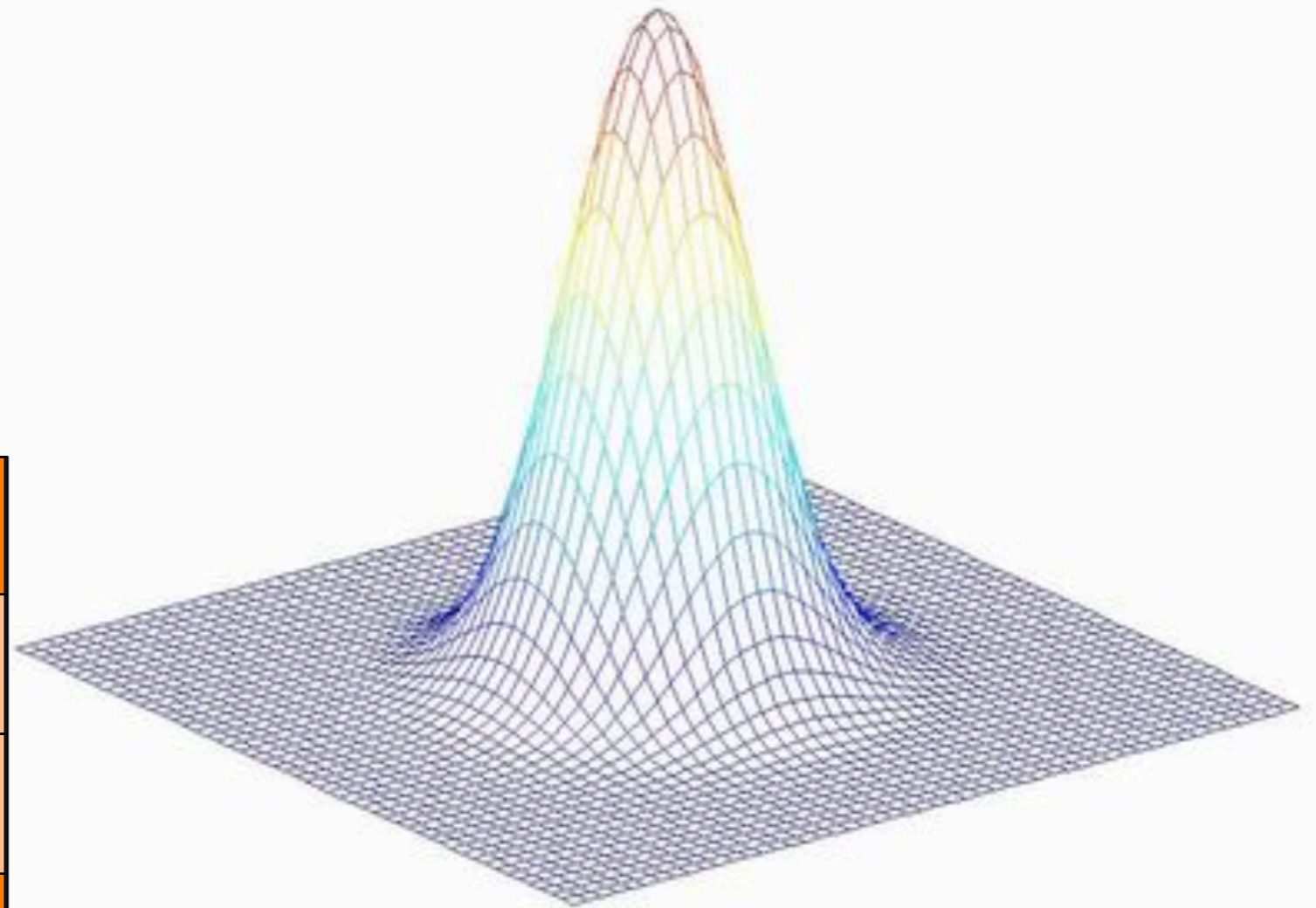
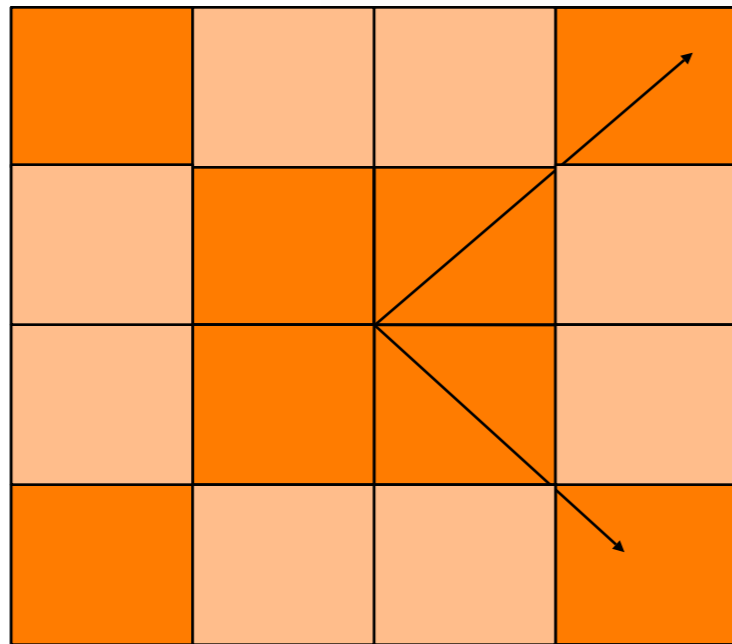


# Modeling Uncertainty



# Modeling Uncertainty

- Uncertainty Representation.



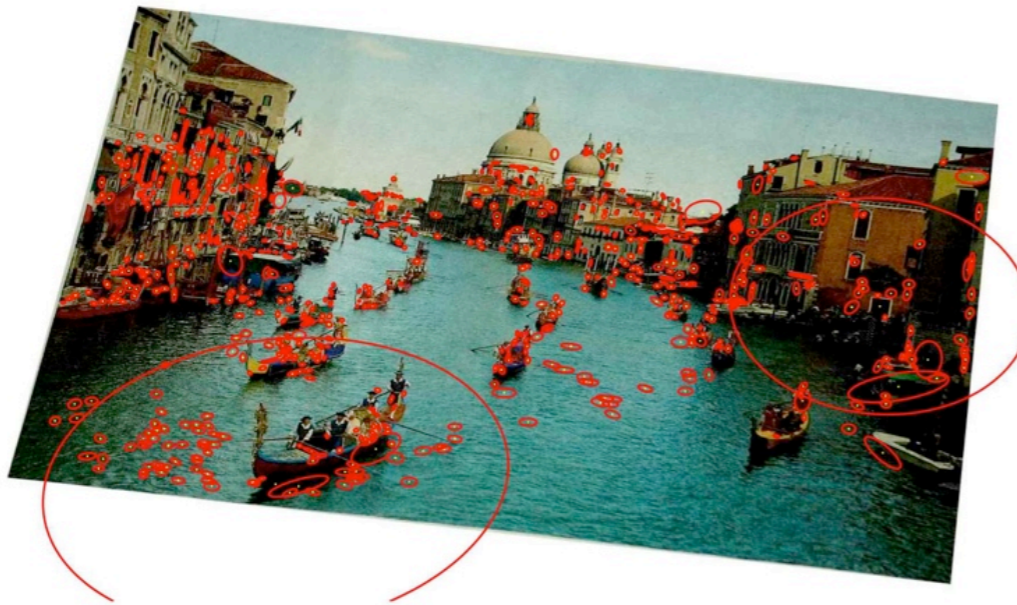


# Modeling Uncertainty

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- Uncertainty Representation.
- Uncertainty Propagation.





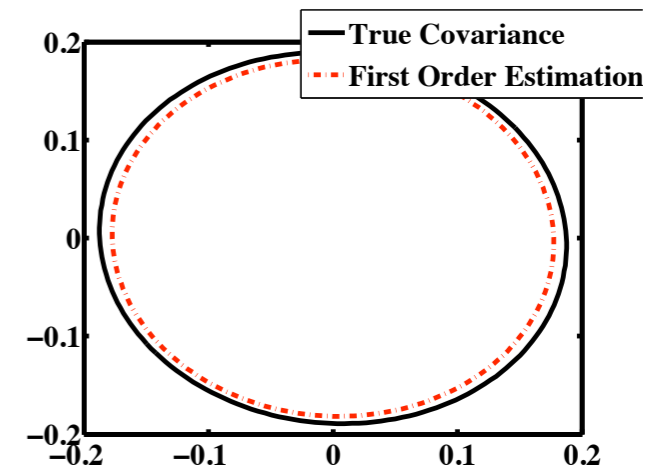
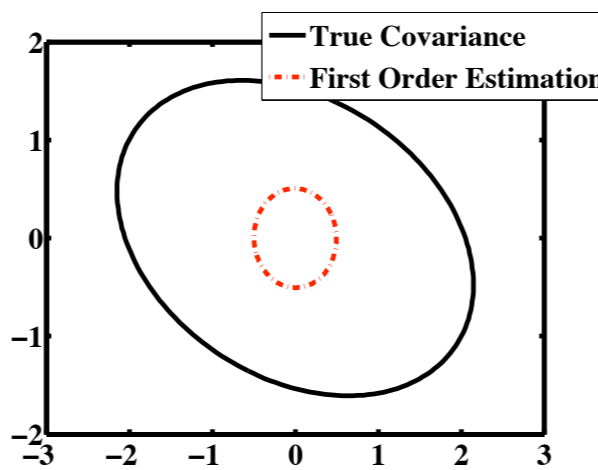
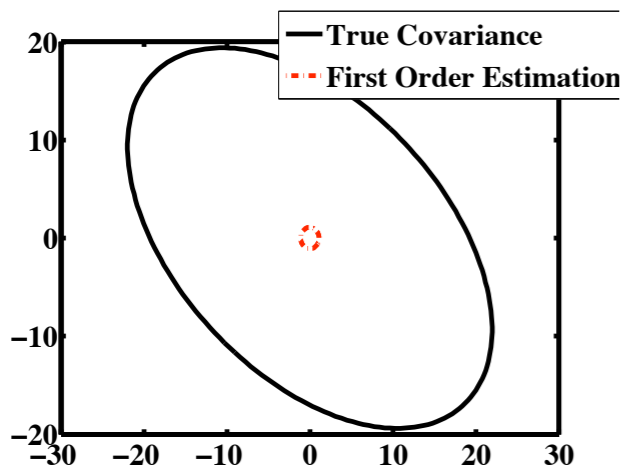
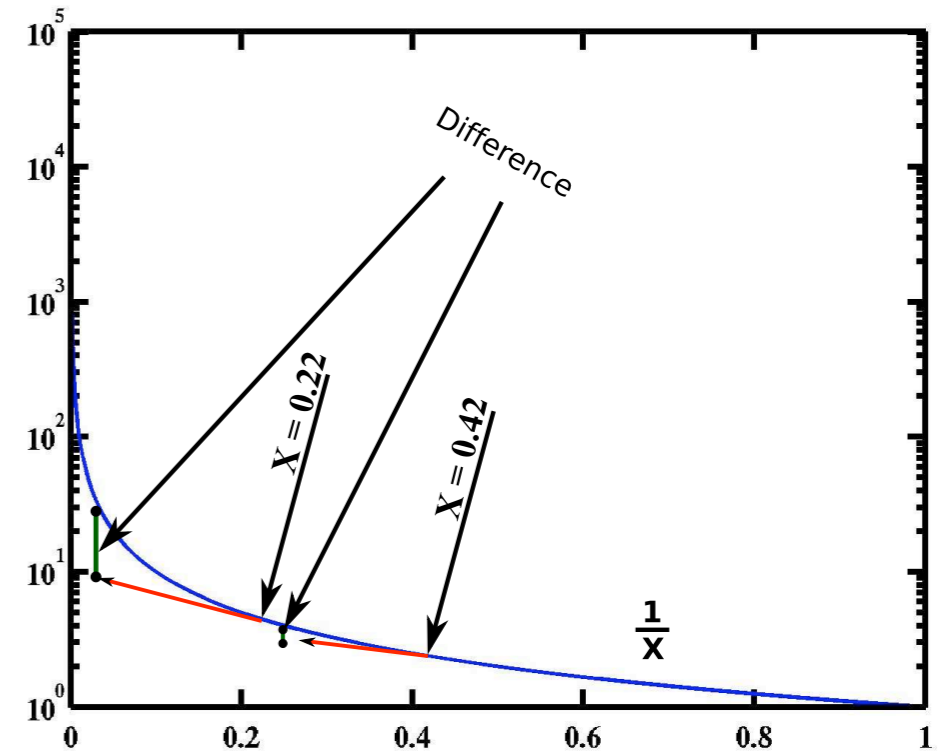
# Modeling Uncertainty

- Uncertainty Representation.
- Uncertainty Propagation.



# Modeling Uncertainty

- Uncertainty Representation.
- Uncertainty Propagation.
- Uncertainty Maintenance.



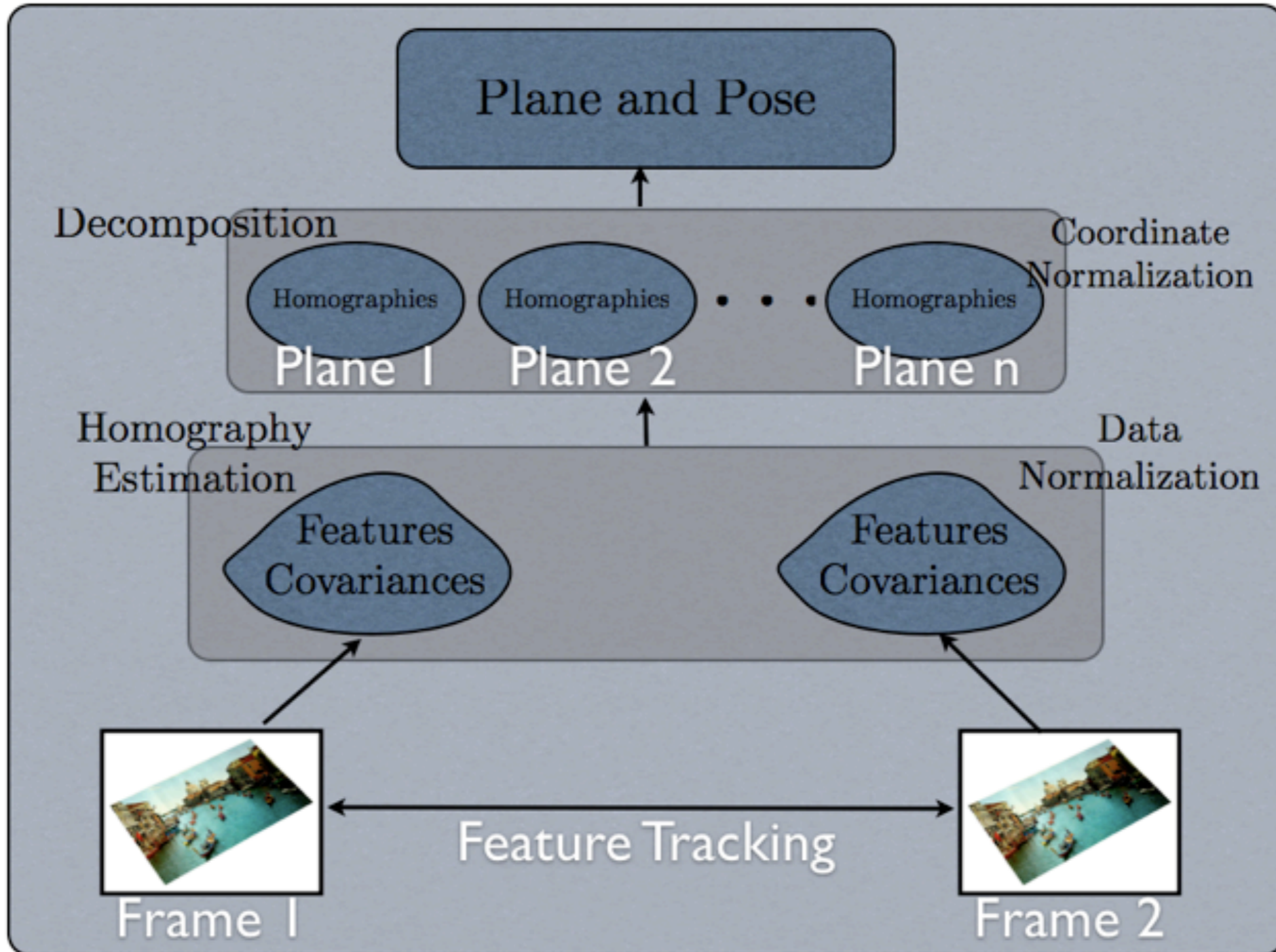


# Modeling Uncertainty

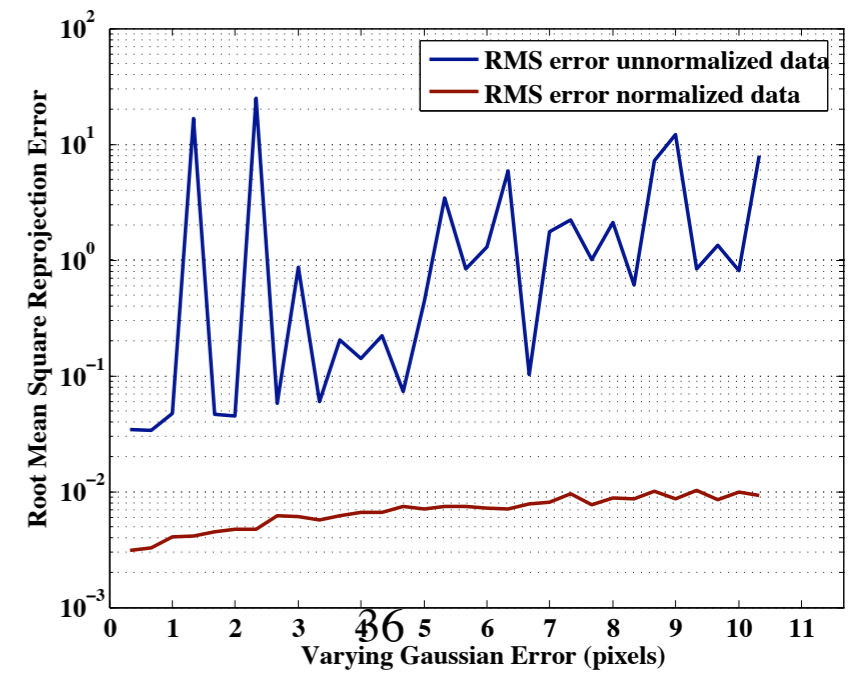
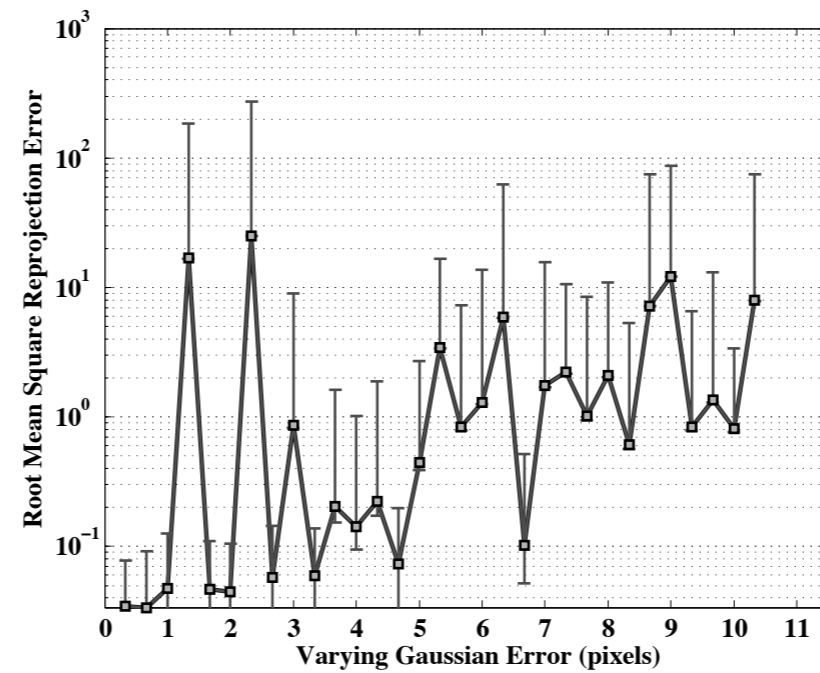
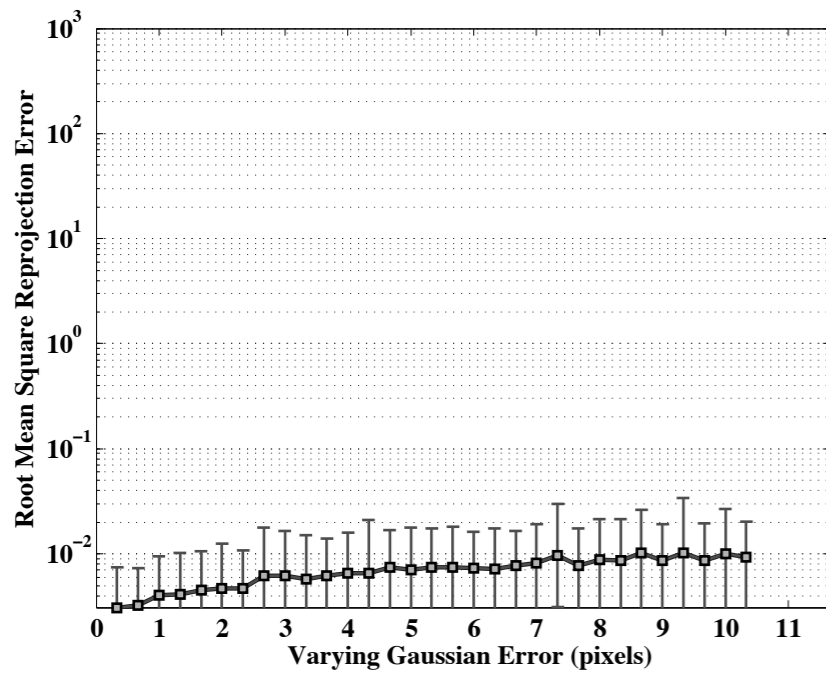
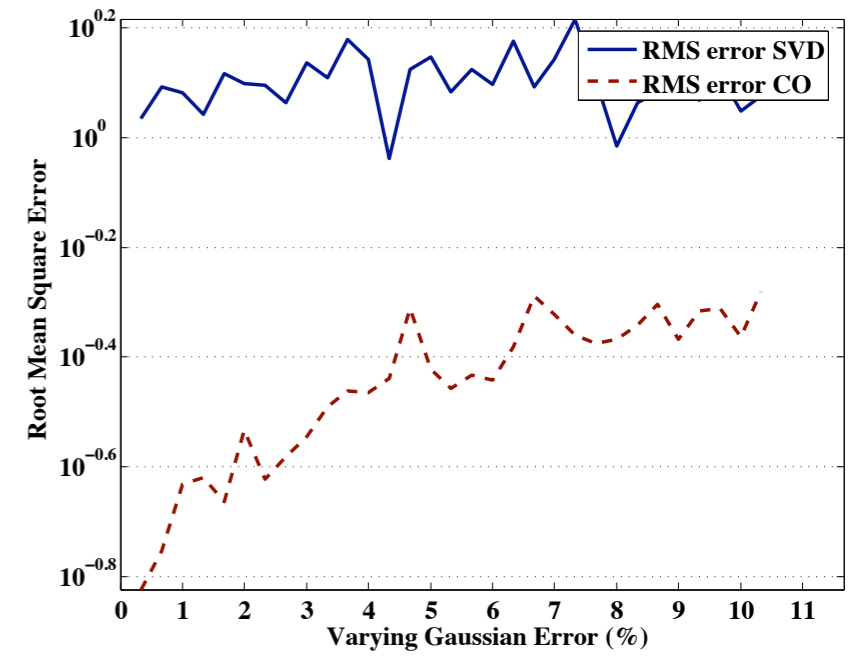
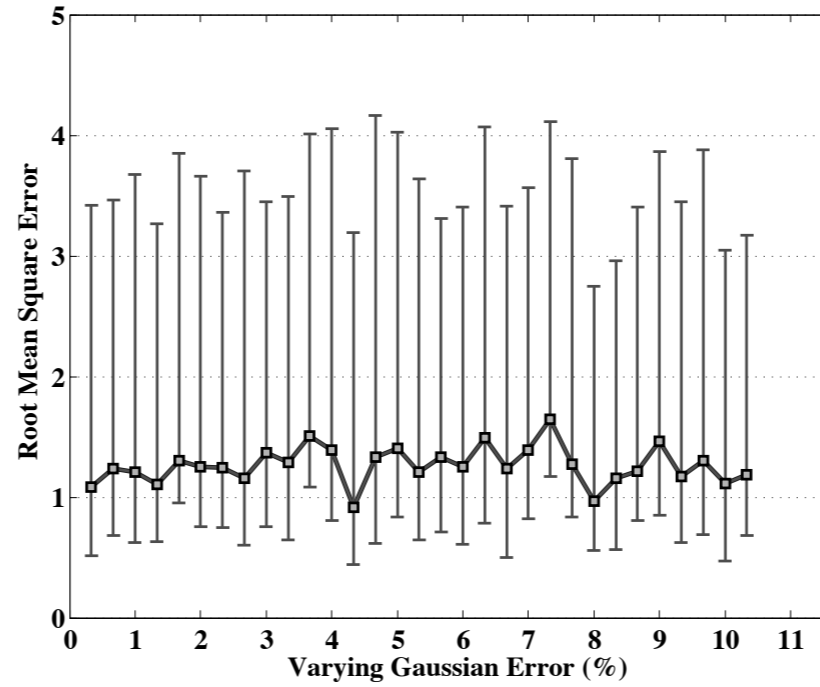
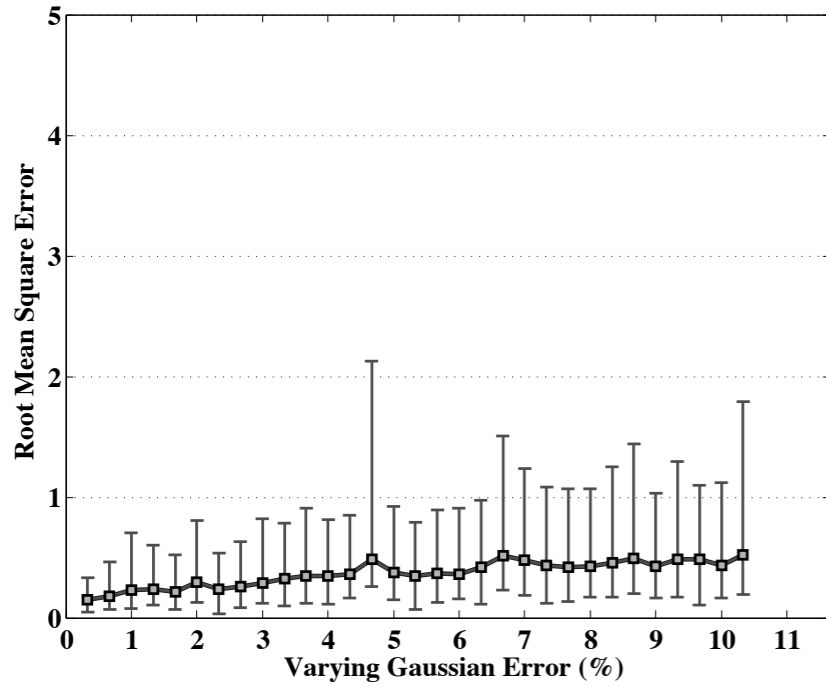
- Uncertainty Representation.
- Uncertainty Propagation.
- Uncertainty Maintenance.



# Initialization

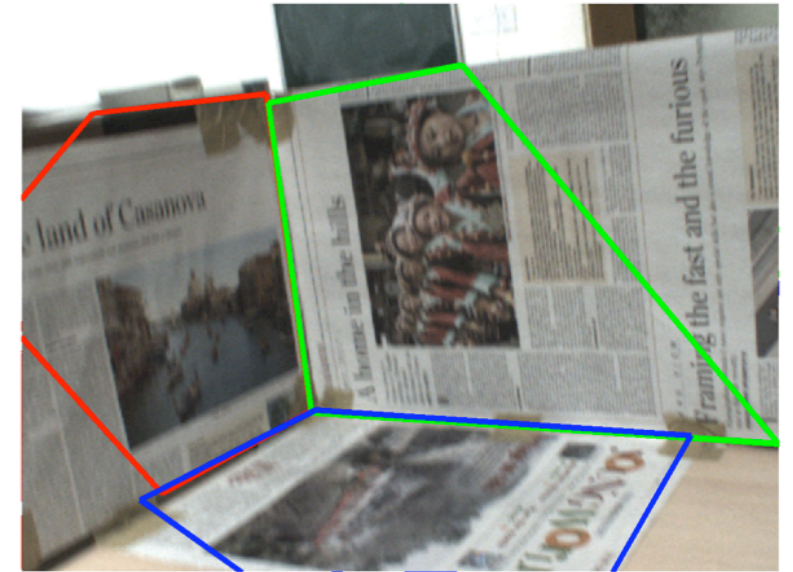
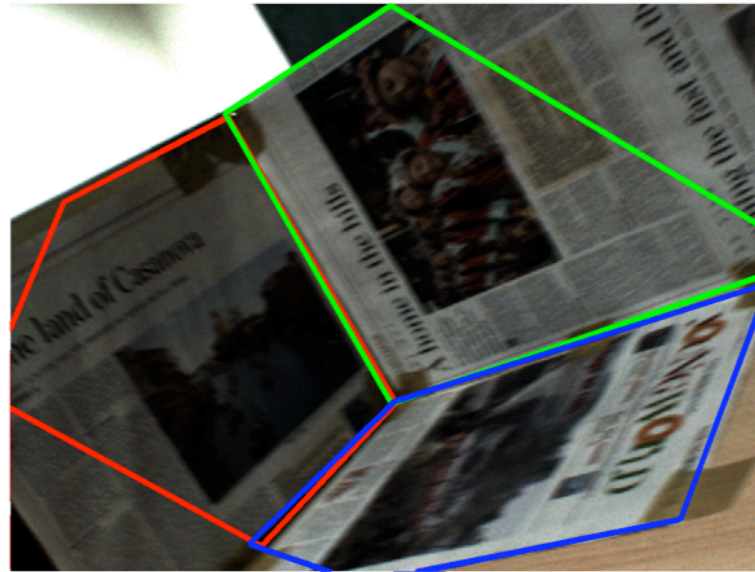


# Results

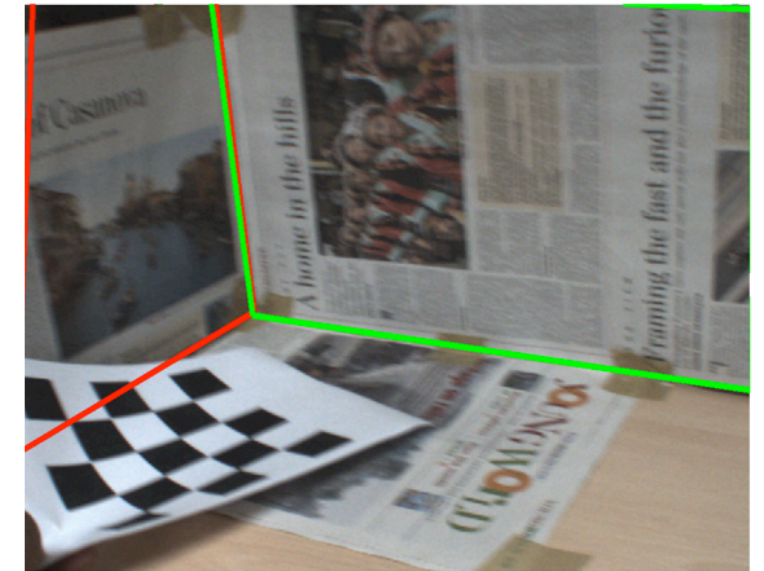
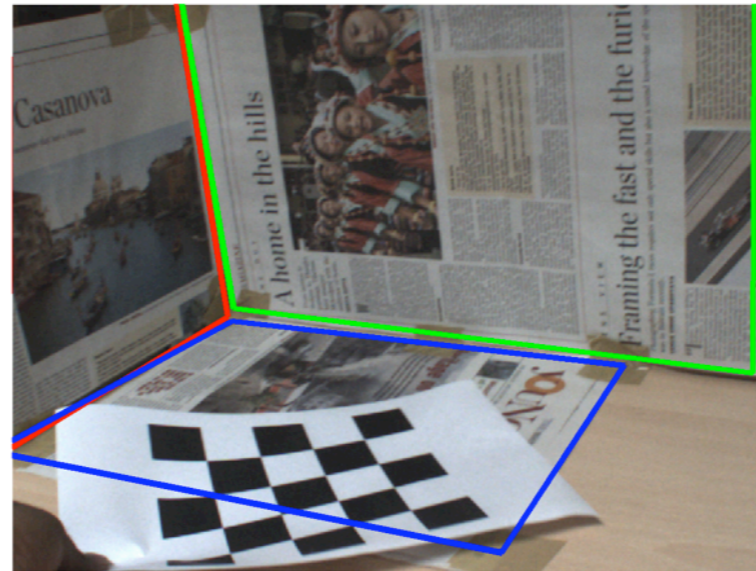
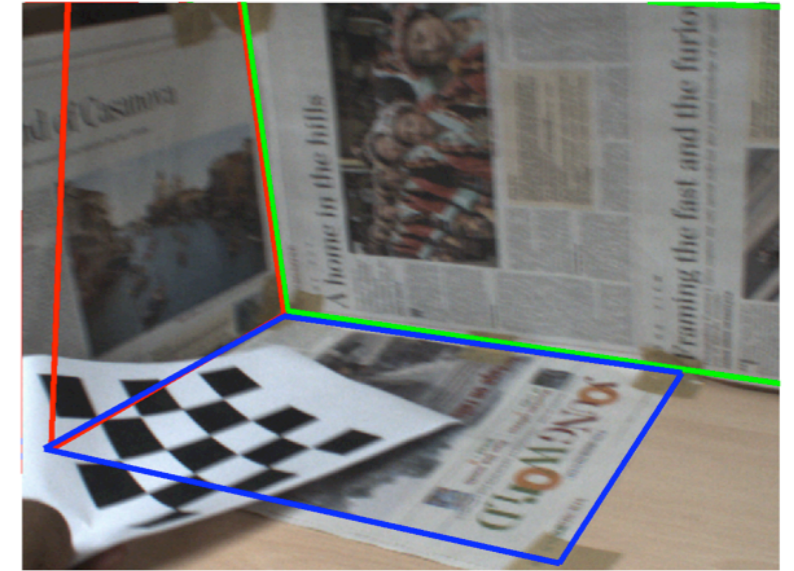
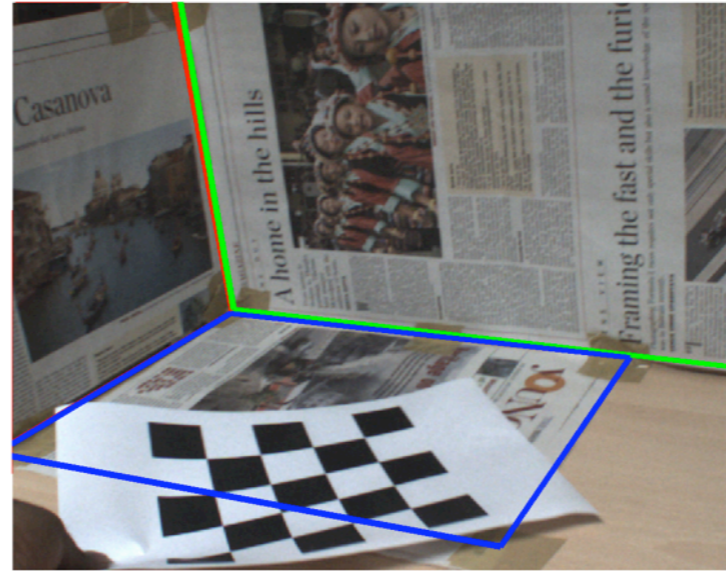




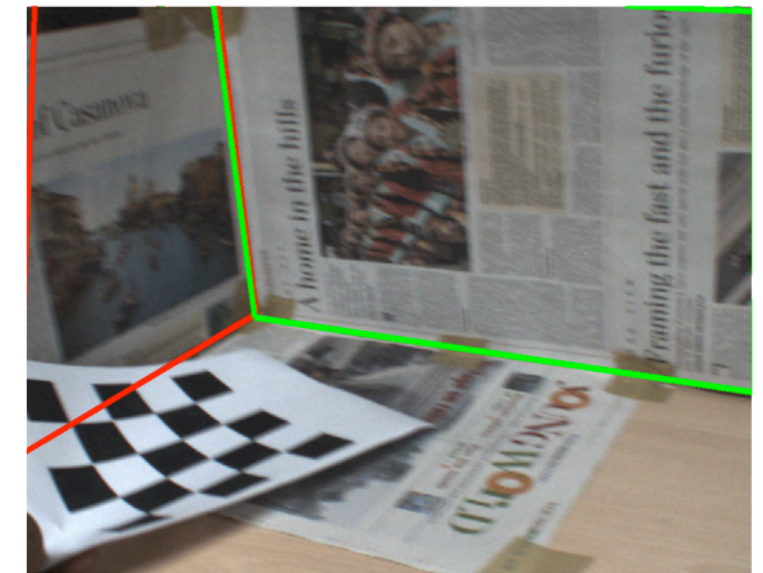
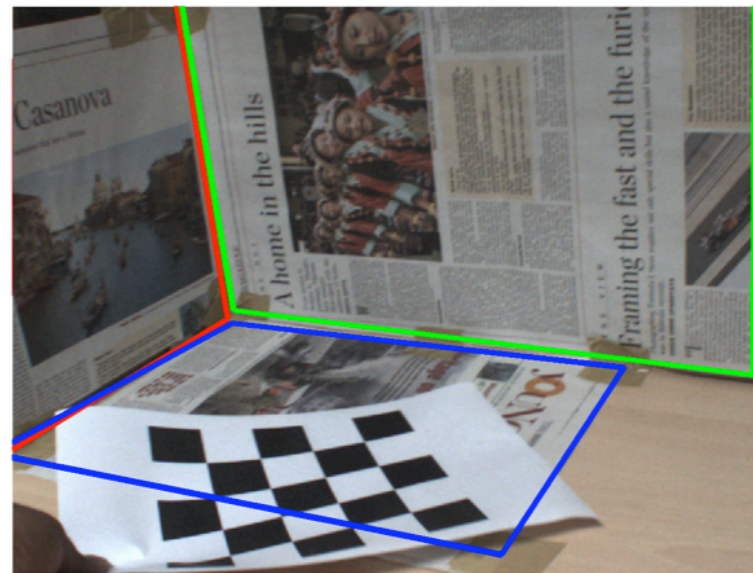
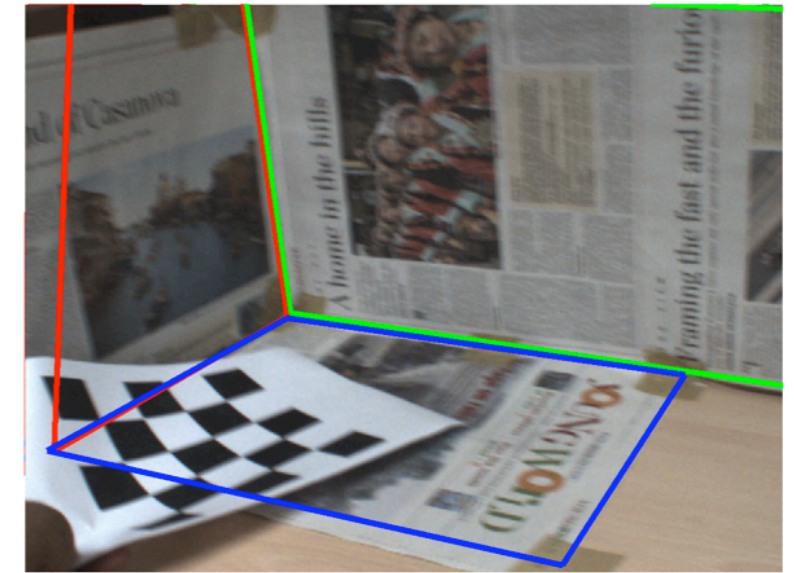
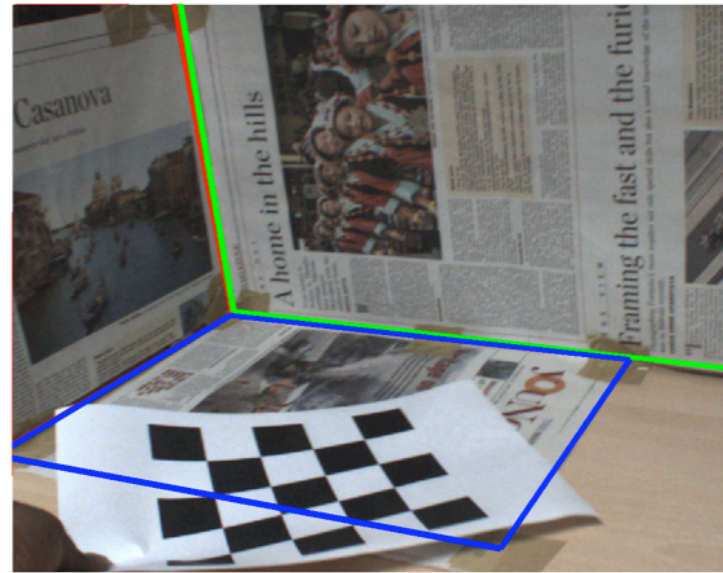
# Results



# Results



# Results



Visesh Chari, C. V. Jawahar. Multiple Plane Tracking using the Unscented Kalman Filter.  
IEEE International Conference on Robotics and Automation (ICRA'09) (Submitted).

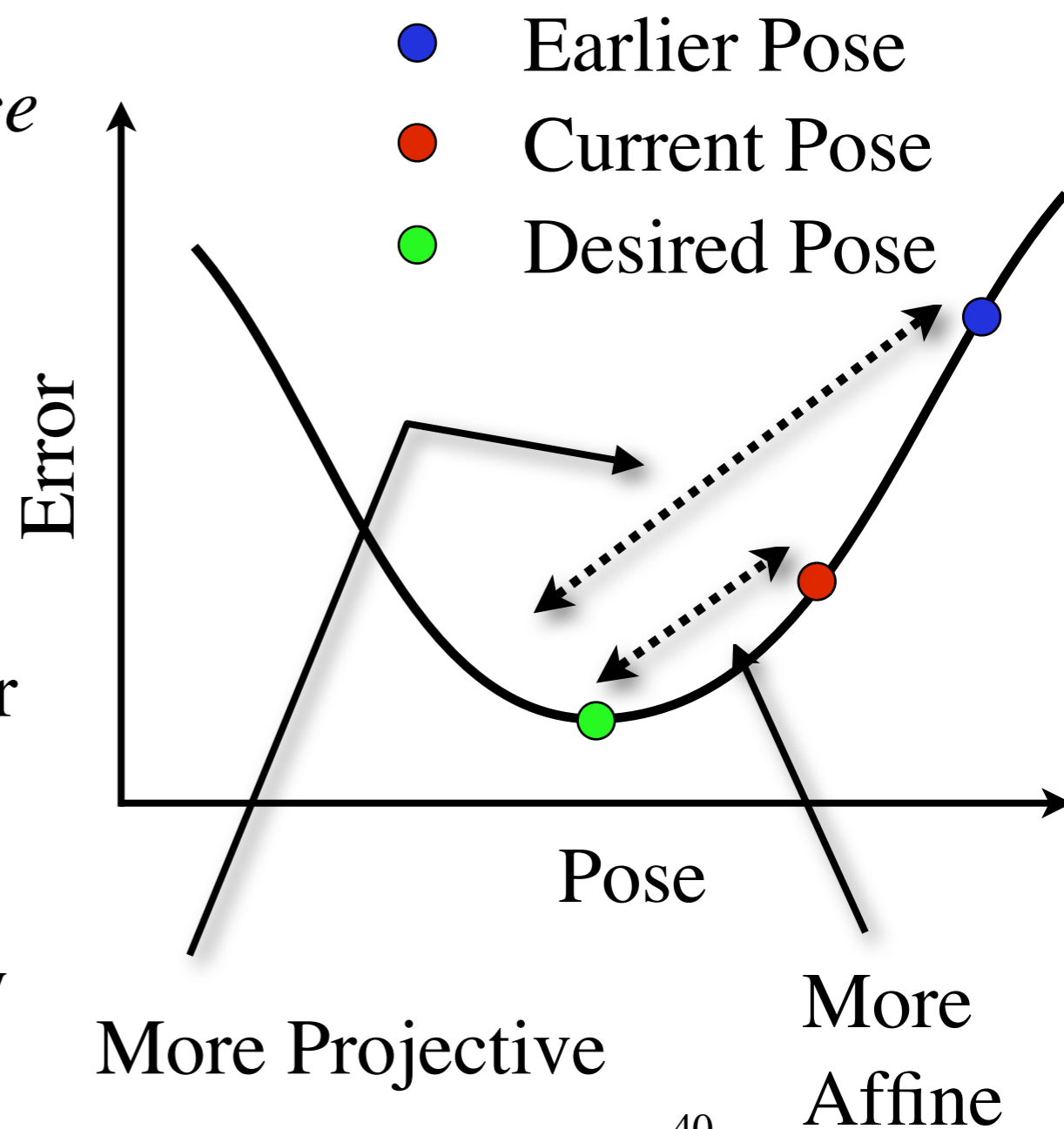
# Conclusions

- A multiple plane tracking algorithm that utilizes the “commonality of pose” for stabilization is proposed.
- The tracker is shown to be consistent across illumination change and occlusion.
- A globally optimal algorithm for initialization of the tracker is also proposed.
- Comparison with the standard KLT tracker is shown.



# Correspondence-less Servoing

- Fourier based methods estimate homography in *absence* of correspondence for affine cases.
- Homography may then be used to obtain correspondence estimate.
- This estimate can be used for servoing.
- Affine estimates are initially inaccurate but get progressively better as current and desired views converge.



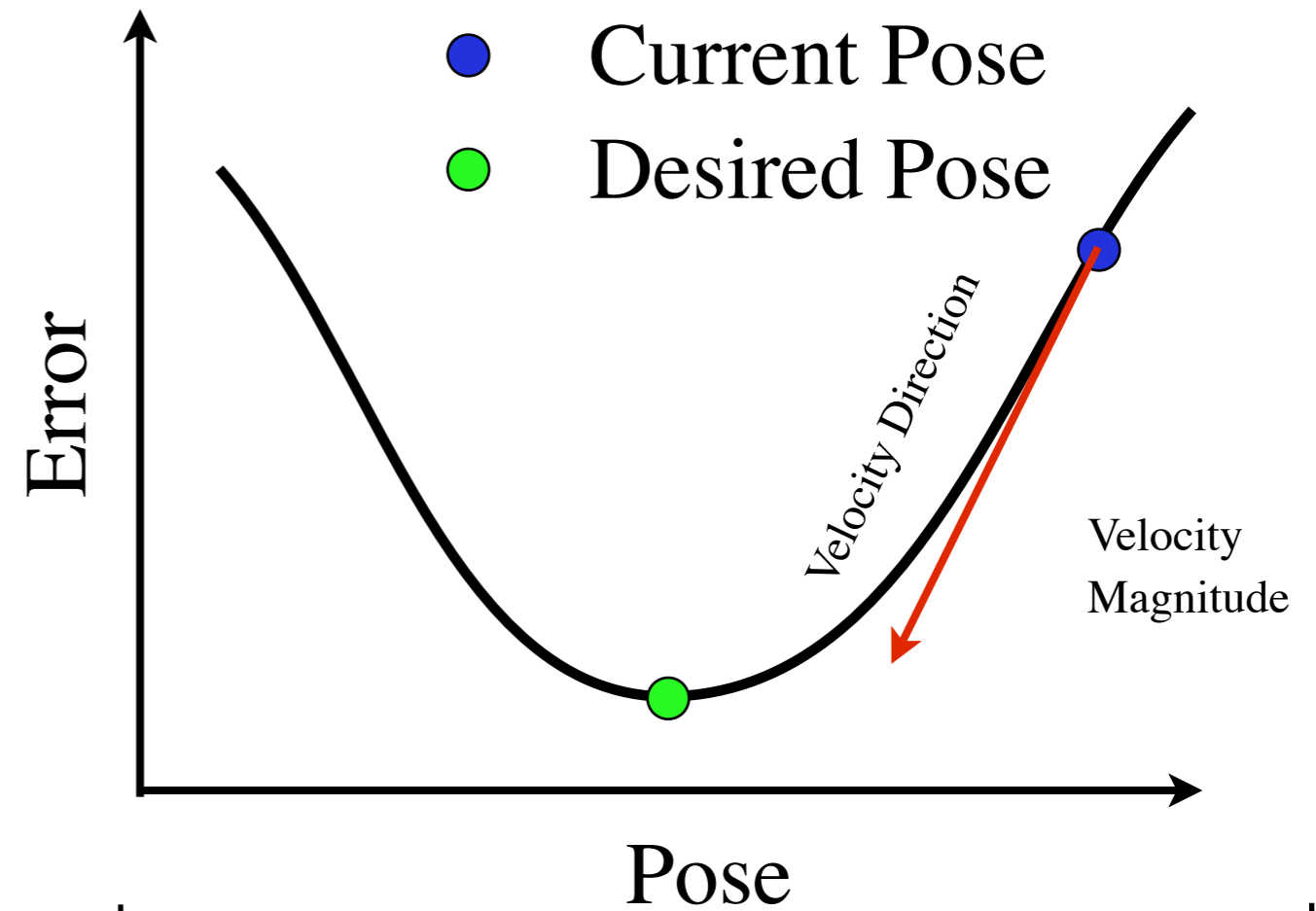


# Straight Cartesian Path Servoing



# Straight Cartesian Path Servoing

- Traditional IBVS.



IBVS Error = Difference in Image Coordinates.

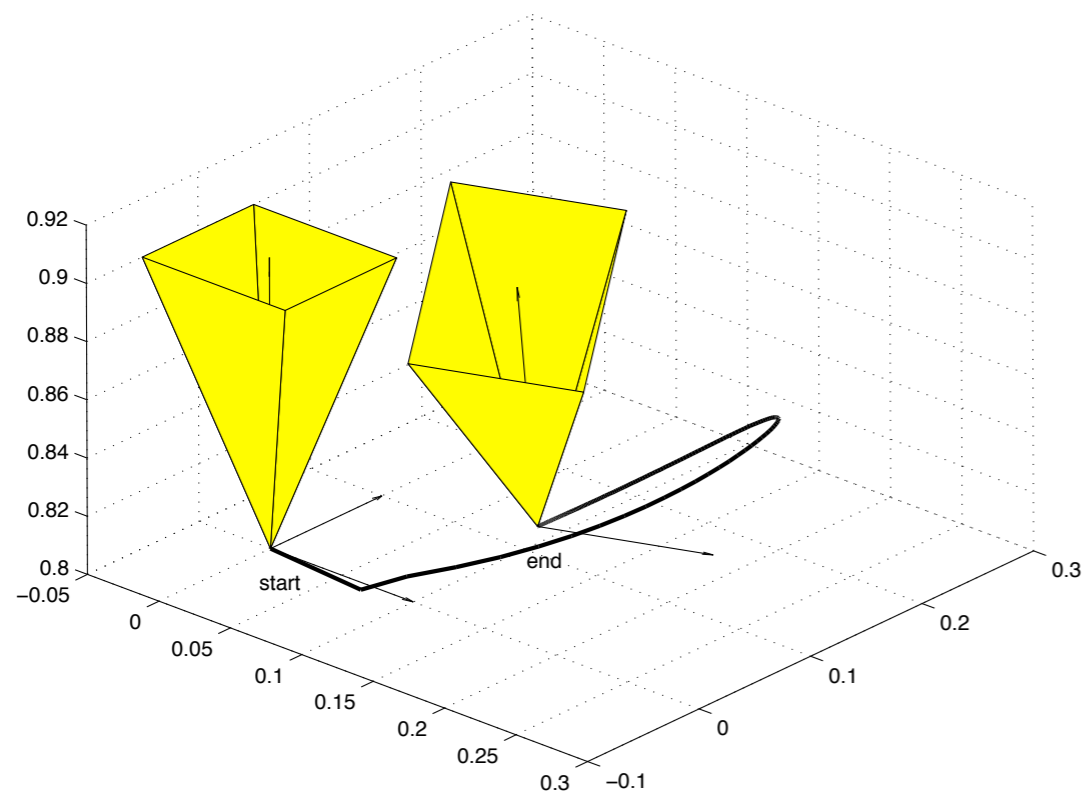


# Straight Cartesian Path Servoing

- Traditional IBVS.
- Cause of “non-straightness” - rotation along  $x, y$  axis.
- In contours, effect of rotation may be removed using Fourier applied to Taylor expansion.

# Straight Cartesian Path Servoing

- Traditional IBVS.
- Cause of “non-straightness” - rotation along x, y axis.



Straight Image Trajectory but non-straight Cartesian path.



# Straight Cartesian Path Servoing

- Traditional IBVS.
- Cause of “non-straightness” - rotation along  $x, y$  axis.
- In contours, effect of rotation may be removed using Fourier applied to Taylor expansion.



# Straight Cartesian Path Servoing

- Traditional IBVS.
- Cause of “non-straightness” - rotation along x, y axis.
- In contours, effect of rotation may be removed using Fourier applied to Taylor expansion.

Take Fourier of image points of current and desired pose.

In 5 DOF servoing, rotation may be linearized around identity matrix (first order approximation).

Coefficients of  $r_x$  (or  $r_y$ ) can consequently be computed using least squares method, by aggregating evidence from all image points.



# Straight Cartesian Path Servoing

- Traditional IBVS.
- Cause of “non-straightness” - rotation along  $x, y$  axis.
- In contours, effect of rotation may be removed using Fourier applied to Taylor expansion.



# Path Following



# Path Following

- Camera trajectory in VS fixed.

Given initial and desired positions, the camera trajectory in visual servoing is determined by the minimization approach.



# Path Following

- Camera trajectory in VS fixed.
- Disadvantage because of inability to plan path.

Thus avoiding obstacles, or in general the task of following a user specified trajectory is not possible.



# Path Following

- Camera trajectory in VS fixed.
- Disadvantage because of inability to plan path.
- Fourier based approach captures global properties of contours.

Since each Fourier component captures details from the entire contour, each component represents a global quantity.



# Path Following

- Camera trajectory in VS fixed.
- Disadvantage because of inability to plan path.
- Fourier based approach captures global properties of contours.
- Weighted Fourier error may be used for path following.

Thus weighting fourier components can change the global character of error space.

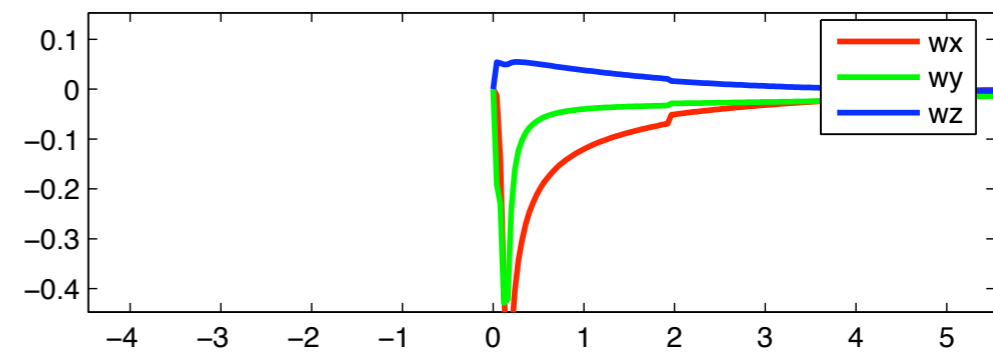
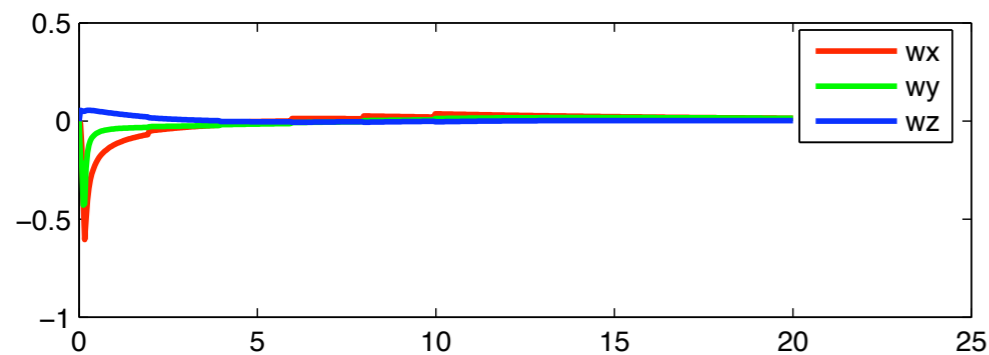
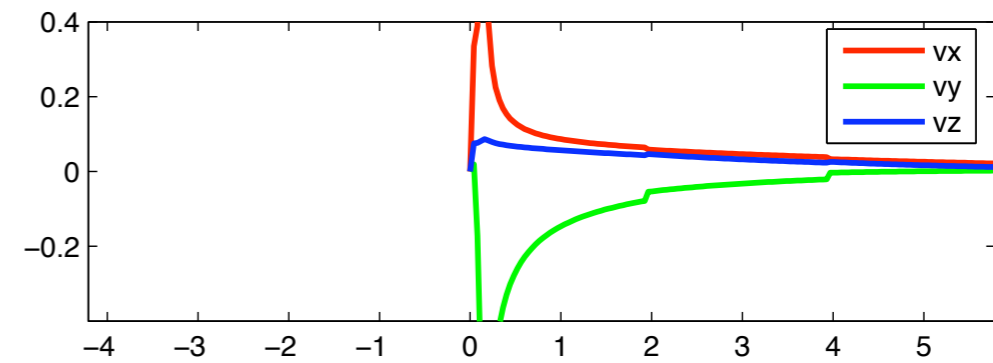
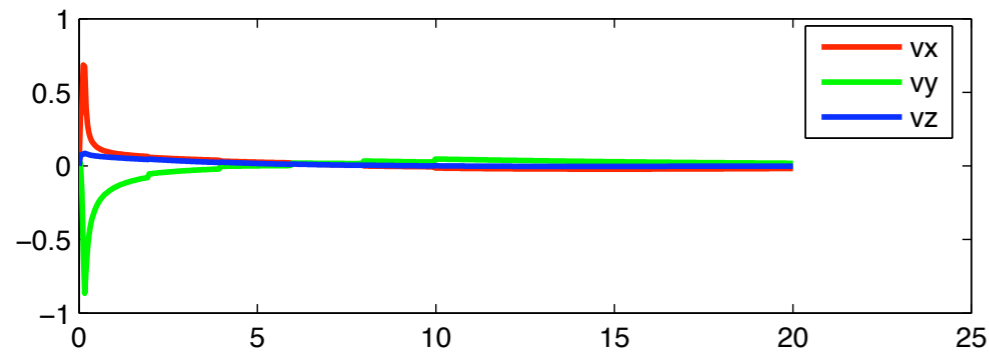
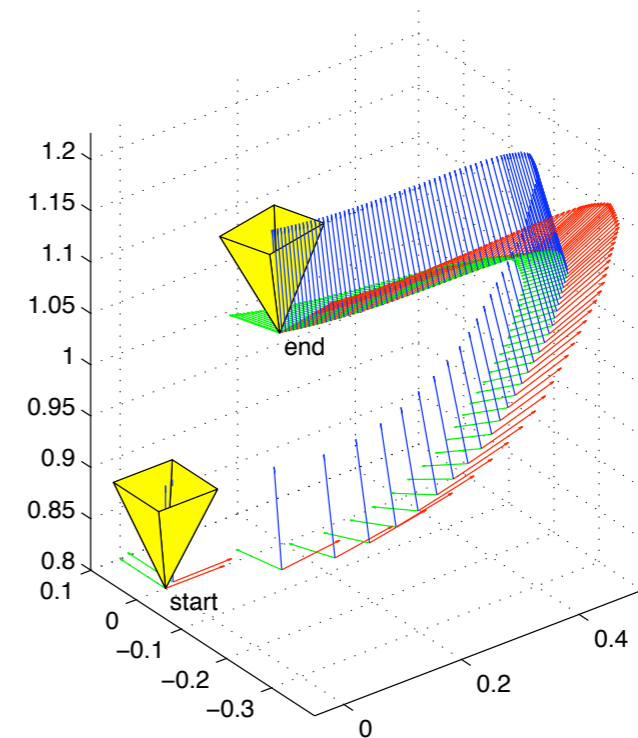
Here the path to be followed can be the output of a path planning algorithm.



# Results

# Results

- Correspondence-less servoing.





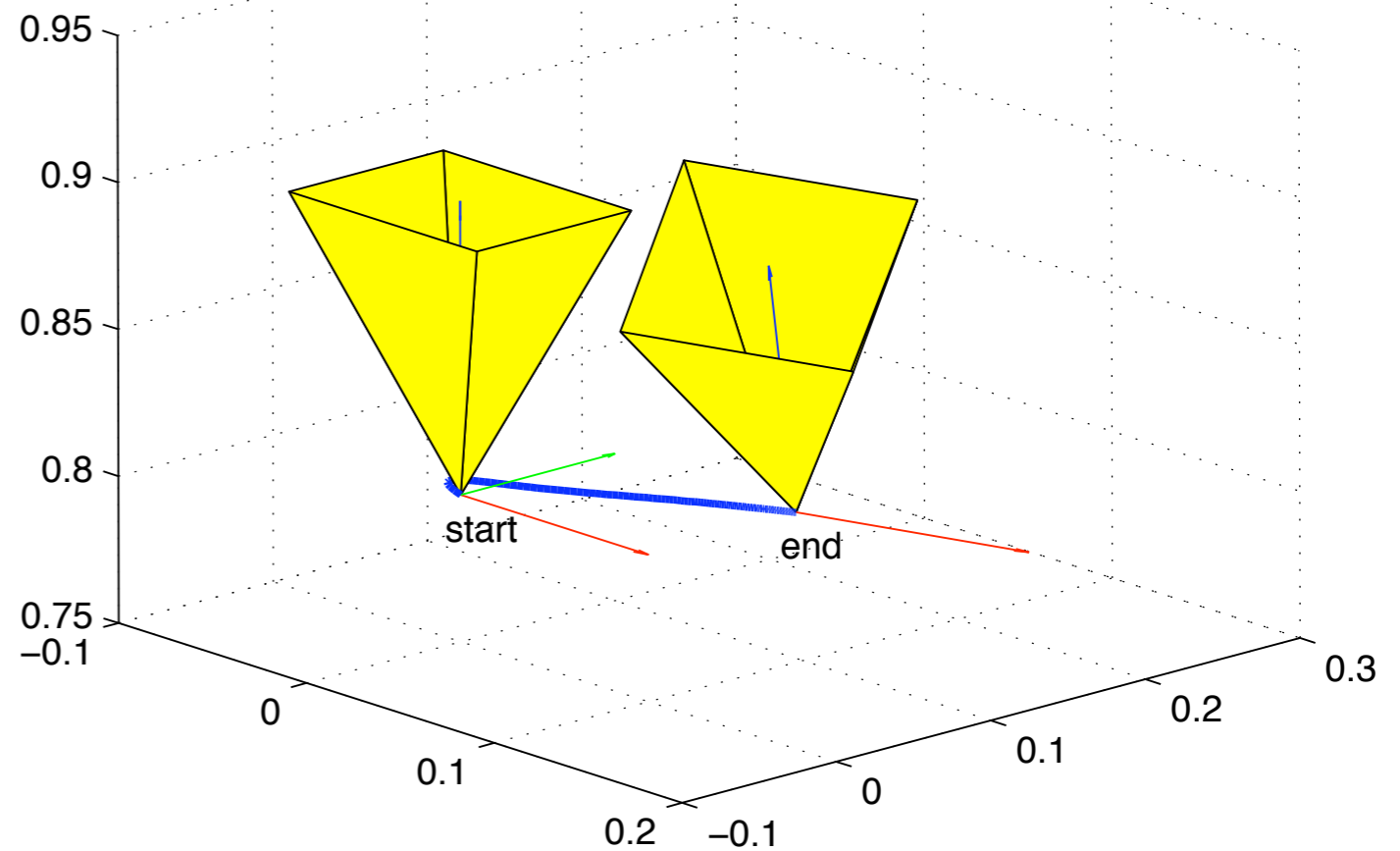
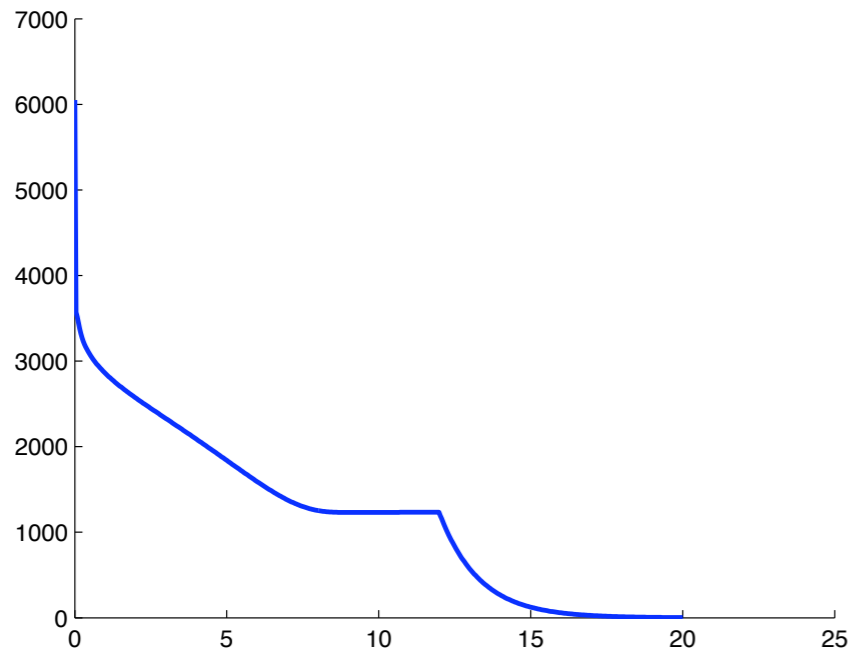
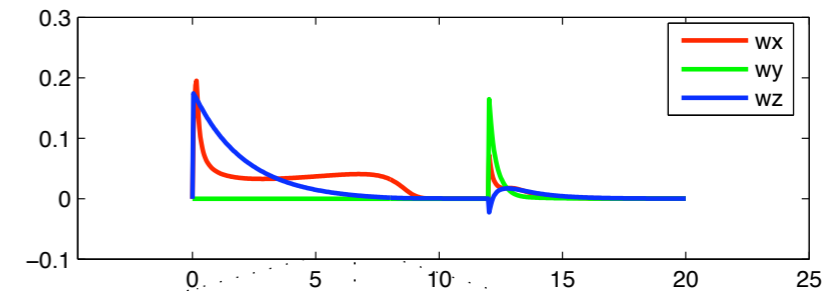
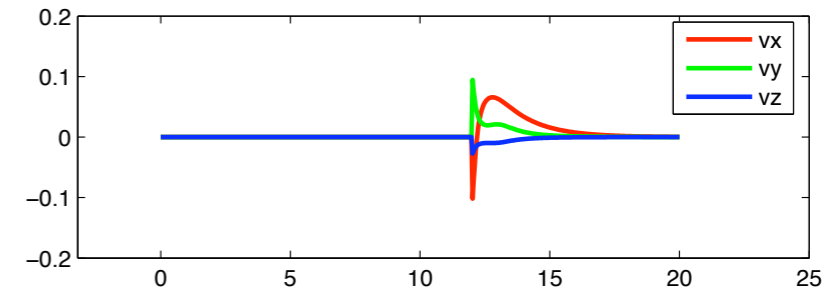
# Results

- Correspondence-less servoing.



# Results

- Correspondence-less servoing.
- Straight Cartesian path.



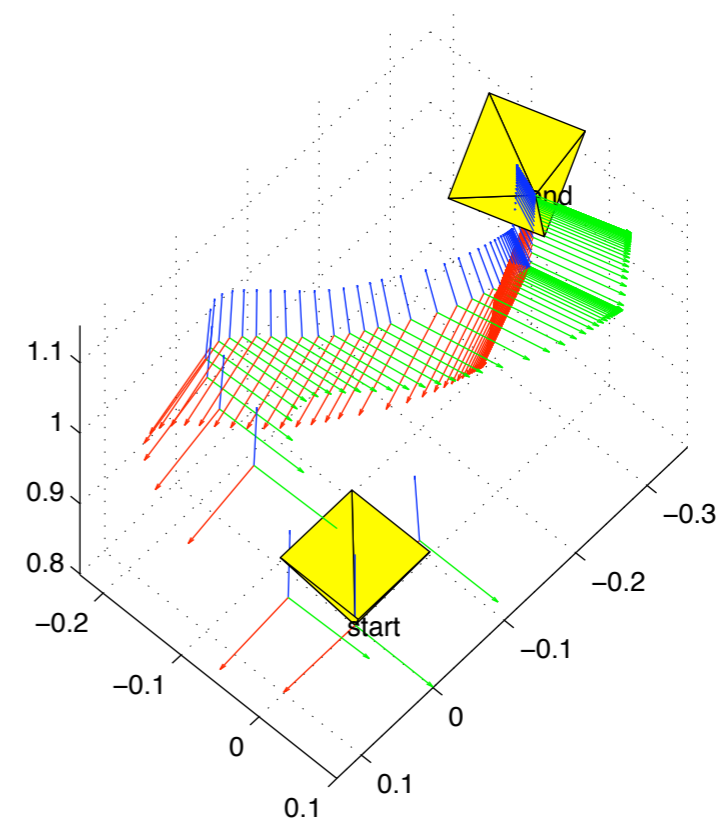
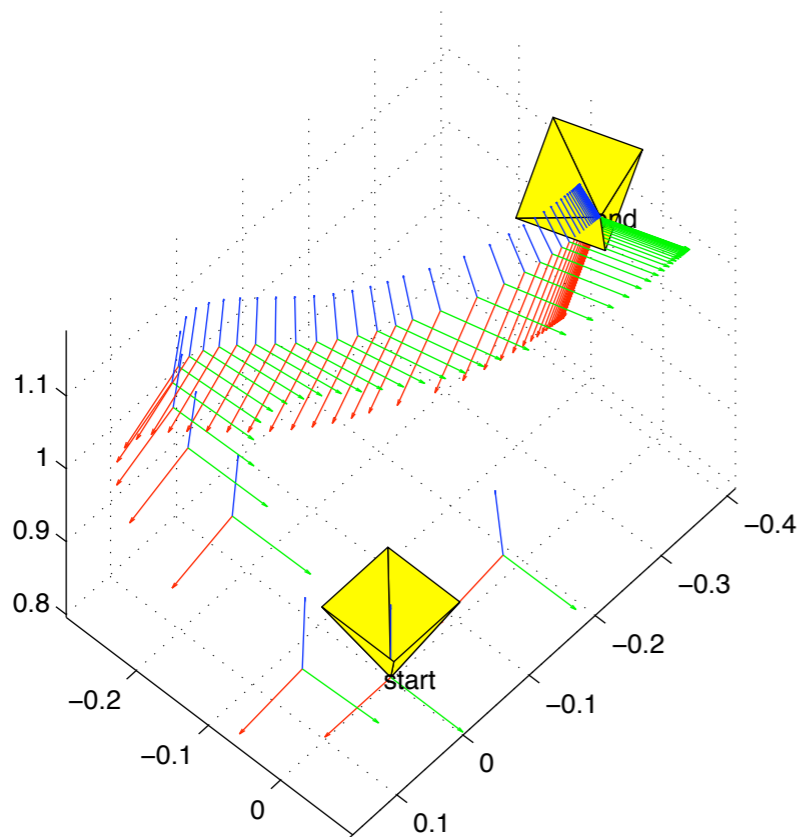


# Results

- Correspondence-less servoing.
- Straight Cartesian path.

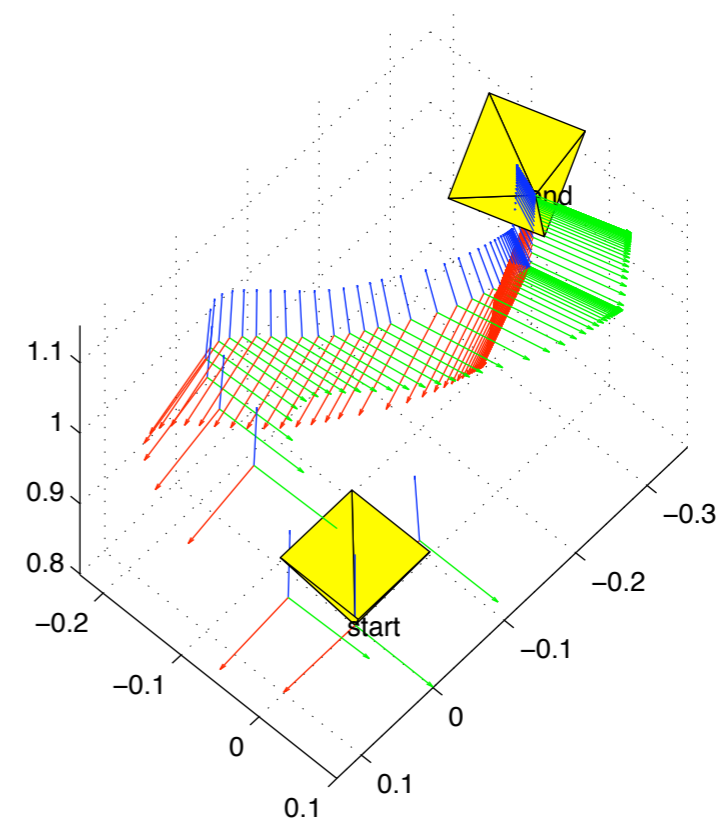
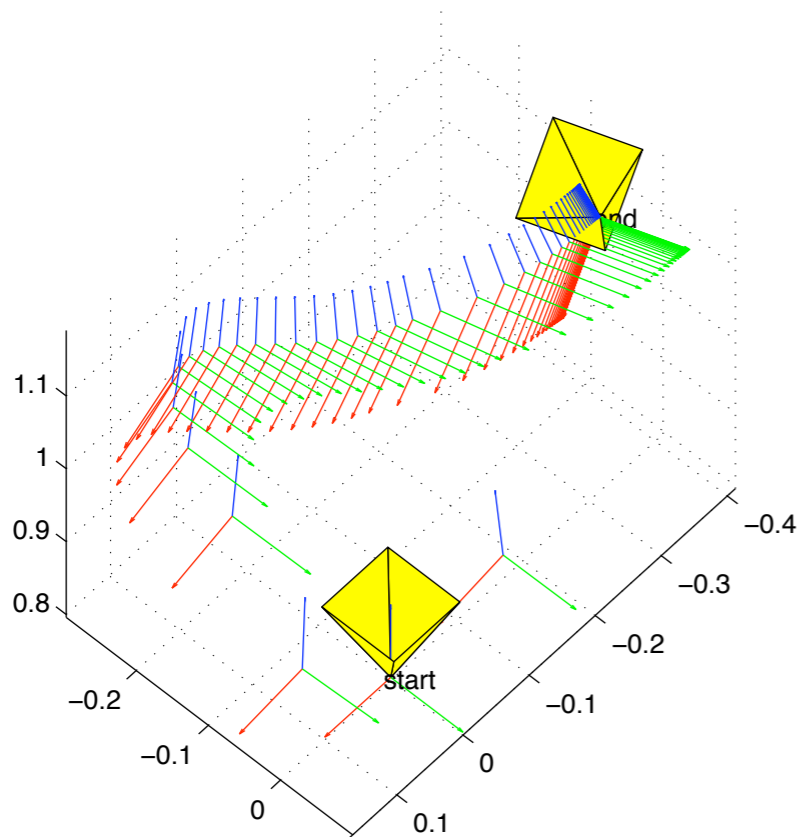
# Results

- Correspondence-less servoing.
- Straight Cartesian path.
- Path following.



# Results

- Correspondence-less servoing.
- Straight Cartesian path.
- Path following.





# Conclusions

- A visual servoing framework that uses Fourier based MVG is proposed.
- The proposed framework has several advantages, and 3 scenarios are presented to illustrate the same.
- Results for the 3 scenarios of correspondence-less servoing, Cartesian straight path servoing, and path following are shown.





# Symmetry results







# Symmetry Transfer

